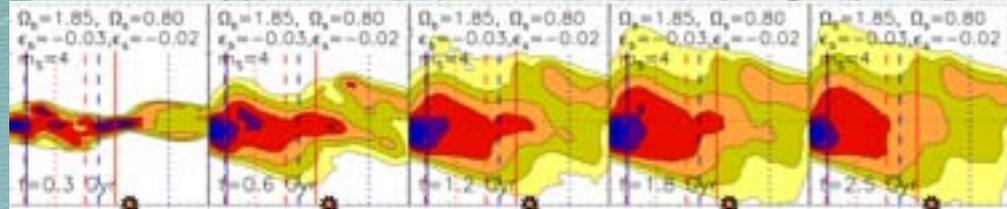


$$H \approx I_1^2 + I_1 \delta - \epsilon I_1^{1/2} \cos \phi - \beta I_1^{1/2} \cos[\phi + \nu t + \gamma]$$



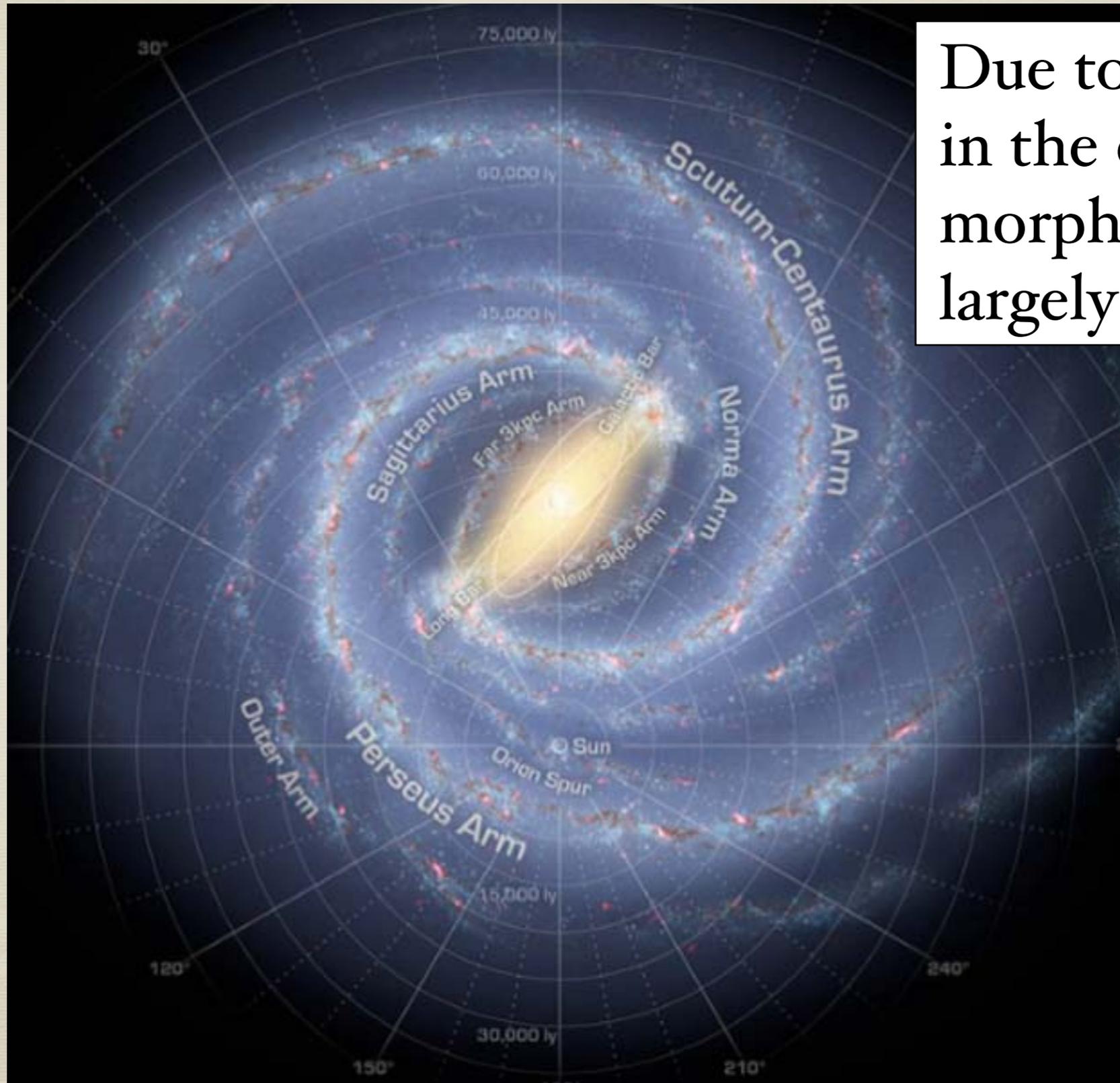
Galaxy simulations in the Gaia era

Ivan Minchev
 Leibniz-Institut für
 Astrophysik Potsdam (AIP)



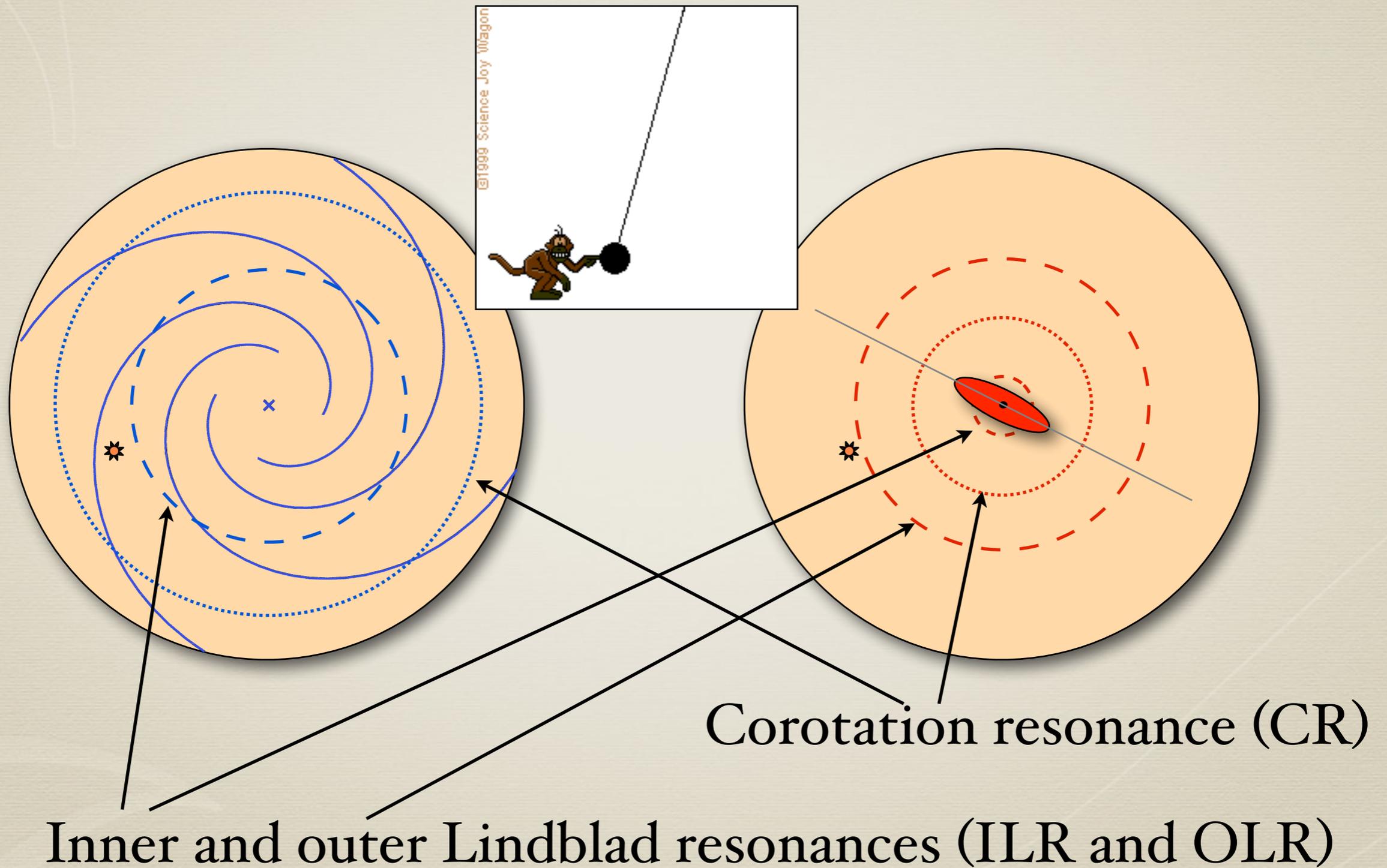
Leibniz-Institut für
 Astrophysik Potsdam

What we think our Galaxy looks like



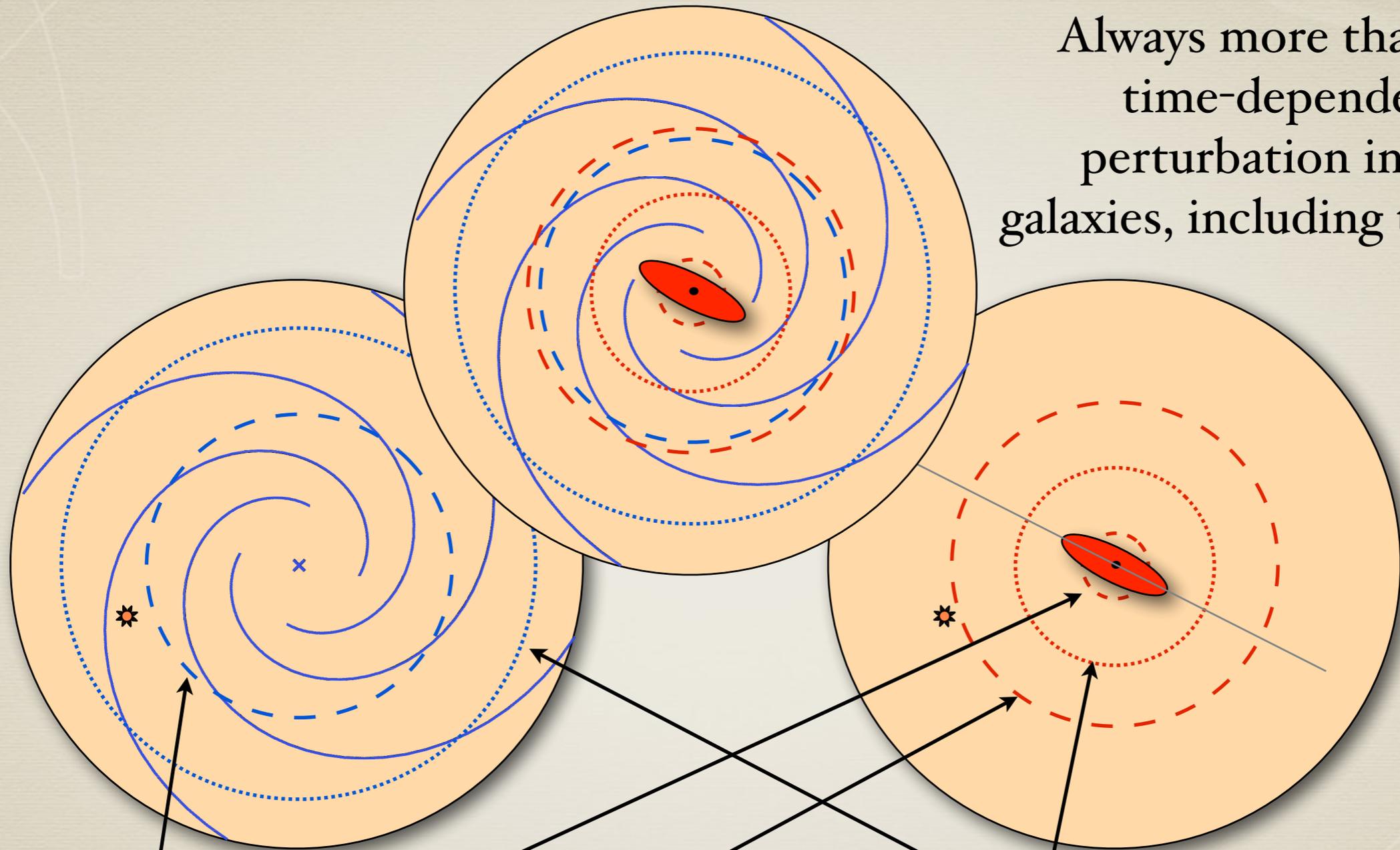
Due to our position in the disk, its morphology is still largely unknown

Resonances in galactic disks



Resonances in galactic disks

Always more than one
time-dependent
perturbation in disk
galaxies, including the MW



Inner and outer Lindblad resonances (ILR and OLR)

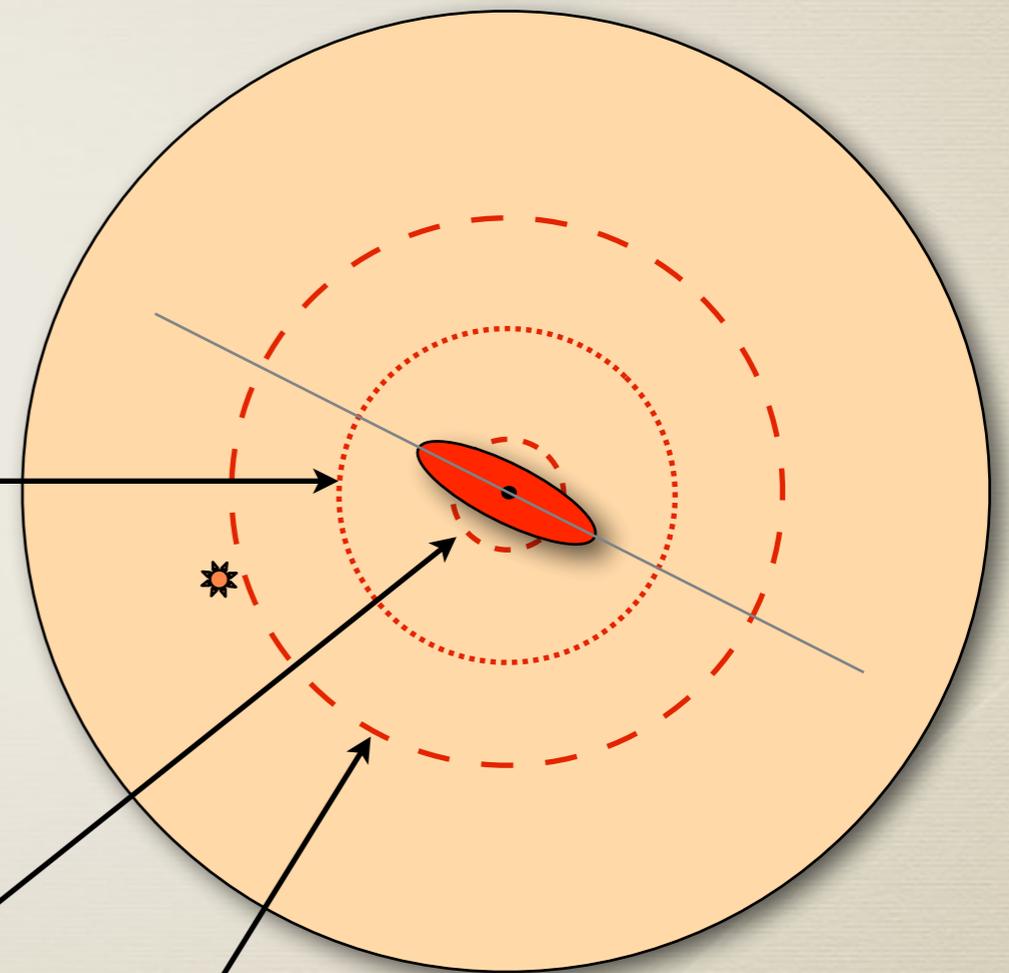
Corotation resonance (CR)

Resonances in galactic disks

- For a flat rotation curve Lindblad resonances are given by

$$\Omega_s = \Omega_0 \pm \kappa / m$$

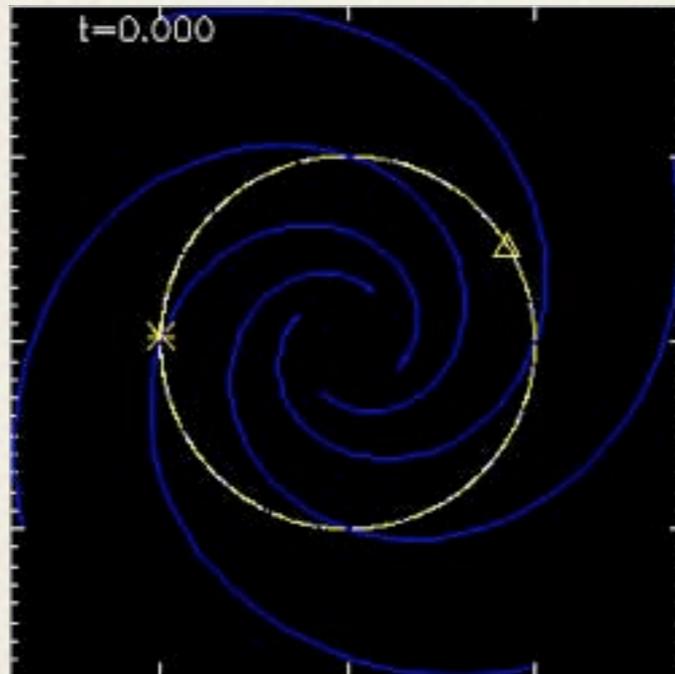
- Corotation is at $\Omega_s = \Omega_0$
- For a 2-armed spiral structure or a bar $m=2$.
- For a 4-armed spiral $m=4$.



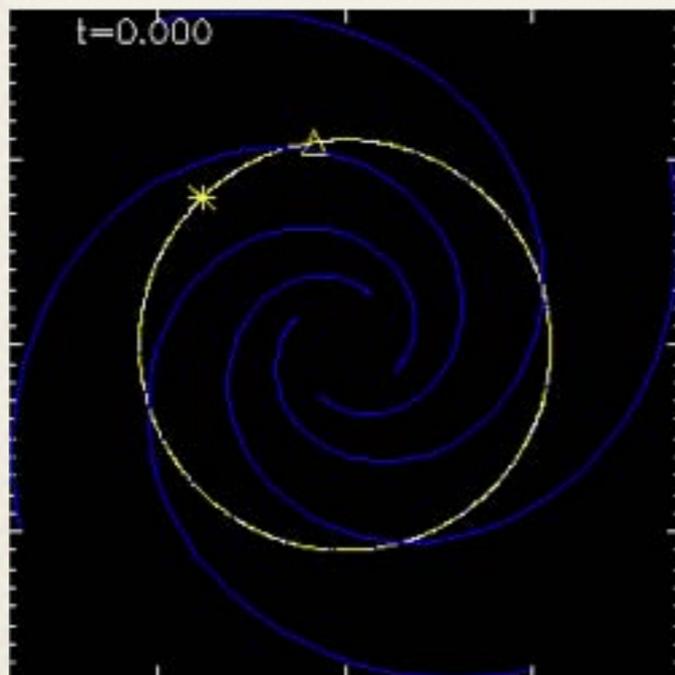
Inner and Outer Lindblad resonances

Stellar orbits near resonances

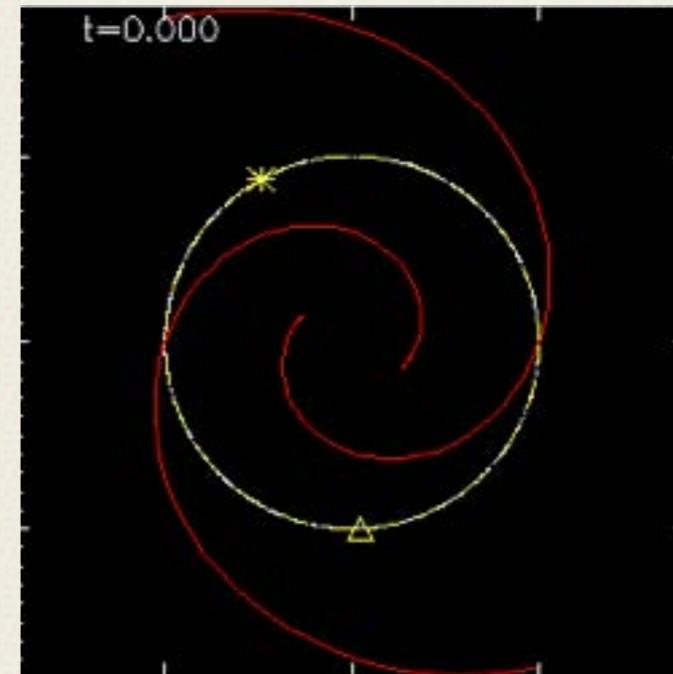
Near OLR



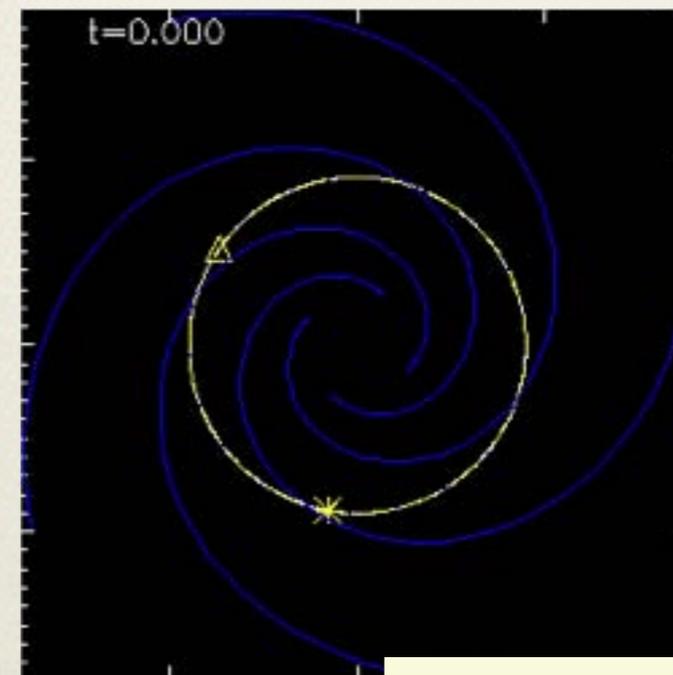
Outside OLR+CR



Near Corotation (CR)



Inside OLR+CR

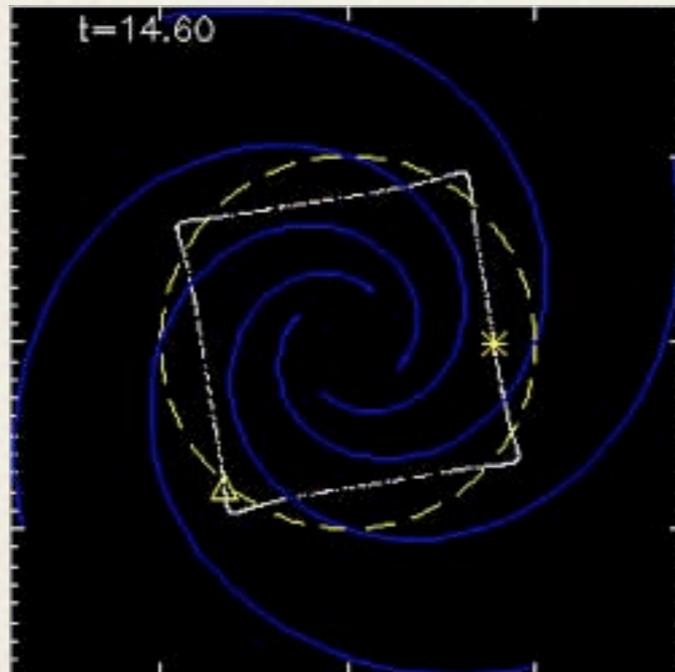


Single spiral
wave

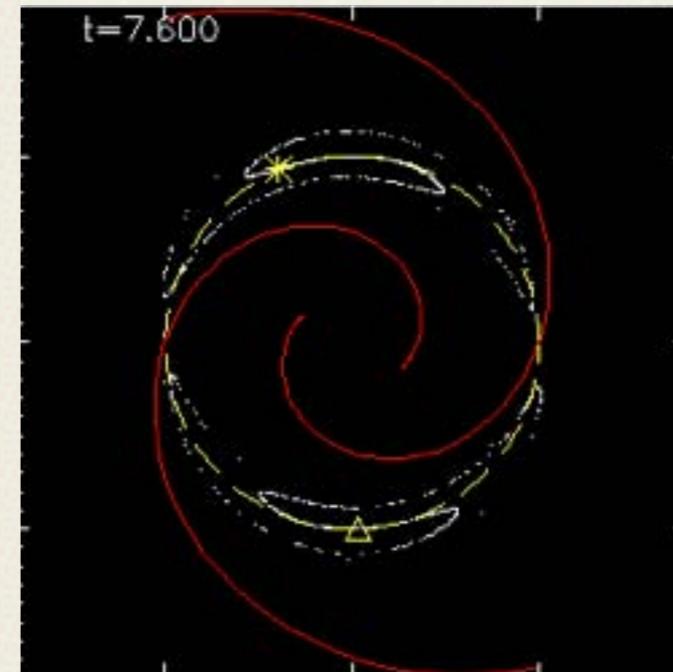
2 spiral
waves

Stellar orbits near resonances

Near OLR

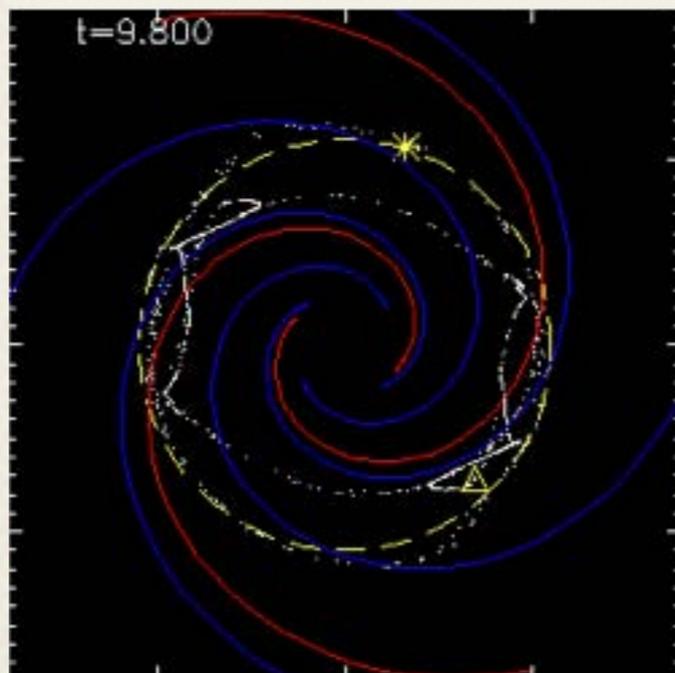


Near Corotation (CR)

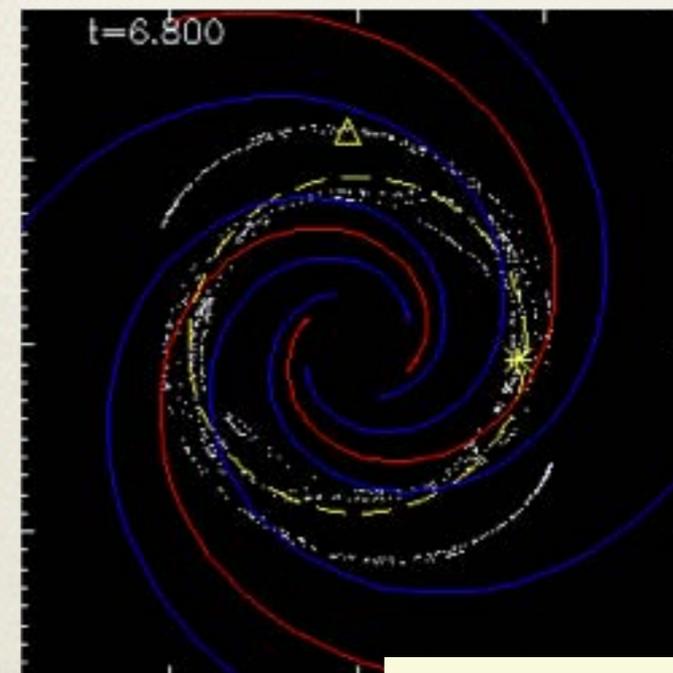


Single spiral
wave

Outside OLR+CR



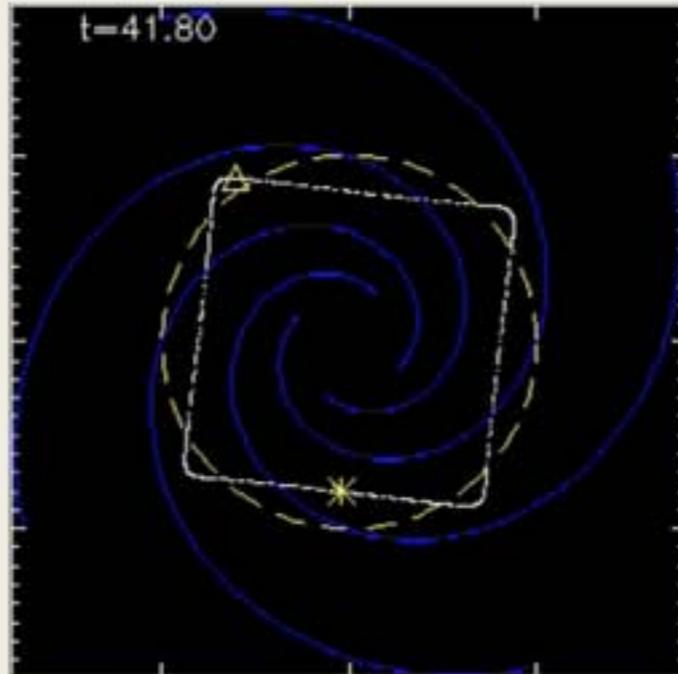
Inside OLR+CR



2 spiral
waves

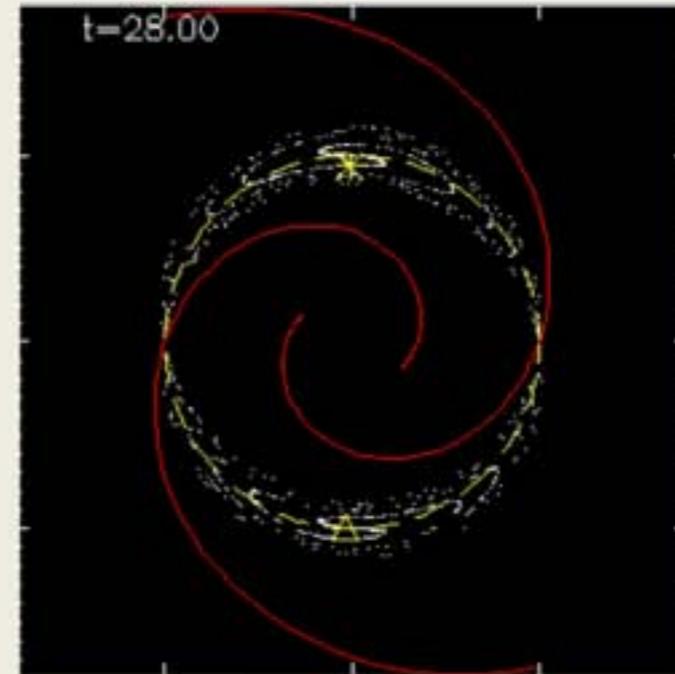
Stellar orbits near resonances

Near OLR

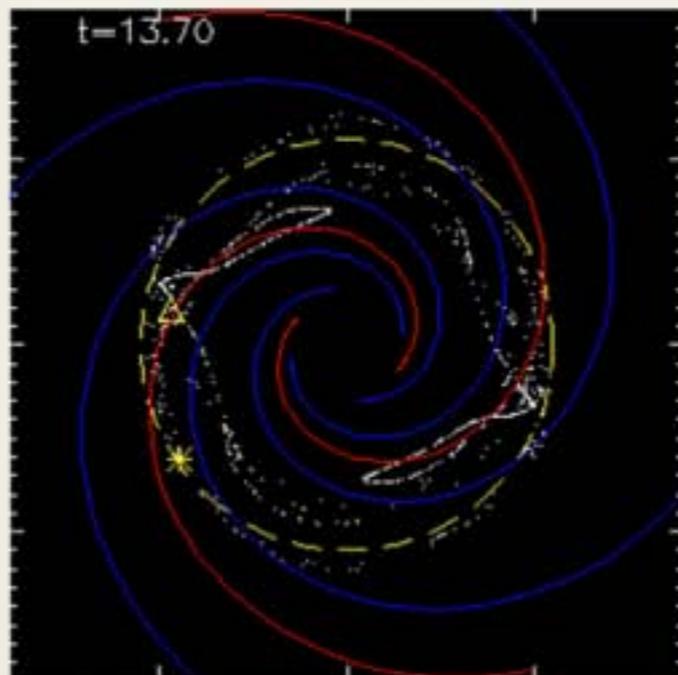


Single spiral wave

Near Corotation (CR)

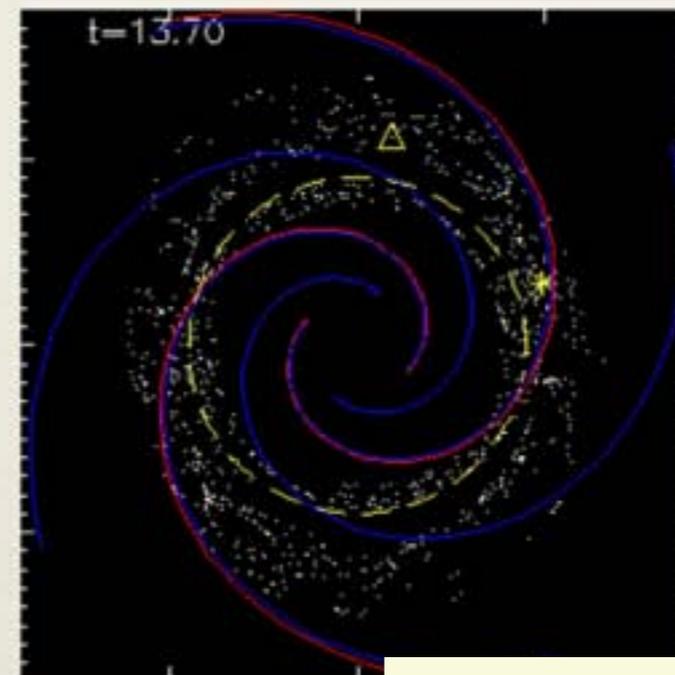


Outside OLR+CR



2 spiral waves

Inside OLR+CR



Much more complex dynamics when 2 perturbations with different pattern speeds

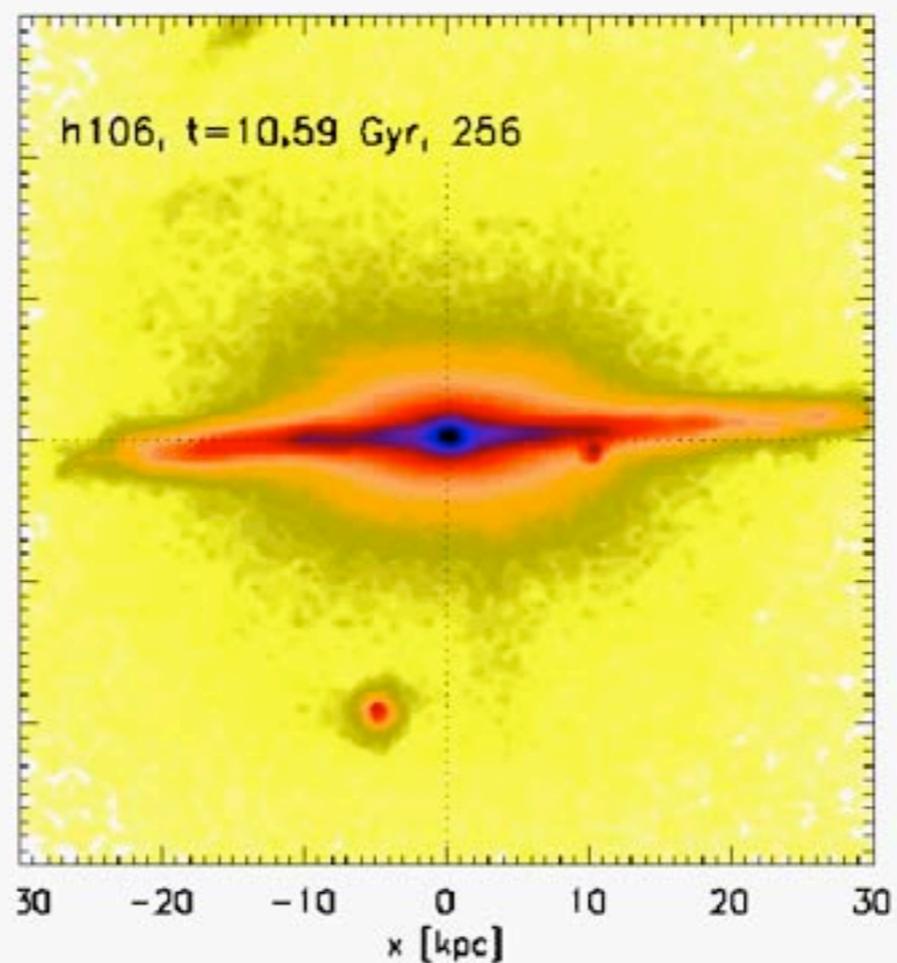
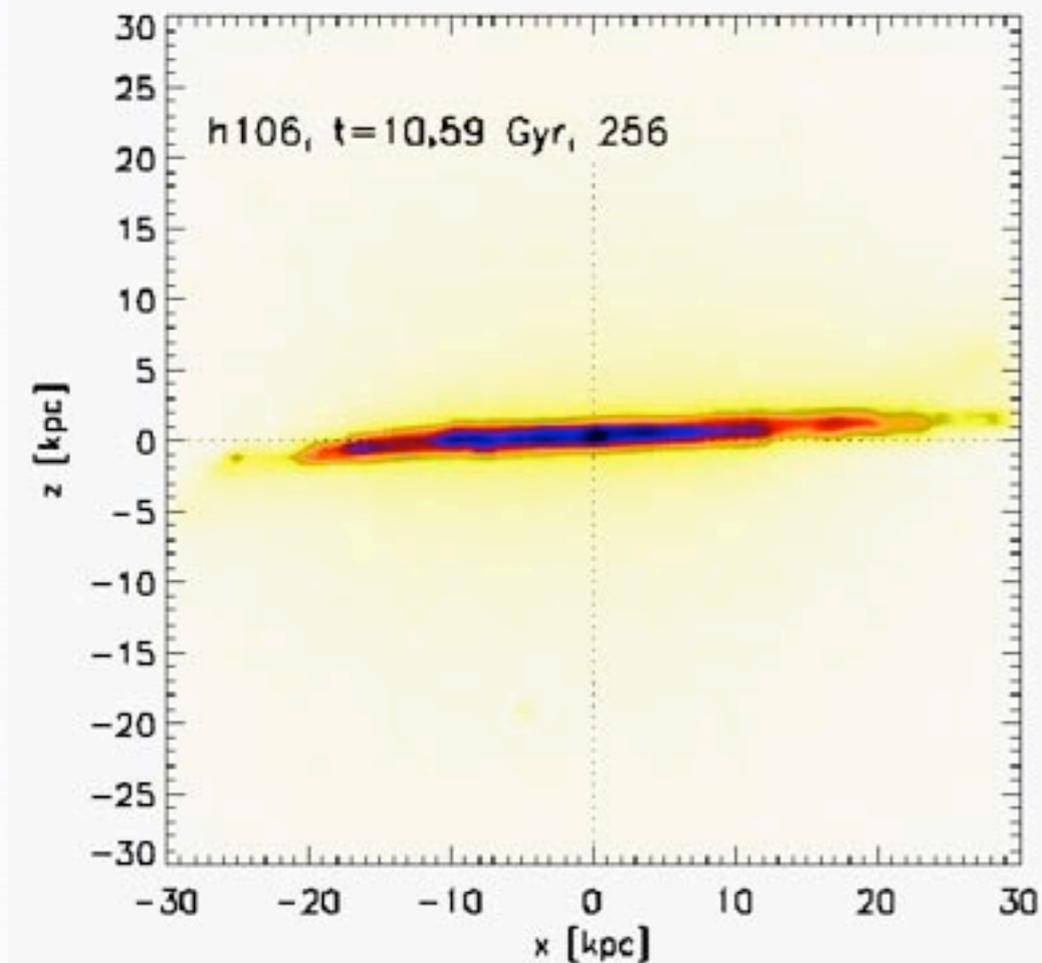
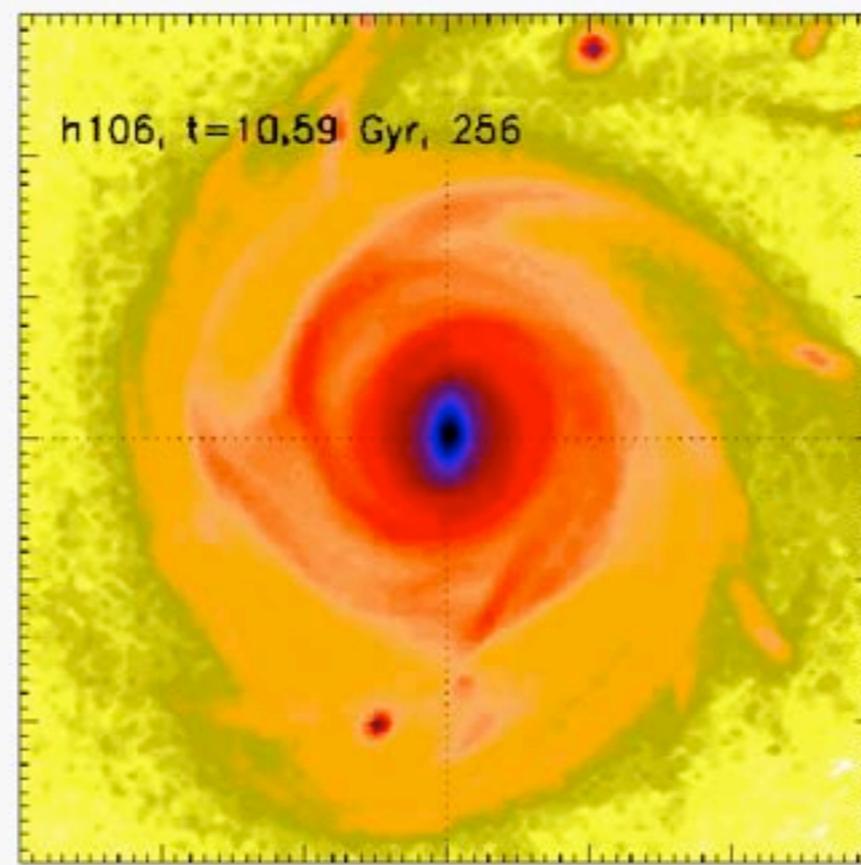
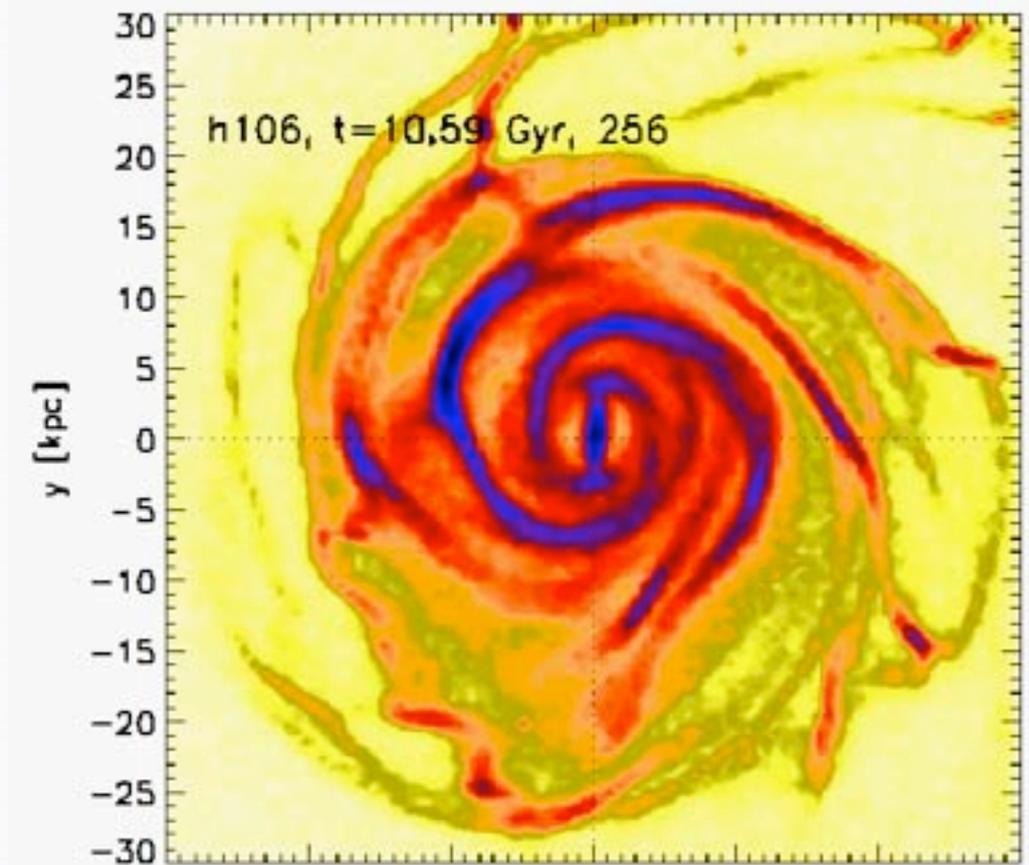
GAS

STARS

Simulation in
cosmological context
Martig et al. (2009, 2012)

Dynamics yet more
complex from a range
of perturbers acting at
the same time!

The disk is
perturbed by the
central bar, spirals,
and **infalling**
satellites.



The need for numerical simulations

- The complex dynamics of stars in the Galaxy **demands the use of N-body simulations**. This allows to take into account the perturbative **effect of spiral arms, central bar, and minor mergers** resulting from infalling satellites.

- **Questions we would like to answer:**

- Spiral structure parameters?
- Bar parameters?
- Bulge structure?
- Disk structure as a fn of radius and distance from plane?
- How did the Milky Way thick disk form?
- How/when did the bulge/bar form?
- How much radial mixing happened in the disk (fn of time and radius)?
- Inside-out disk formation?



describing current
disk state



requires a disk
formation model

A. Helmi will tell us about halo next

Some examples of outstanding problems

- Pattern speed and length of the Galactic bar and nature of the Hercules stream.

Fast bar, about 3 kpc long (Dehnen 2000, Fux et al. 2001, Minchev et al. 2007, 2010, Antoja et al. 2008, Monari et al. 2017)

Slow bar, about 5 kpc long (Wegg et al. 2015, Pérez-Villegas 2017)

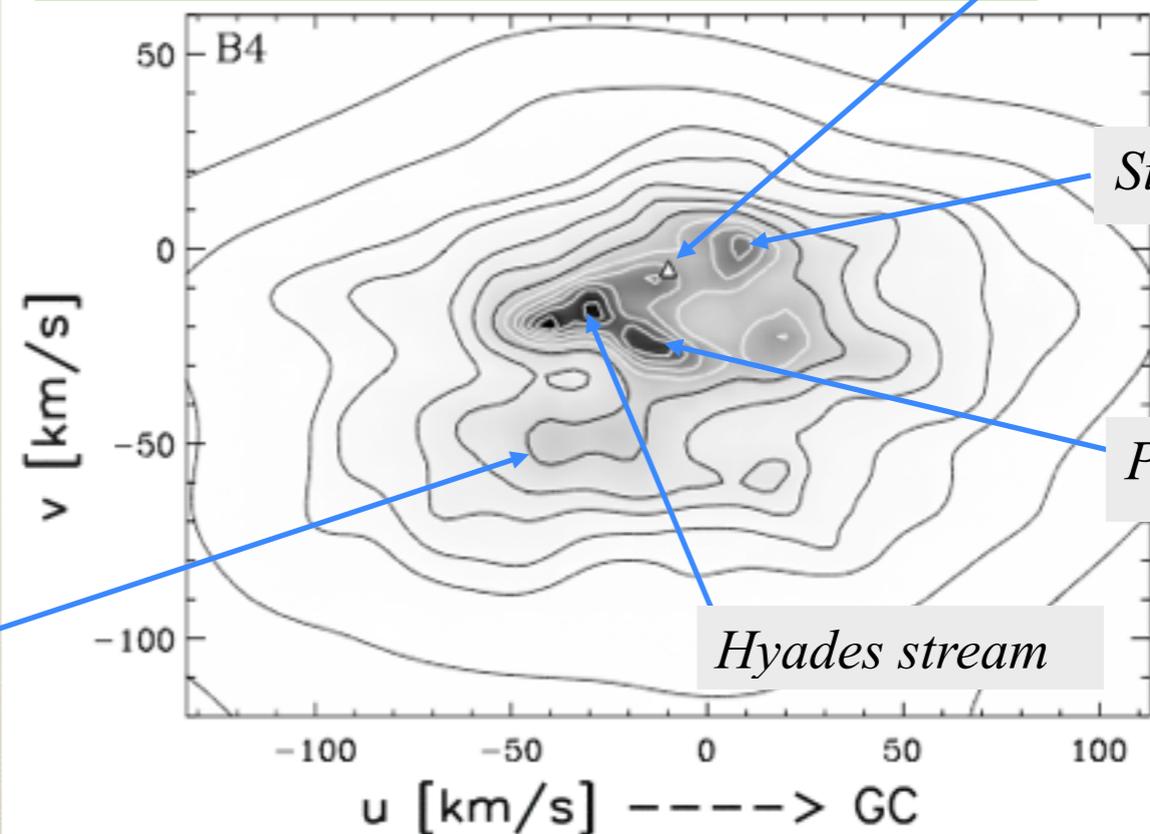
or

Outer Lindblad Resonance
or Corotation gives rise to
the Hercules stream?

Neither?

Hercules stream

Stellar velocity distribution, Dehnen (1998)



Coma Berenices group

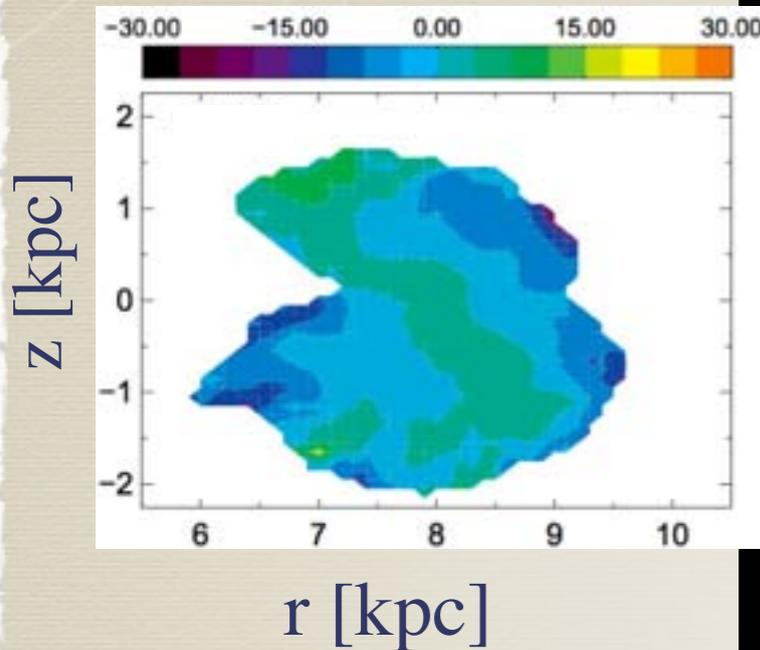
Sirius group

Pleiades group

Hyades stream

Some examples of outstanding problems

- What is the nature of the vertical wave patterns seen in the Milky Way disk?

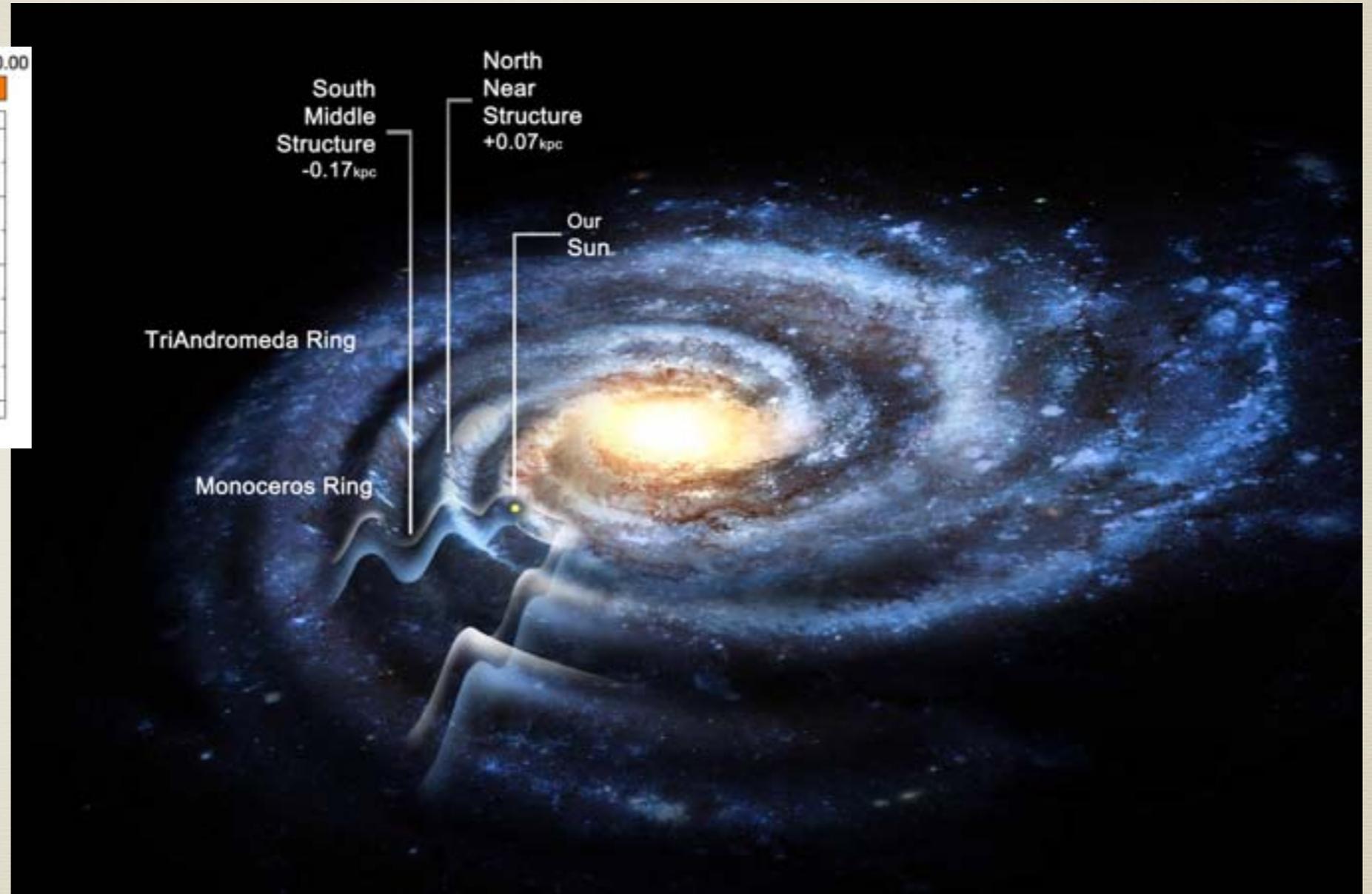


Willams + RAVE (2013)

First reported from SEGUE G-dwarfs by Widrow et al. (2012)

Also seen in LAMOST data

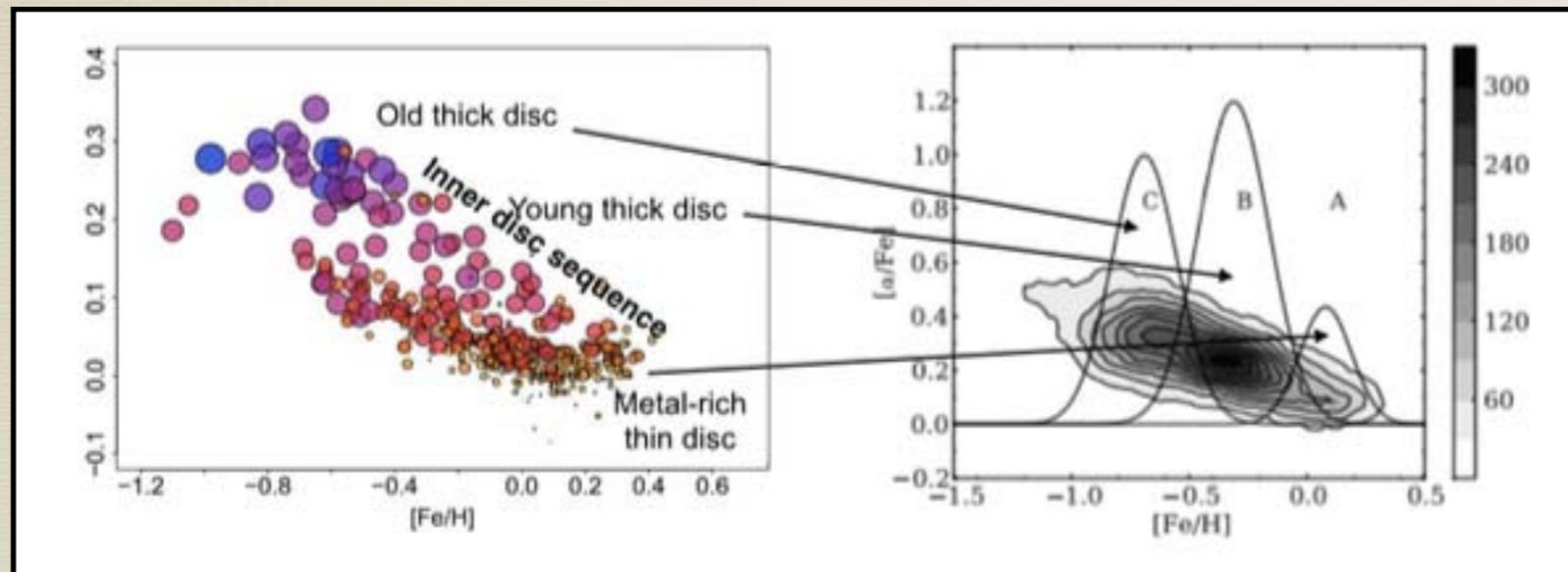
(Carlin et al. 2013)



- Are the local vertical disk asymmetries and Monoceros Ring part of the same global structure?
- Caused by bar/spirals or Sgr dwarf?

Some examples of outstanding problems

- **Bulge formation:** Inward stellar migration gives rise to different stellar populations in the bulge?



Di Matteo (2016)

Local HARPS Adibekyan

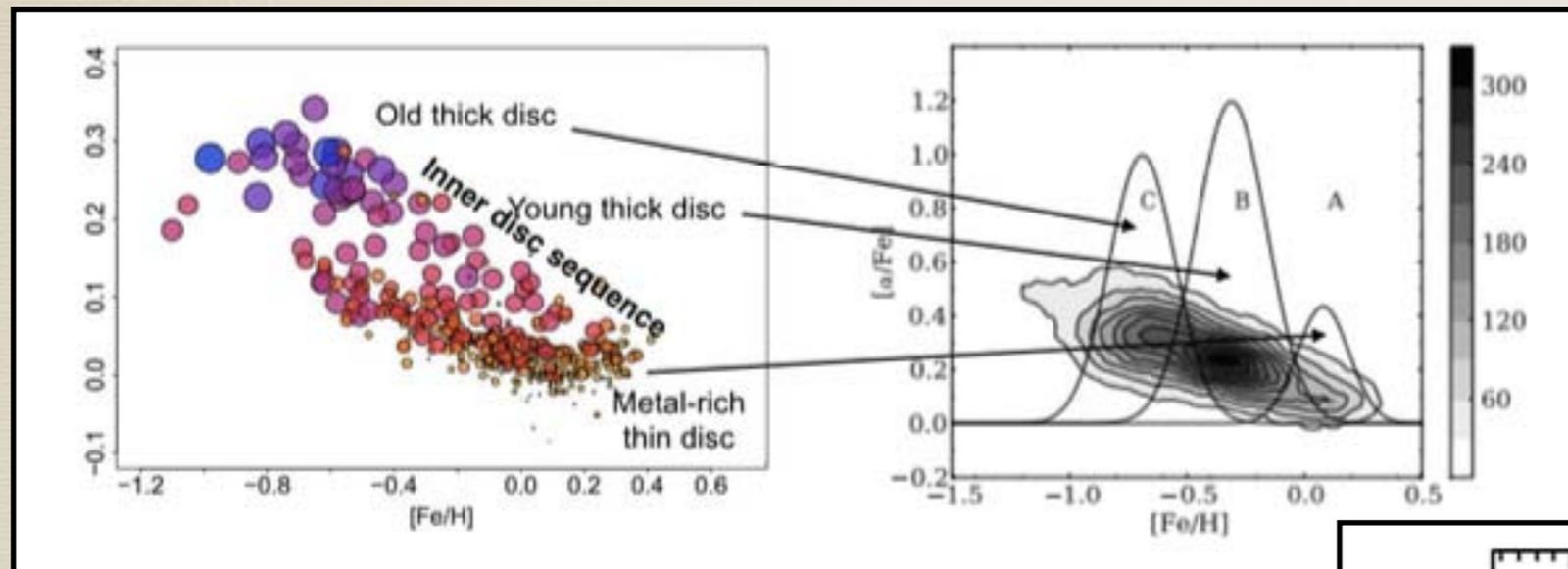
sample Haywood et al. (2013)

ARGOS bulge data

Ness et al. (2014)

Some examples of outstanding problems

- **Bulge formation:** Inward stellar migration gives rise to different stellar populations in the bulge?



Di Matteo (2016)

Local HARPS Adibekyan
sample Haywood et al. (2013)

ARGOS bulge data
Ness et al. (2014)

or

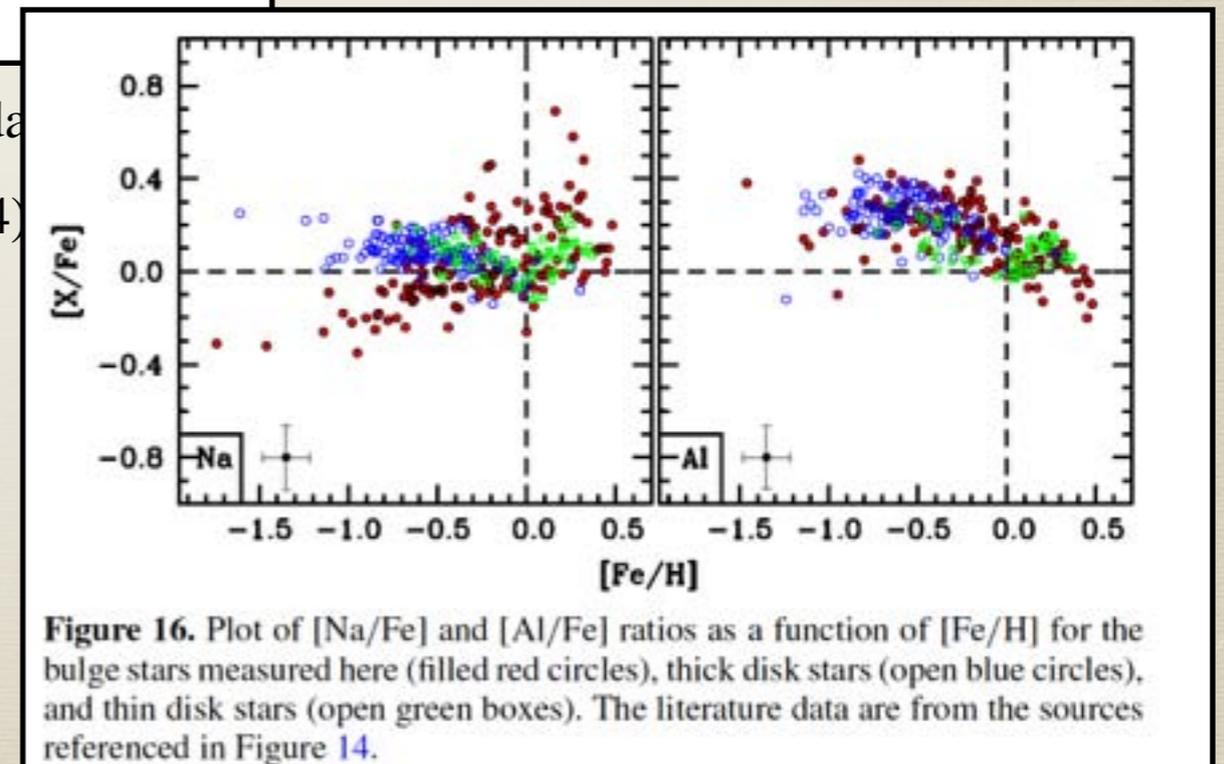


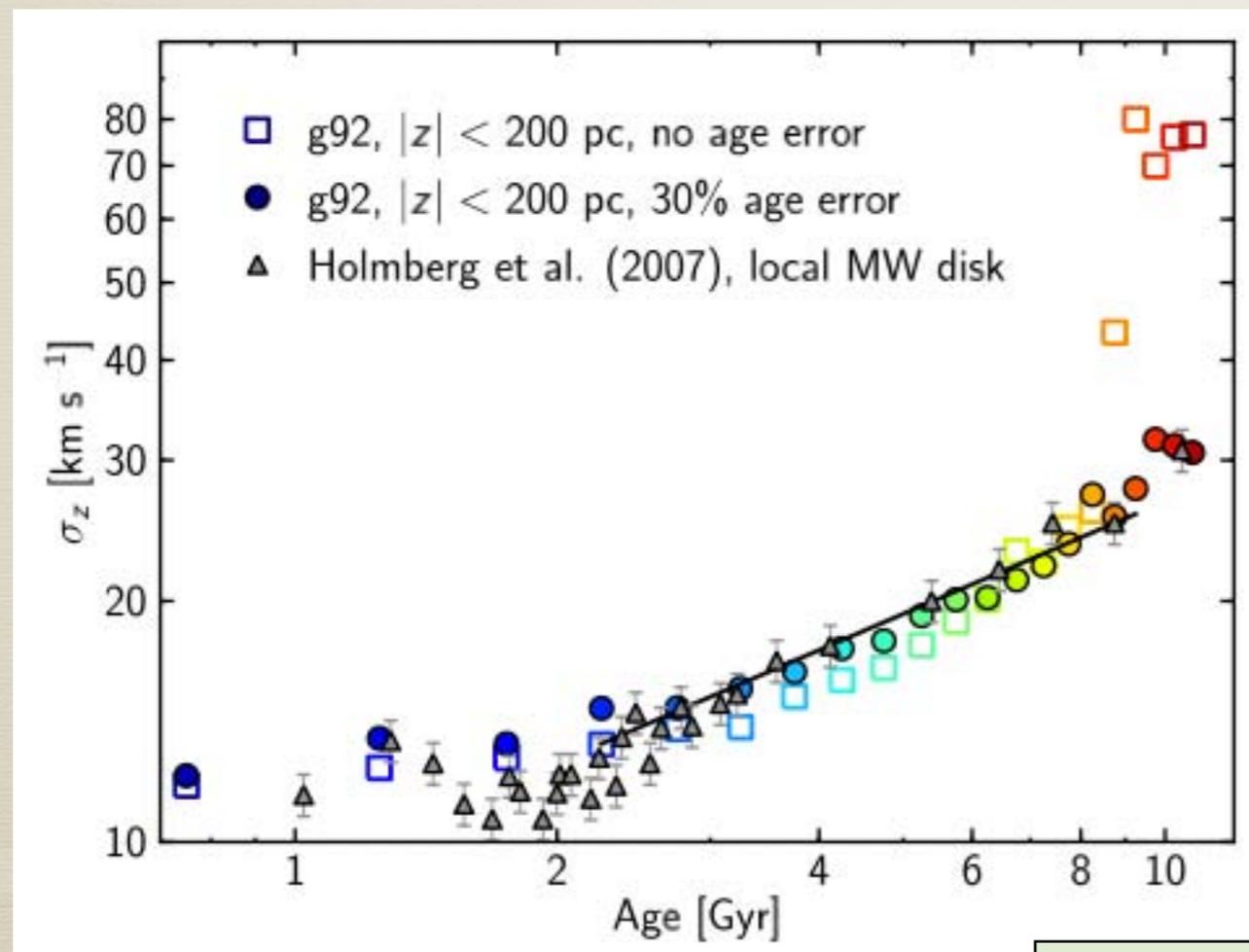
Figure 16. Plot of $[\text{Na}/\text{Fe}]$ and $[\text{Al}/\text{Fe}]$ ratios as a function of $[\text{Fe}/\text{H}]$ for the bulge stars measured here (filled red circles), thick disk stars (open blue circles), and thin disk stars (open green boxes). The literature data are from the sources referenced in Figure 14.

- Bulge chemistry distinct from that of the thick disk?

Johnson et al. (2014)

Some examples of outstanding problems

- **The age-velocity relation:** Increase of stellar velocity dispersion with age as a power law or a step at 8-10 Gyr from last massive merger?

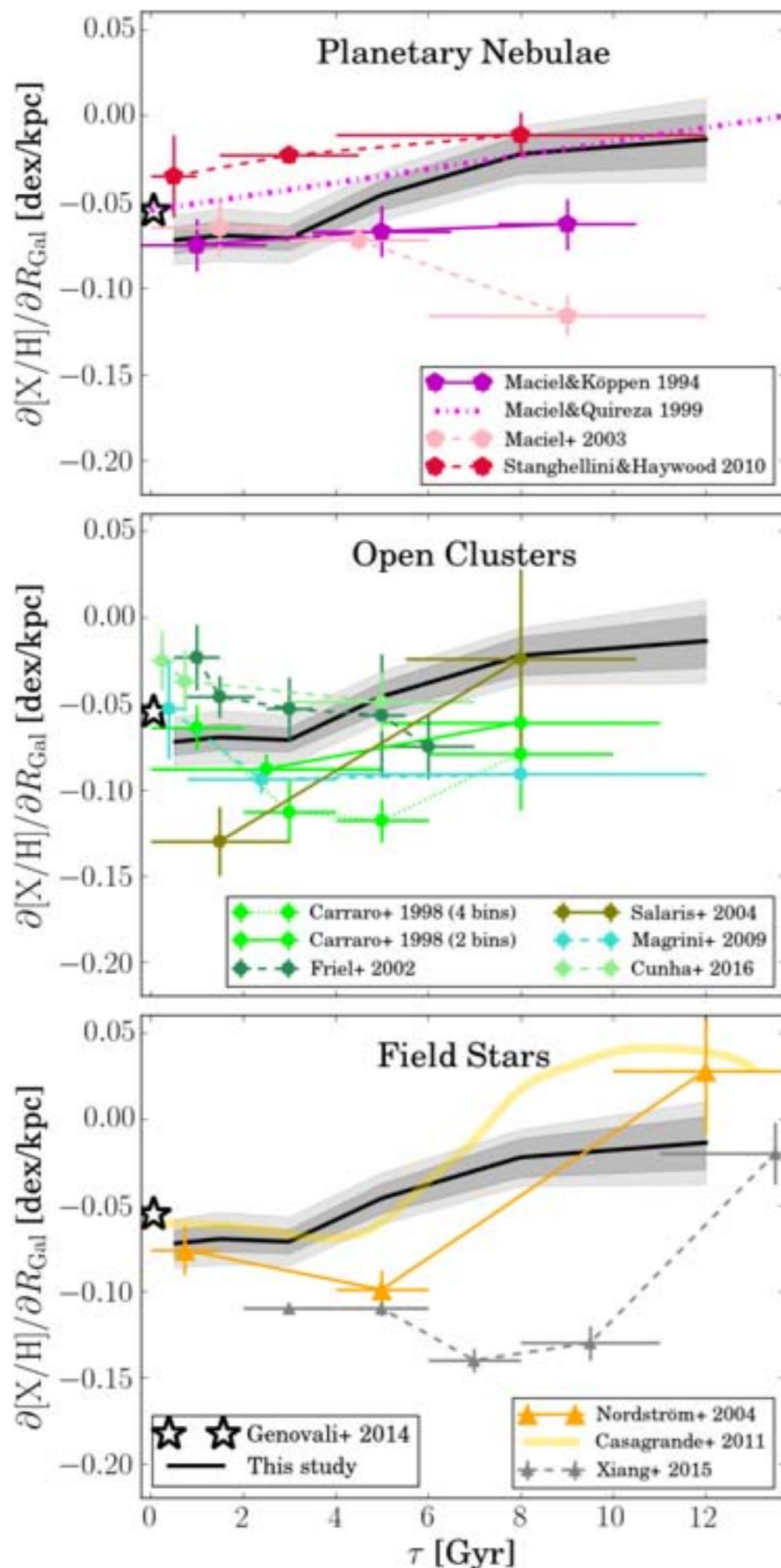


Step at 10 Gyr due to strong mergers.

Erased when 30% age errors convolved into simulated data.

Martig, Minchev and Flynn (2014b)

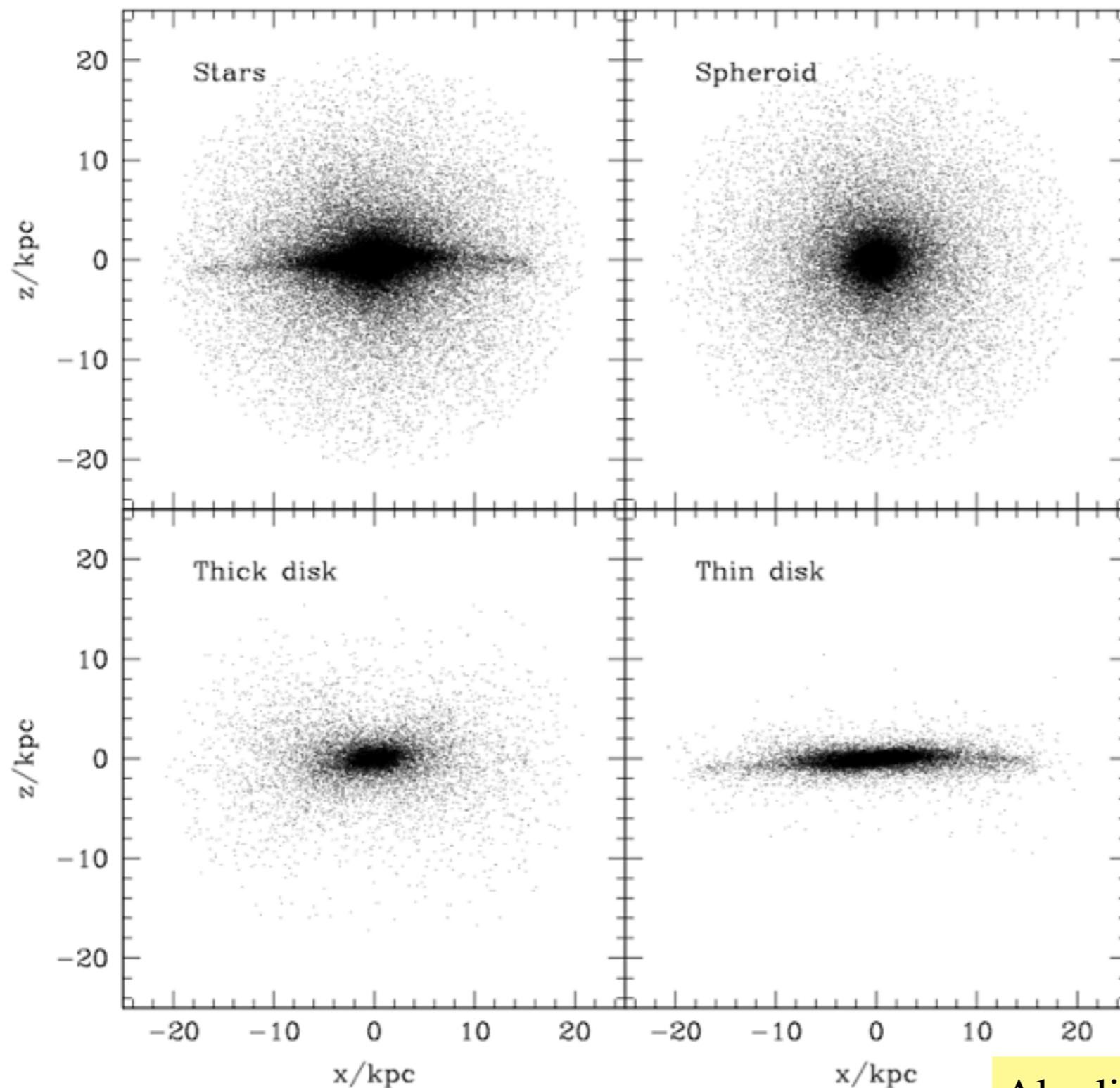
The time evolution of the radial metallicity gradient



- Using APOGEE abundances + CoRoT asteroseismic ages (CoRoTGEE sample)
- Mean gradient mostly constant over the past 5 Gyr
- Scatter caused by radial migration

Anders et al. (2016b)

Disk formation in cosmological simulations



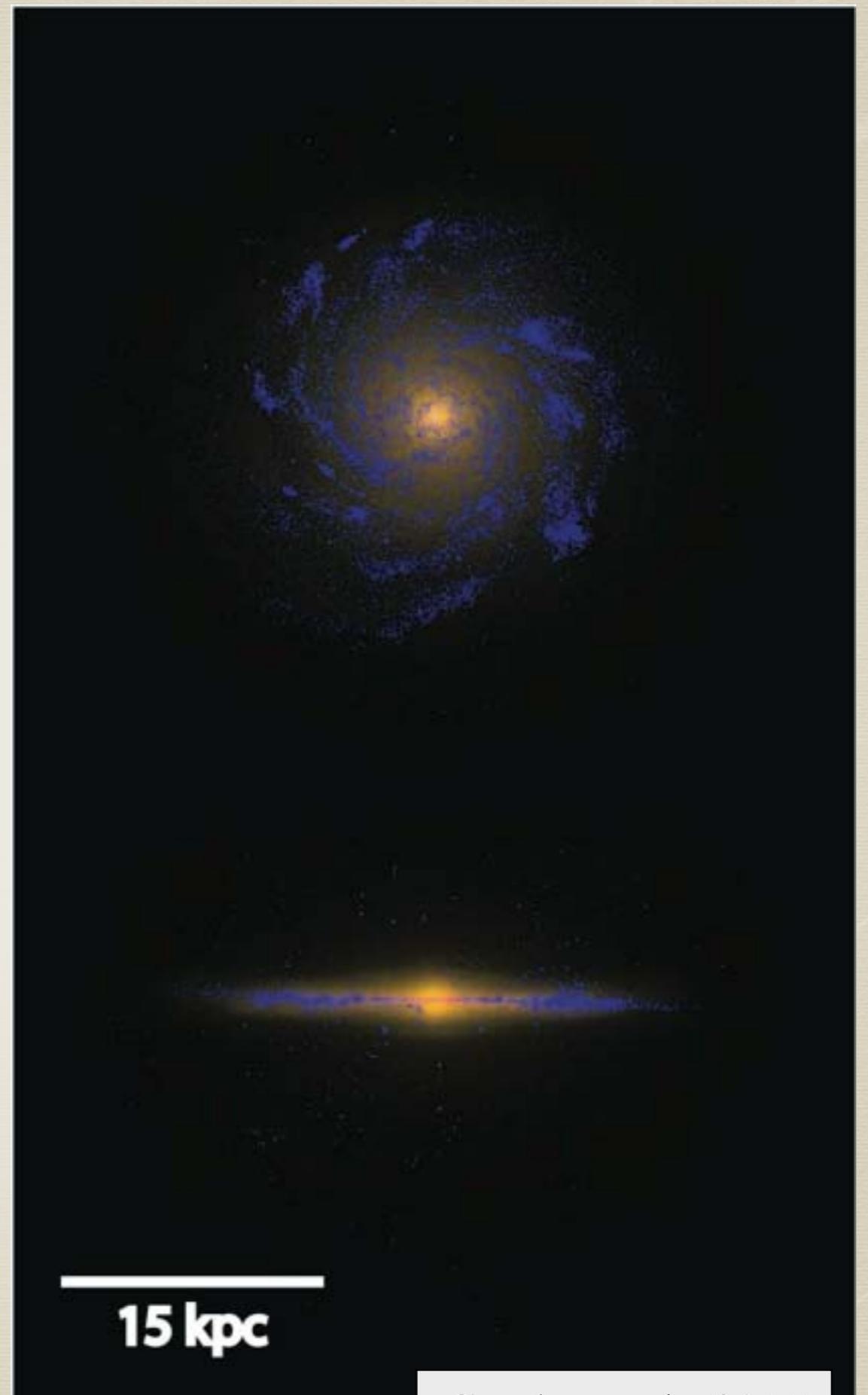
- Traditionally a challenge (e.g., Navarro and Benz 1991; Abadi et al. 2003):
- Extreme angular momentum loss during mergers.
- Overly-concentrated mass distributions and massive bulges.

Abadi et al. (2003)

Recent improvements

- Increase in resolution and better modeling of star formation and feedback produce **MW-mass galaxies with reduced bulge fractions** (e.g., Agertz et al. 2011; Guedes et al. 2011; Martig et al. 2012).
- However, no chemical treatment!

ERIS simulation

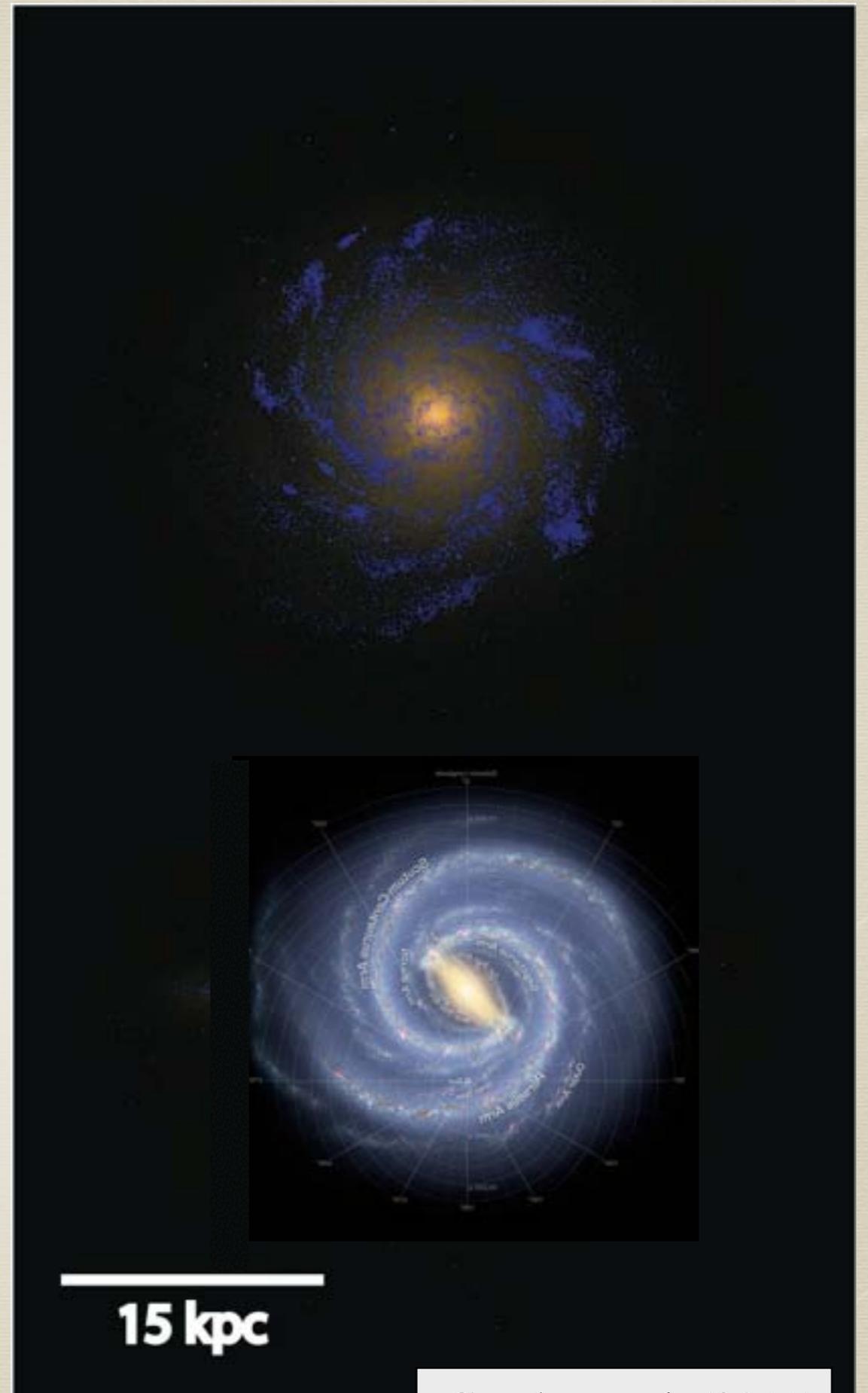


Guedes et al. (2011)

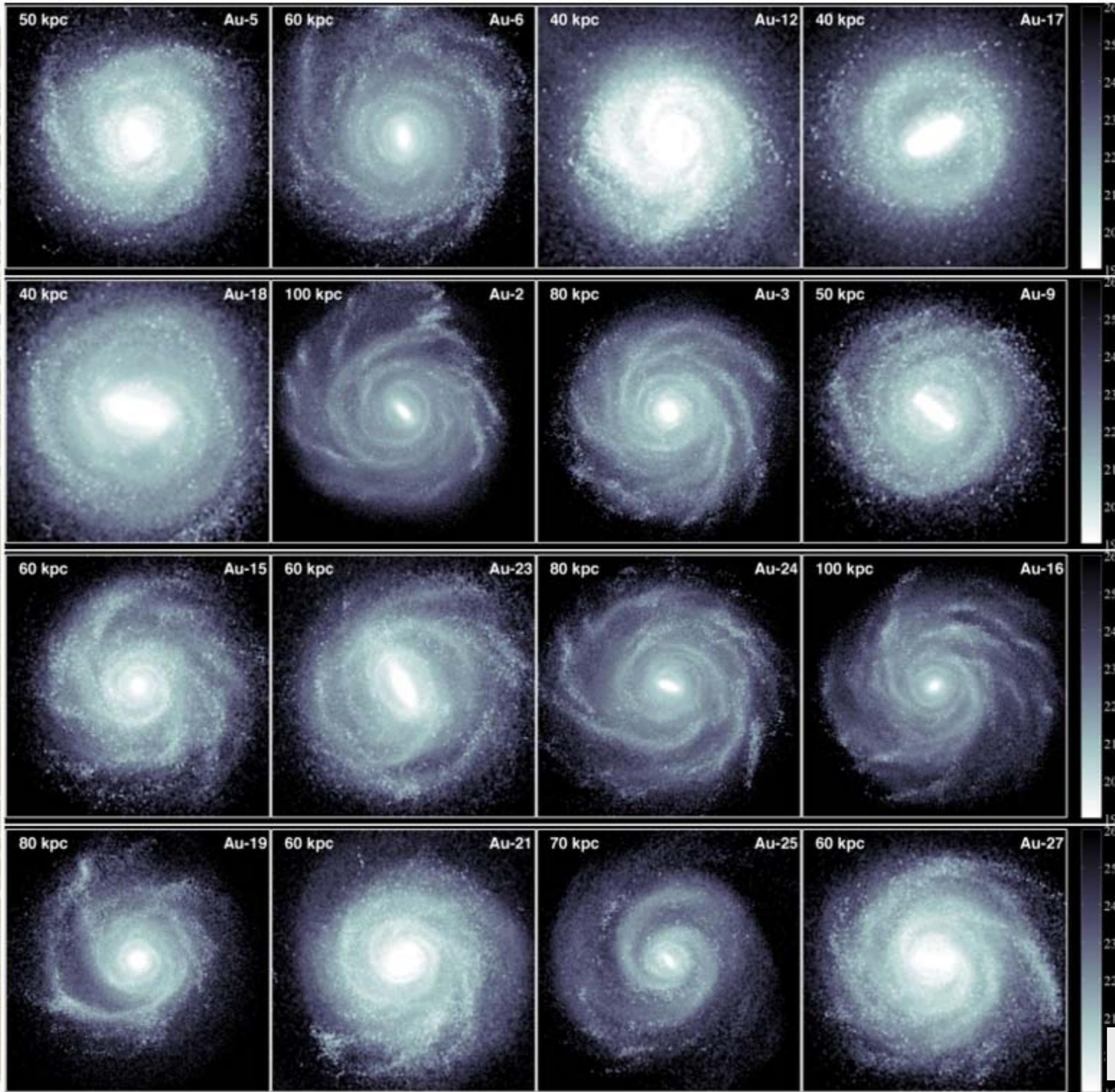
Recent improvements

- Increase in resolution and better modeling of star formation and feedback produce **MW-mass galaxies with reduced bulge fractions** (e.g., Agertz et al. 2011; Guedes et al. 2011; Martig et al. 2012).
- However, no chemical treatment!
- Milky Way disk morphology not easily reproducible in fully cosmological simulations.

ERIS simulation



Guedes et al. (2011)



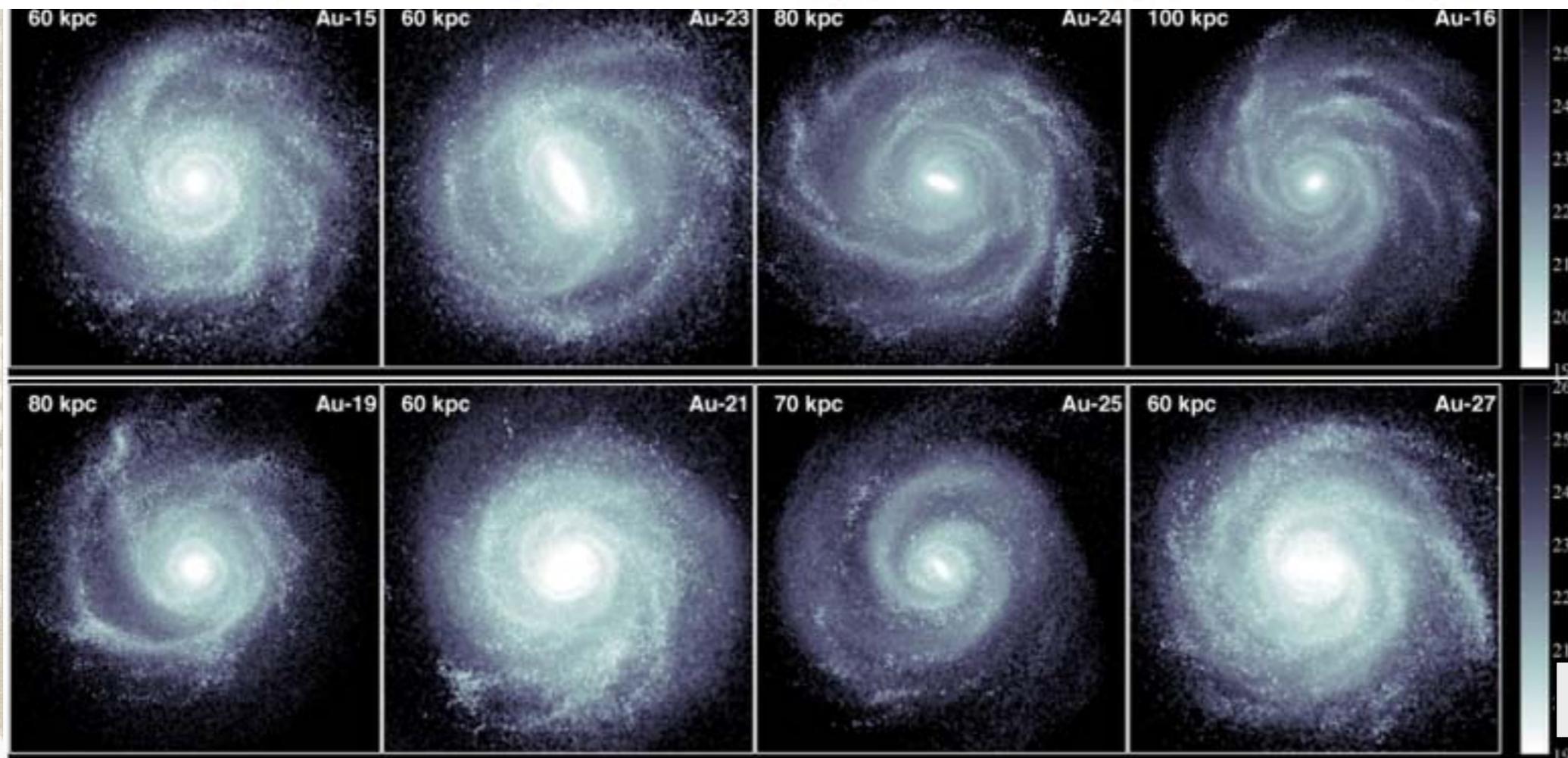
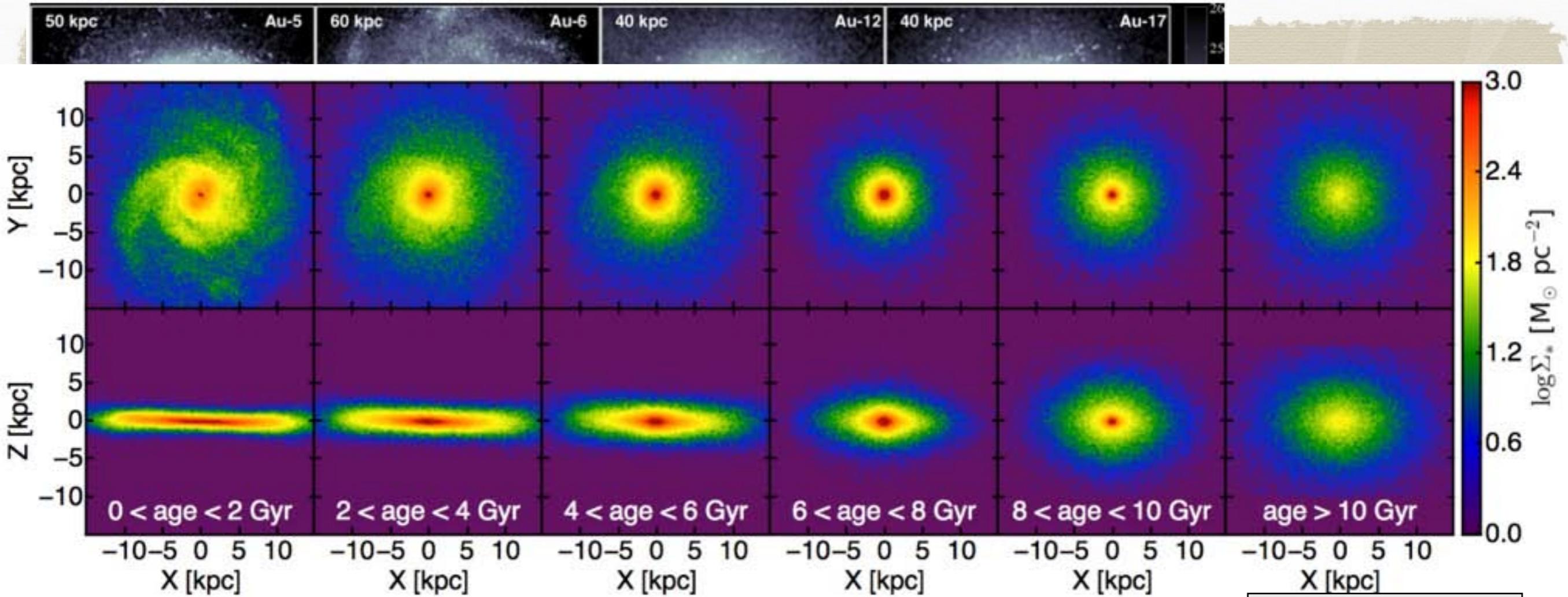
Auriga simulations

AREPO code

([Springel 2010](#),
[Vogelsberger et al. 2013](#),
[Marinacci et al. 2014](#))

~ $10^4 M_{\odot}$ resolution.
 369 pc spatial res.

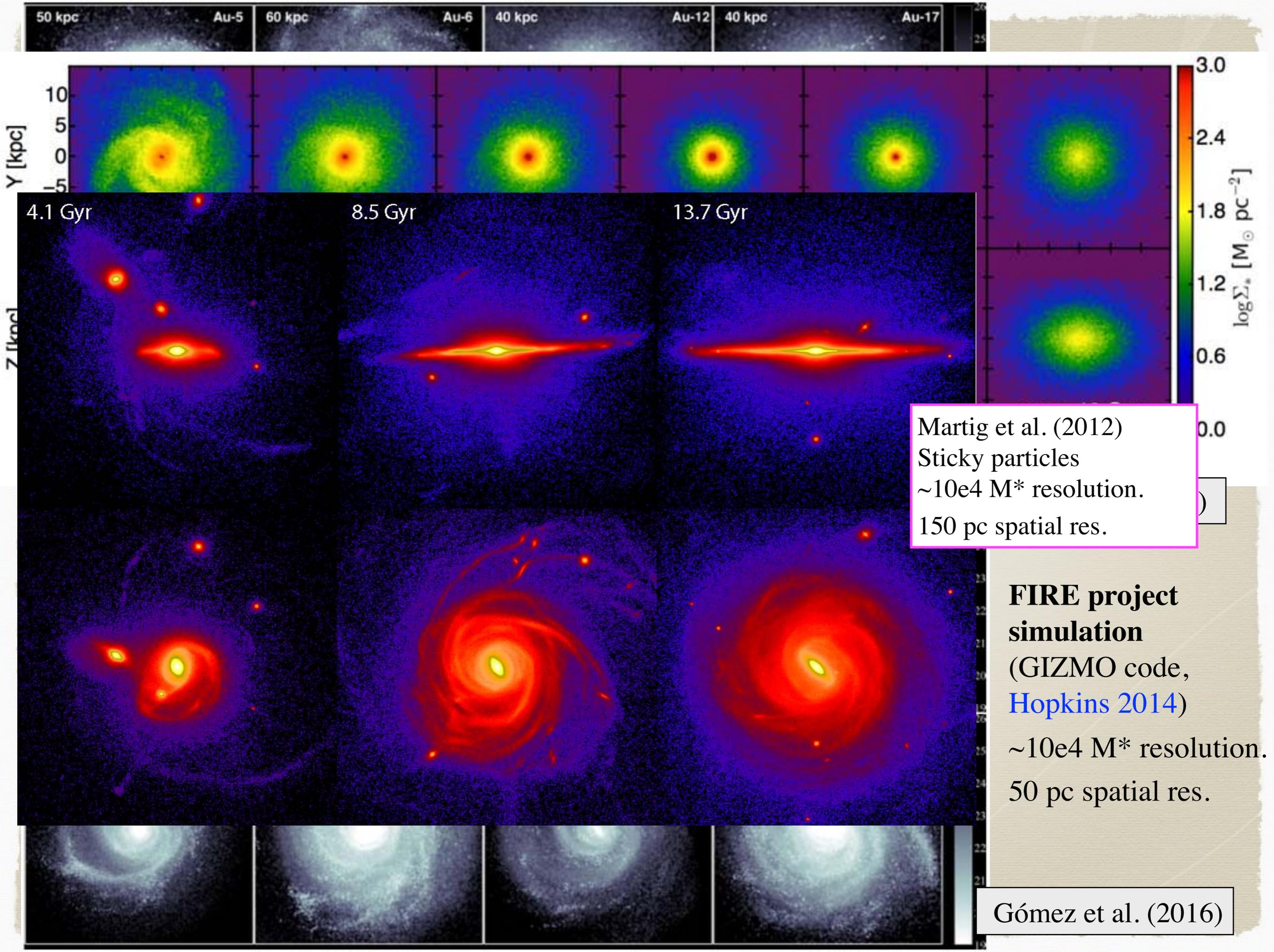
Gómez et al. (2016)



Ma et al. (2016)

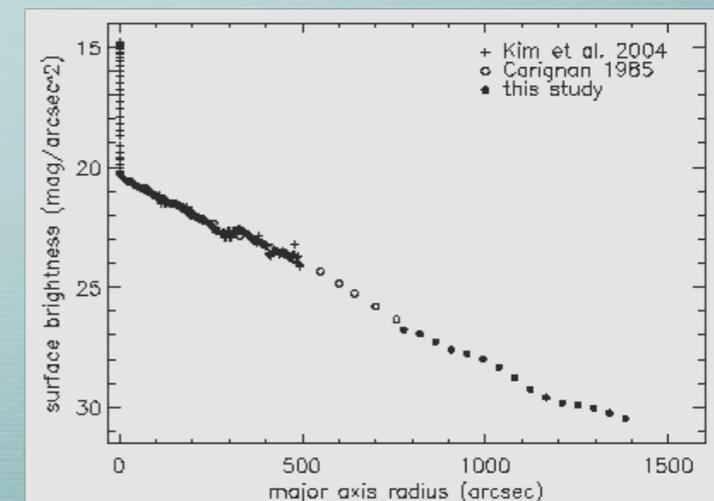
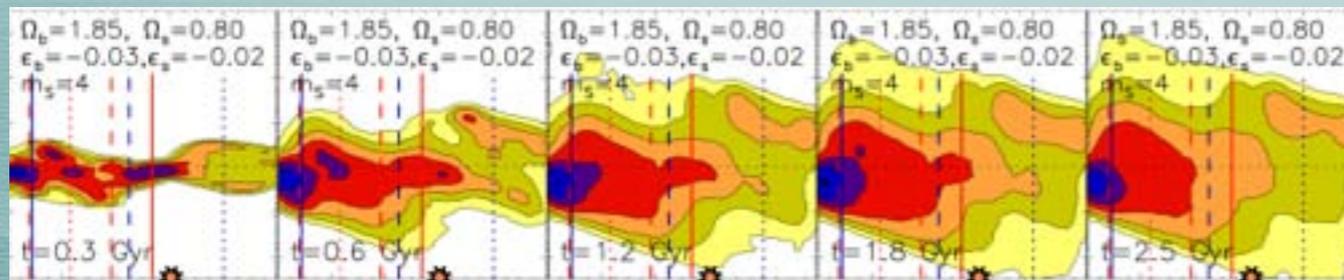
FIRE project simulation
 (GIZMO code,
[Hopkins 2014](#))
 ~10e4 M* resolution.
 50 pc spatial res.

Gómez et al. (2016)



Stellar radial migration

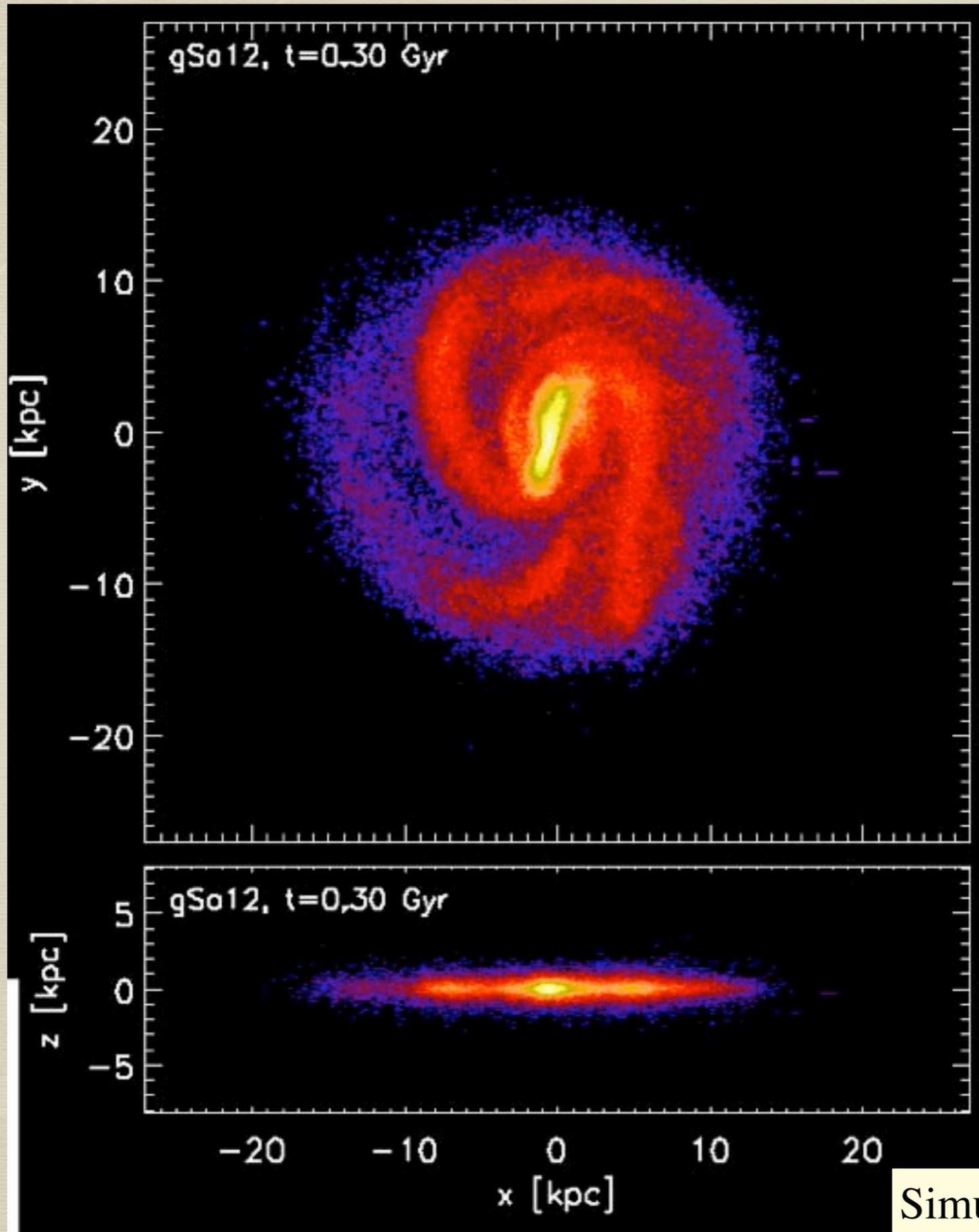
- Formally introduced by Sellwood and Binney (2002)
- A number of works on the topic since:
 - ◆ Roskar et al. (2008), Schoenrich and Binney (2009) - from transient spirals
 - ◆ Quillen et al. (2009), Bird et al. (2013) - from orbiting satellites
 - ◆ Minchev and Famaey (2010) - from multiple long-lived patterns
 - ◆ Grand et al. (2012) - corotating spirals



N-body Tree-SPH

Disk expands due to strong angular momentum transport outwards
(Minchev et al. 2012a).

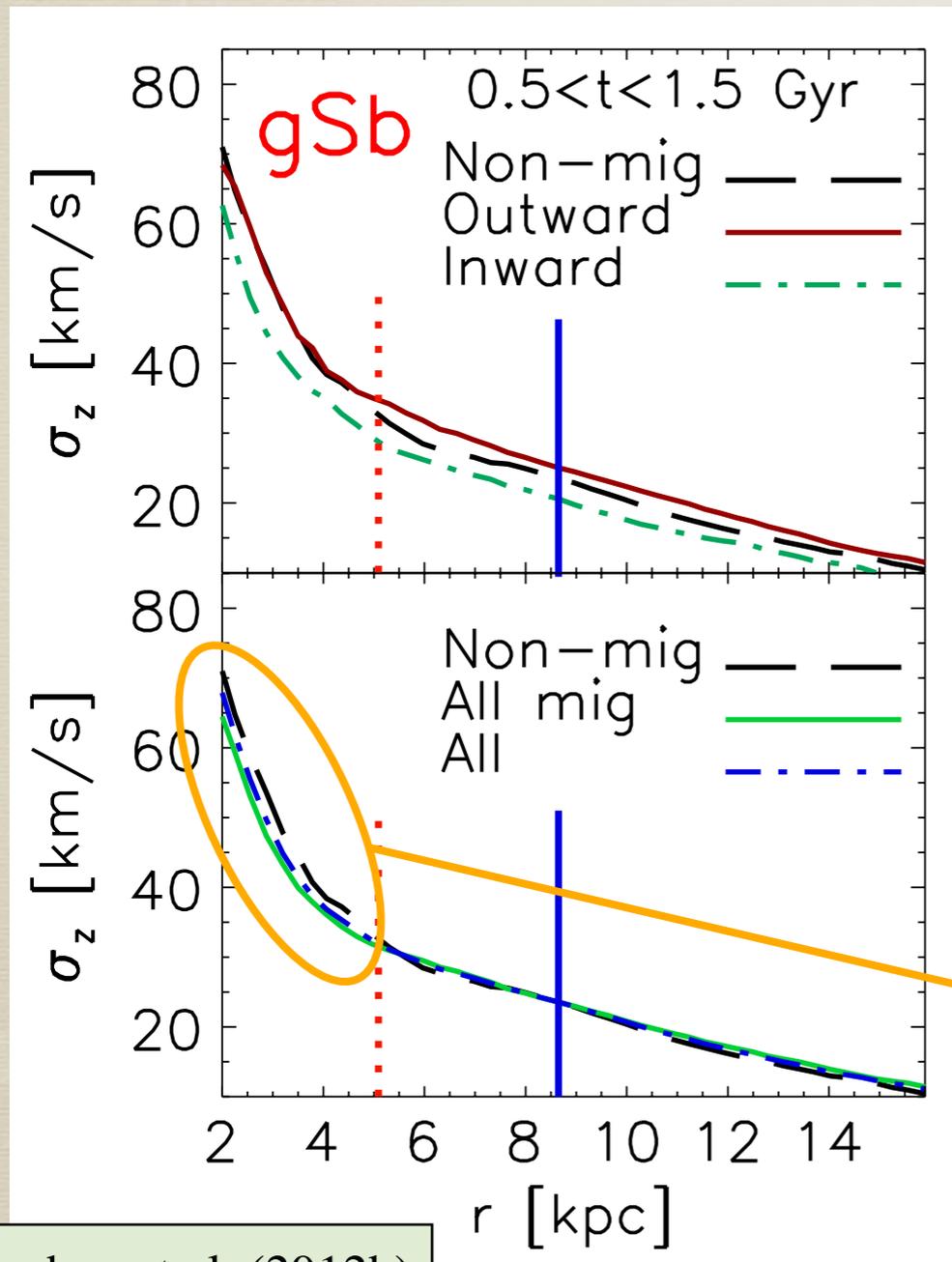
Disk thickens from bar/spirals. Not from radial migration (see Minchev et al. (2012b)!



Simulation by
P. Di Matteo

Migrators' contribution to the disk velocity dispersion **in the absence of mergers**

Vertical velocity dispersion



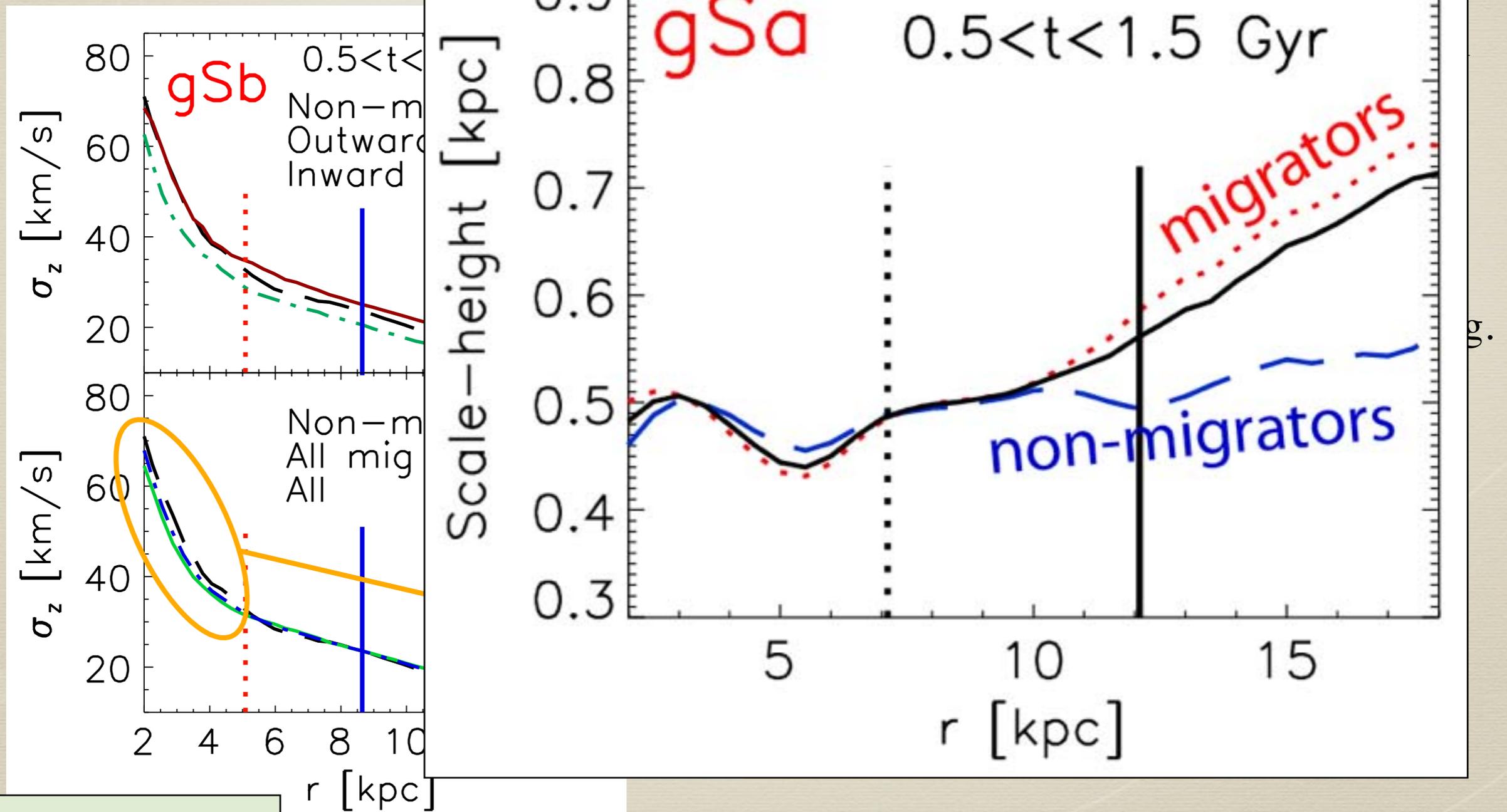
Minchev et al. (2012b)

- Some **increase** in velocity dispersion from outward migrators.
- Some **decrease** in velocity dispersion resulting from inward migrators.
- **Negligible overall effect** to disk thickening.
- In agreement with Vera-Ciro et al. (2013, 2014), Martig et al. (2014), Grand et al. (2016), Aumer et al. (2016)

Vertical disk cooling!

Migrators' contribution to the disk velocity dispersion **in the absence of mergers**

Vertical velocity dispersion



Conservation of vertical action

Vertical and radial actions conserved if:

- Vertical motion decouples from the radial motion
- Stars migrate (change guiding radii) slower than vertical and epicyclic oscillations.

Then

$$J_z = E_z / \nu = \text{Const.}$$

Vertical energy

Vertical epicyclic frequency

From Gauss' law and Poisson's equation

$$\nu \sim \sqrt{2\pi G \Sigma}$$

$$\Sigma \sim \exp(-r/r_d)$$



$$\nu(r) \sim \exp(-r/2r_d)$$

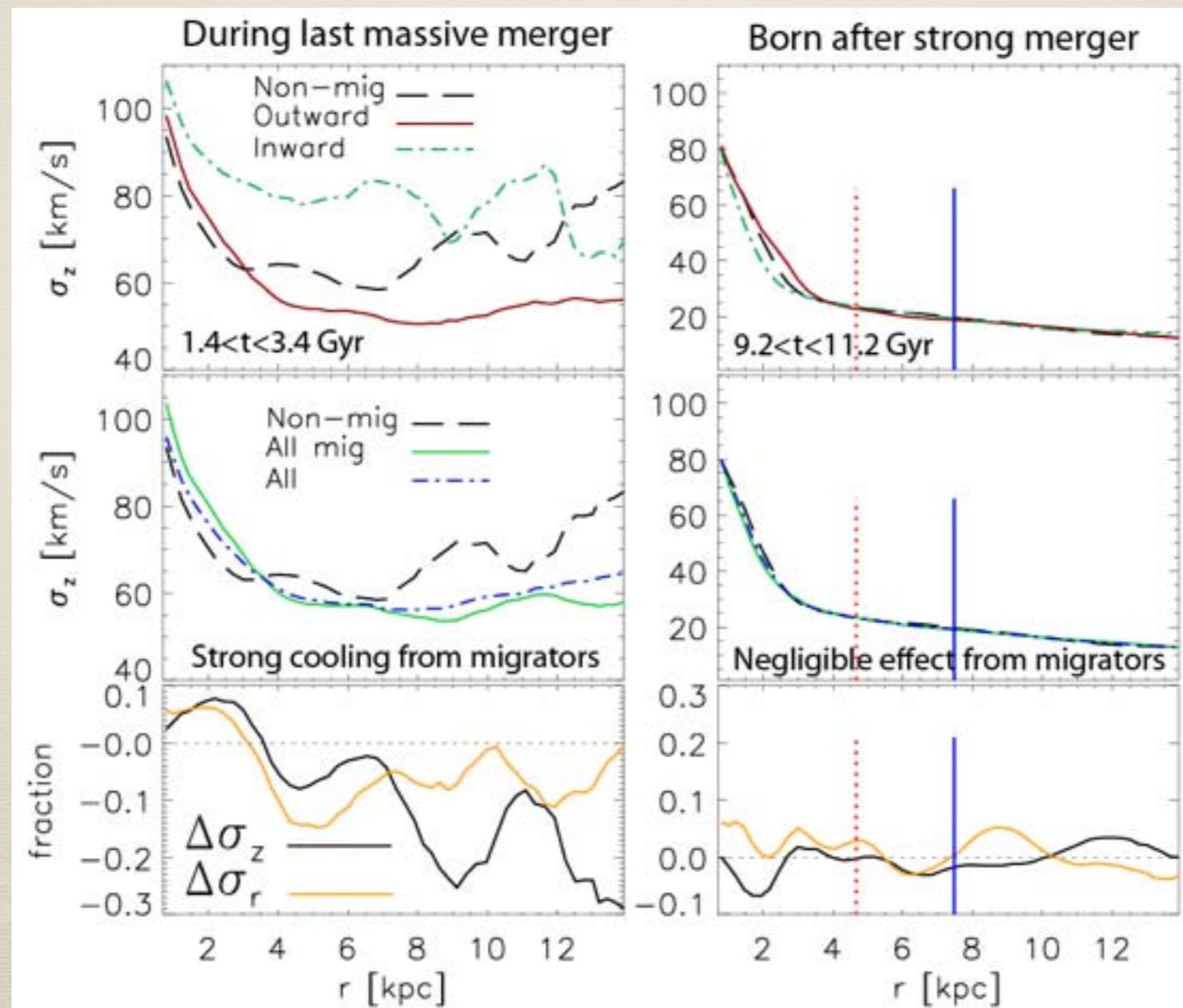
Therefore, to preserve vertical action

$$\langle E_z \rangle \sim \sigma_z^2 \sim \exp(-r/r_d)$$

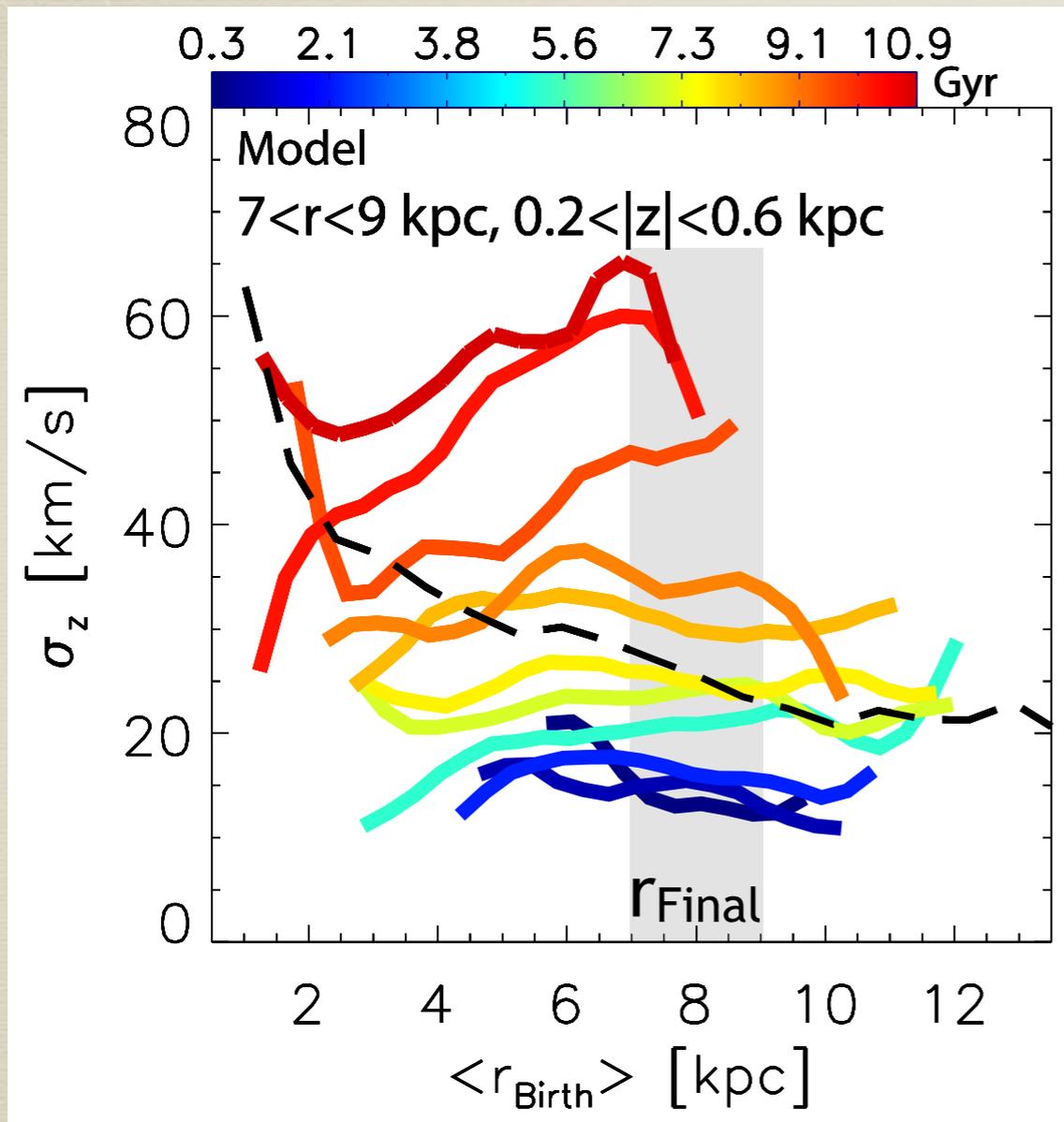
Migration cools the disk during mergers

Migration works against disk flaring

No effect on the vertical velocity dispersion.



Radial migration cools outer disk



Minchev + RAVE (2014)

Explains inversion of vel. dispersion - [Mg/Fe] relation in RAVE and SEGUE G-dwarf data.

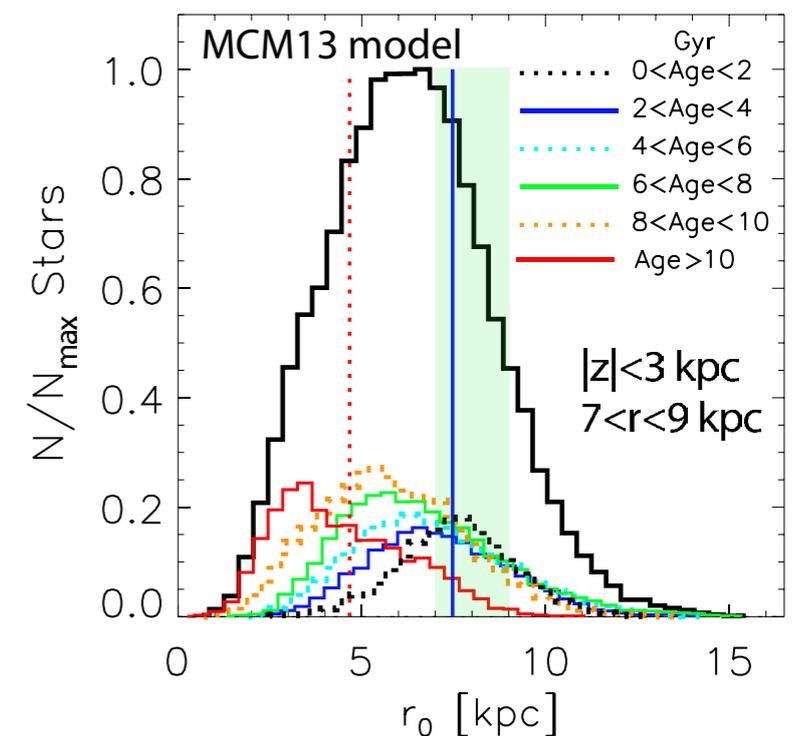
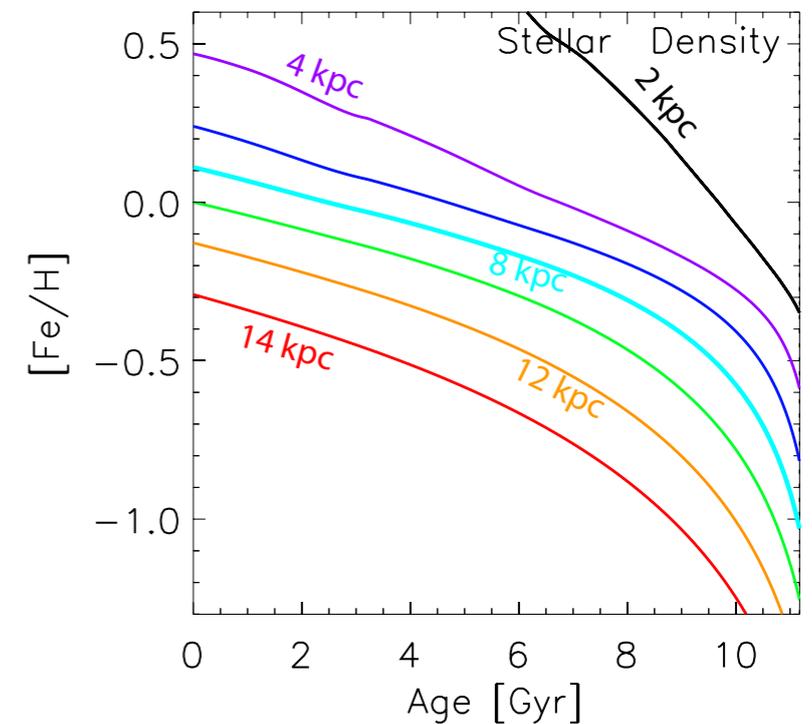
When a realistic disk growth in the cosmological context considered, migration cools outer disk.

Old stars coming from the inner disk are cooler than locally born stars by up to 30 km/s.

Slope becomes negative for the last several Gyr (no significant mergers).

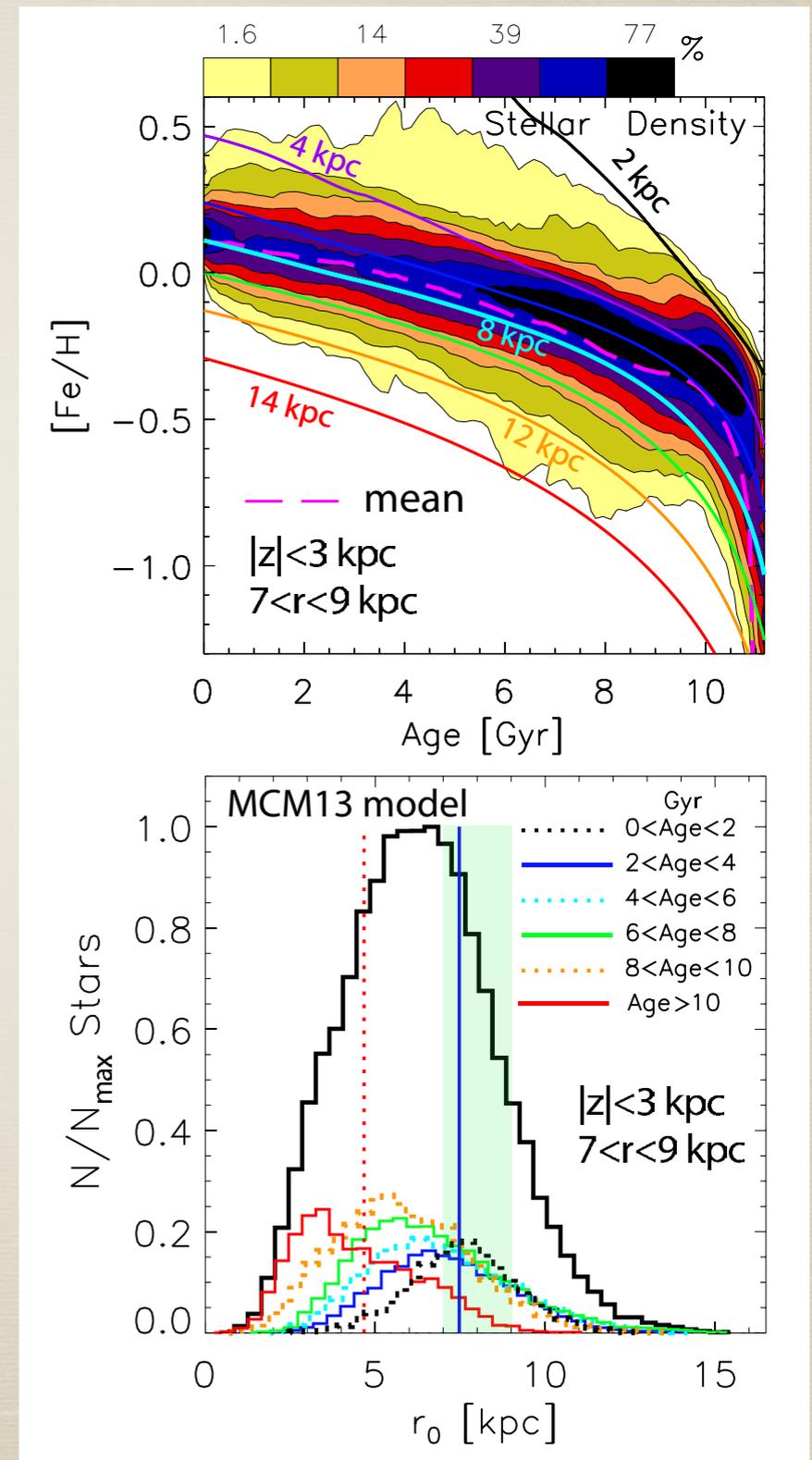
Classical chemical evolution modeling hampered by radial migration

- Stars move away from their birth places (e.g., [Sellwood and Binney 2002](#), [Roskar et al. 2008](#), [Schoenrich and Binney 2009](#)).



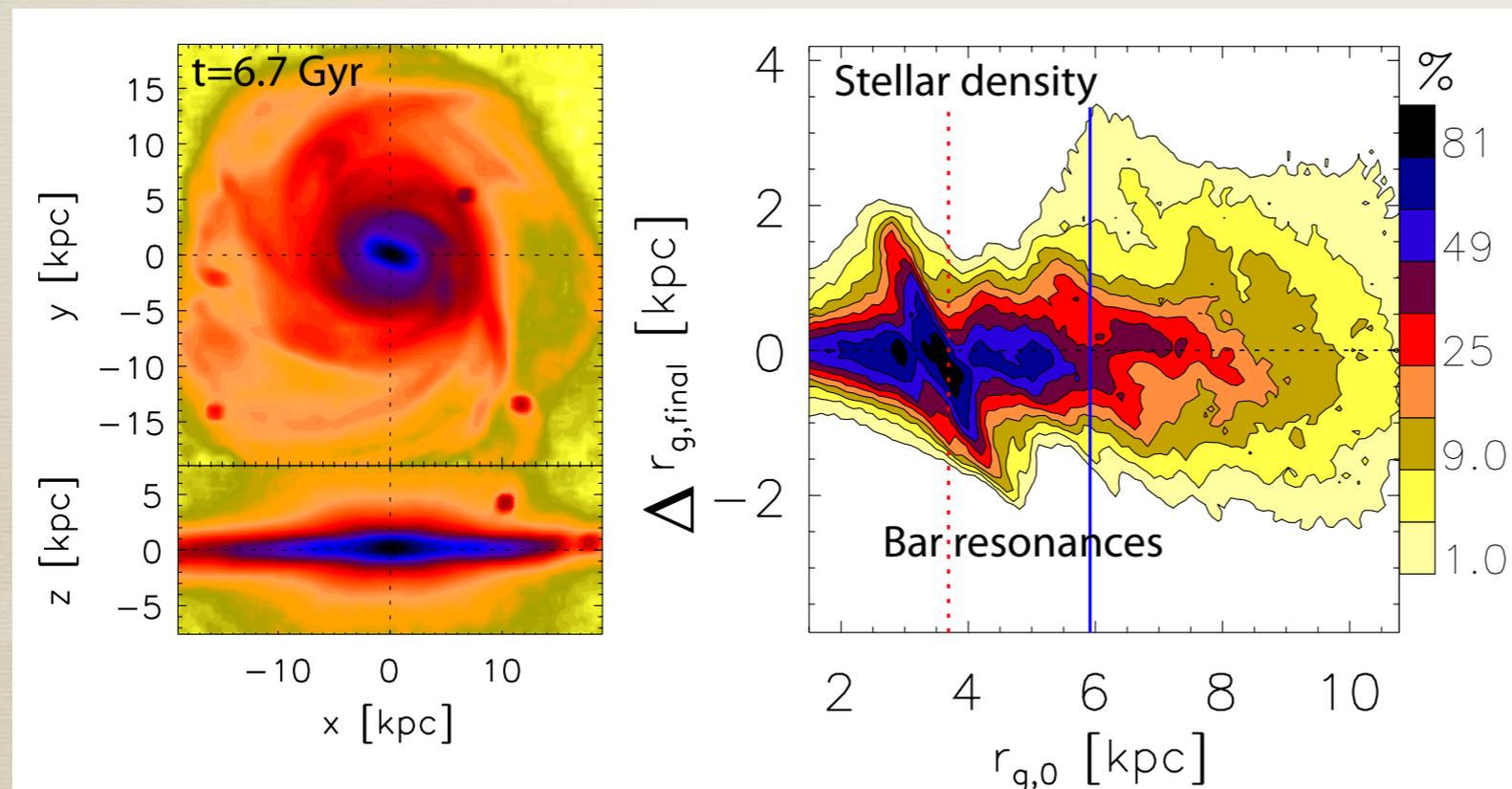
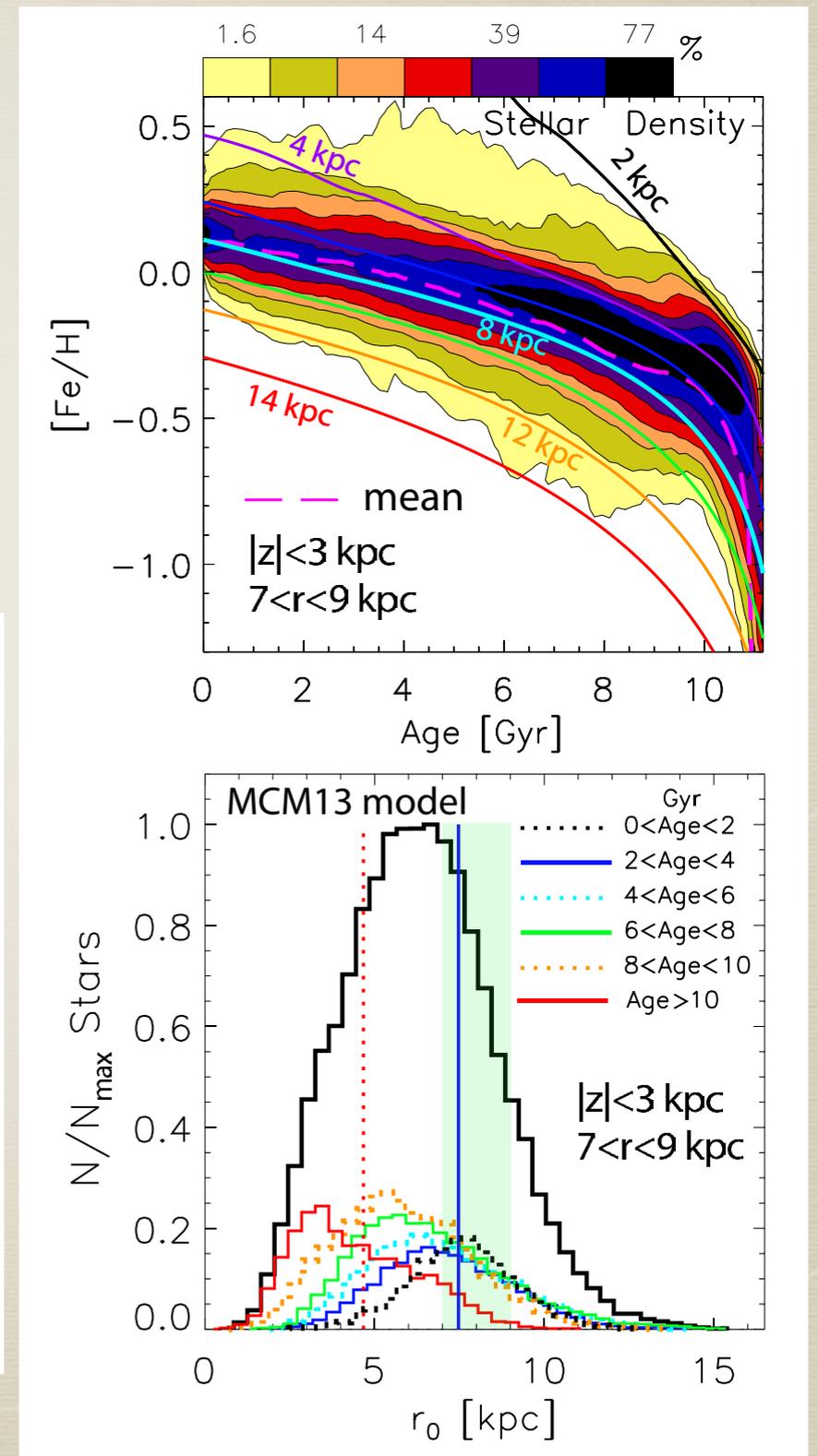
Classical chemical evolution modeling hampered by radial migration

- Stars move away from their birth places (e.g., Sellwood and Binney 2002, Roskar et al. 2008, Schoenrich and Binney 2009).



Classical chemical evolution modeling hampered by radial migration

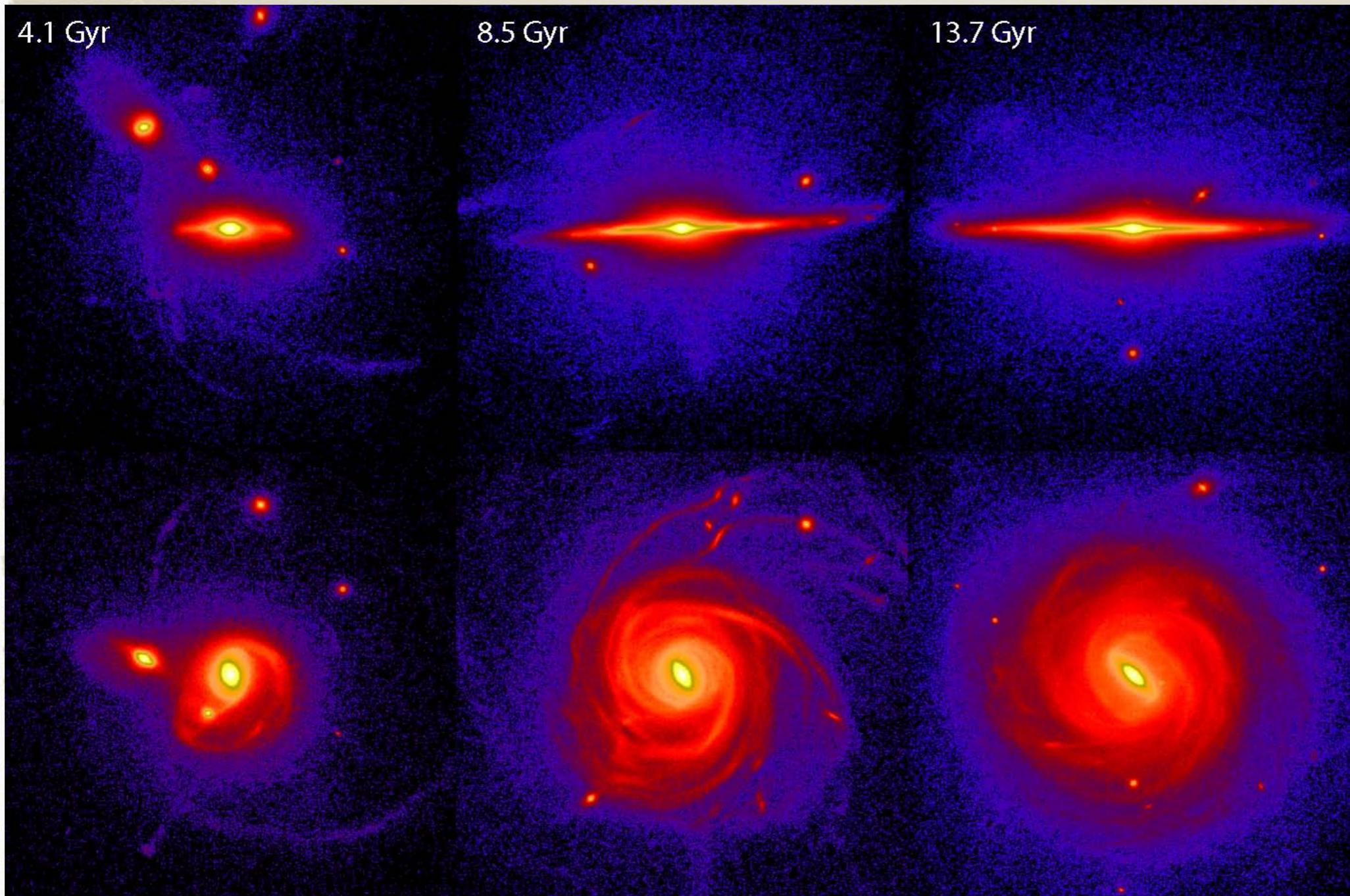
- Stars move away from their birth places (e.g., Sellwood and Binney 2002, Roskar et al. 2008, Schoenrich and Binney 2009).
- We need to recover the migration efficiency as a function of Galactic radius and time.



A hybrid chemo-dynamical evolution model for the Milky Way

- A high-resolution simulation of a disk assembly in the cosmological context:
 - Gas infall from filaments and gas-rich mergers
 - Merger activity decreasing toward redshift zero
- Disk properties at redshift zero consistent with the dynamics and morphology of the Milky Way:
 - The presence of a Milky Way-size bar
 - A small bulge
 - Bar's Outer Lindblad Resonance at ~ 2.5 disk scale-lengths
- A detailed chemical evolution model:
 - Matching a number of observational constraints in the Milky Way, similar to Matteucci and Francois (1989), Prantzos & Aubert (1995), Chiappini et al. (1997).

Galactic disk assembly in the cosmological context



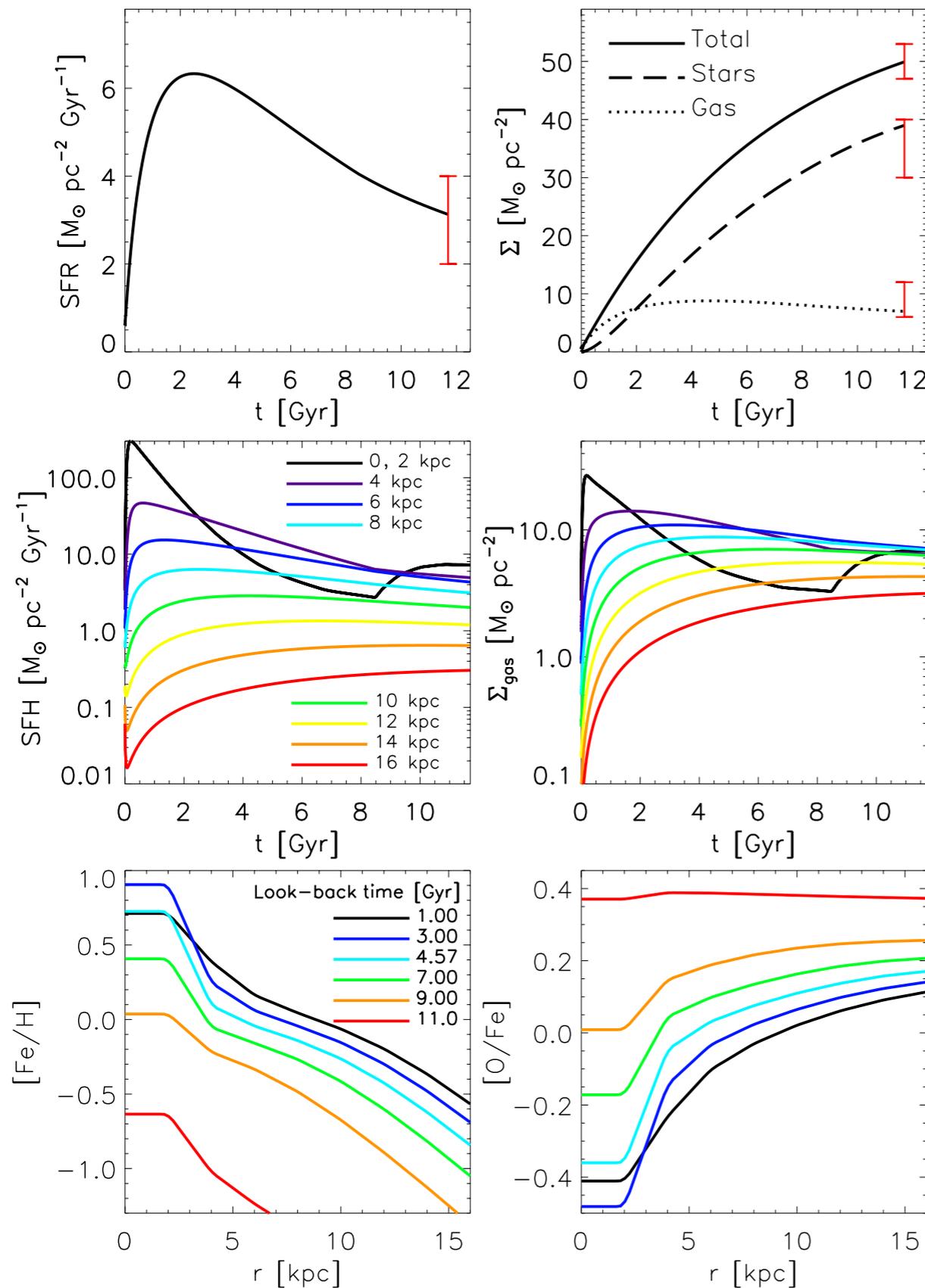
Simulation in
cosmological context
Martig et al. (2009, 2012)

Used for our chemo-
dynamical model
(Minchev, Chiappini &
Martig 2013, 2014)

**Stars born hot at
high redshift:**

Similar to
Brook et al. (2012),
Stinson et al. (2013),
Bird et al. (2013)

A classical chemical model coupled with the simulation

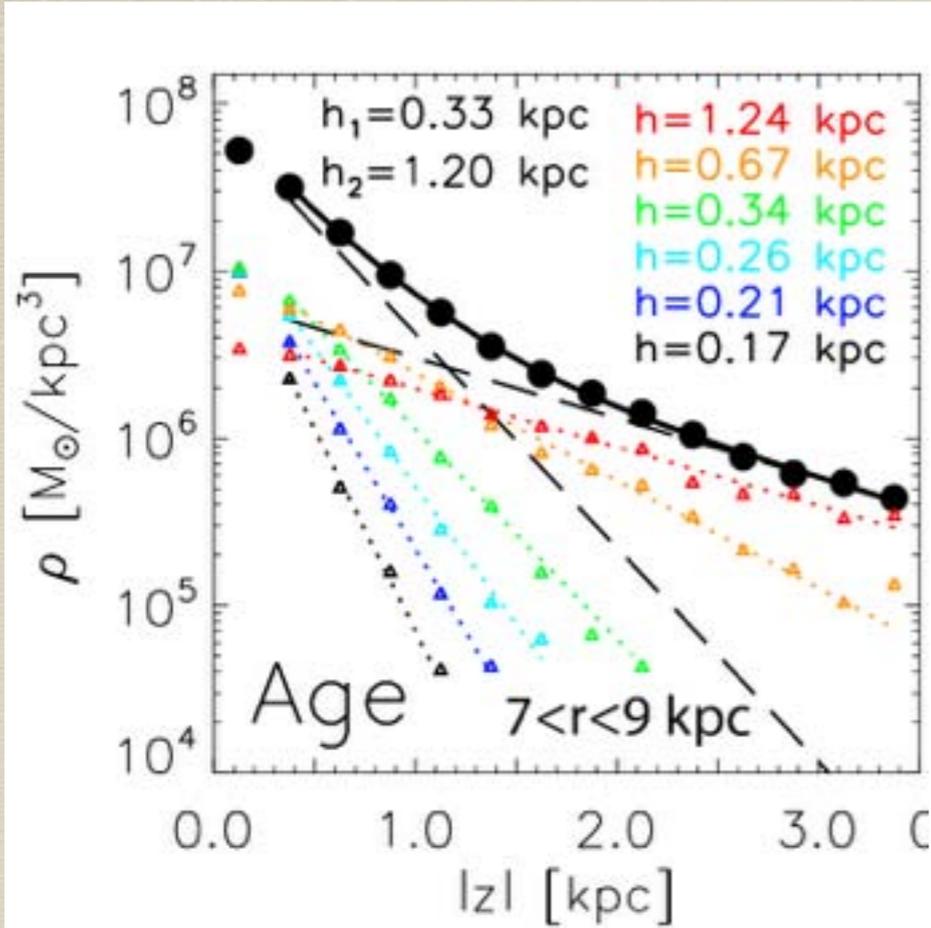


Similar to Chiappini (2009)

Constrained by:

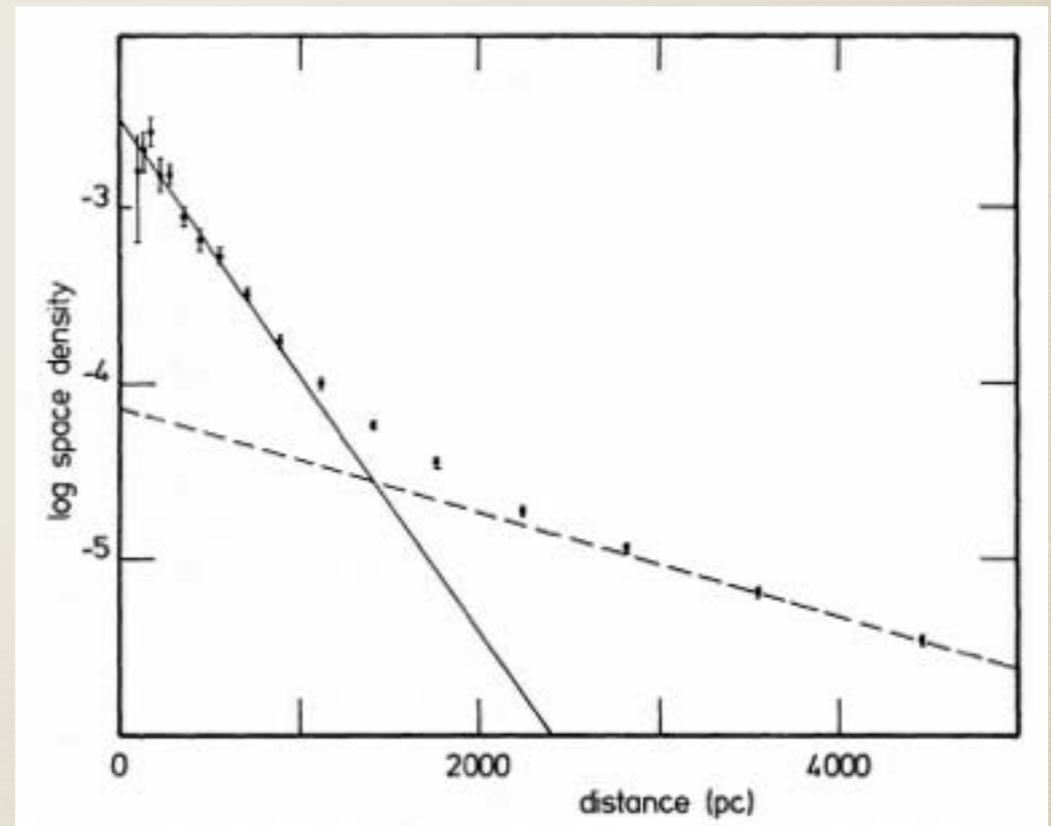
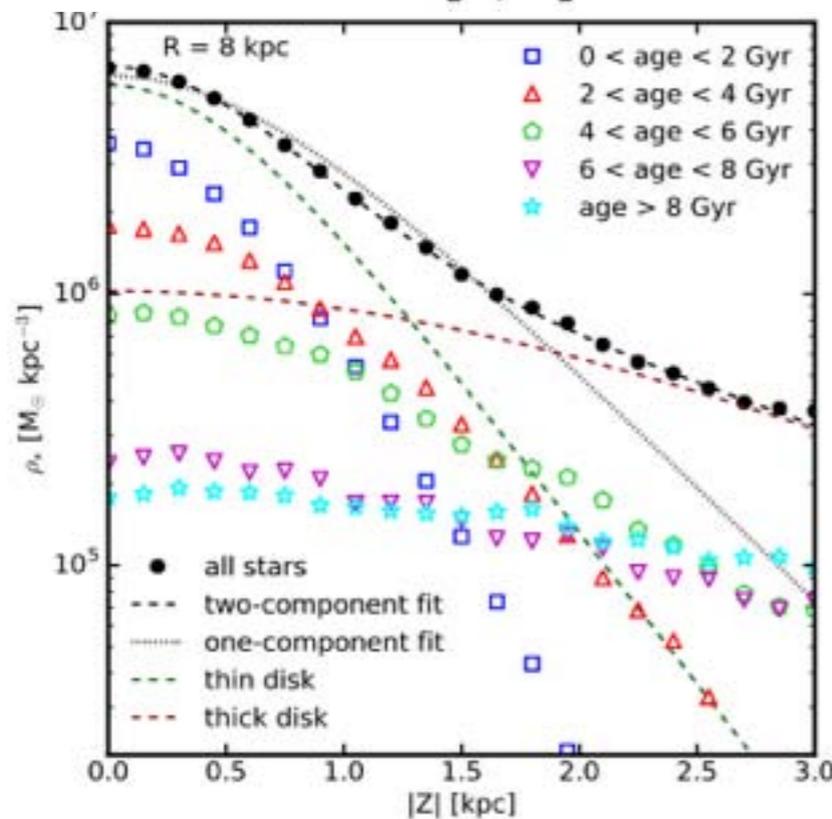
- The solar and present day abundances of more than 30 elements
- The present SFR
- The current stellar, gas and total mass densities at the solar vicinity
- The present day supernovae rates of type II and Ia
- The metallicity distribution of G-dwarf stars

Thin-thick disk decomposition near Sun



Minchev, Chiappini and Martig (2013)

Sticky particles simulation by Martig et al.



Gilmore and Ried (1983)

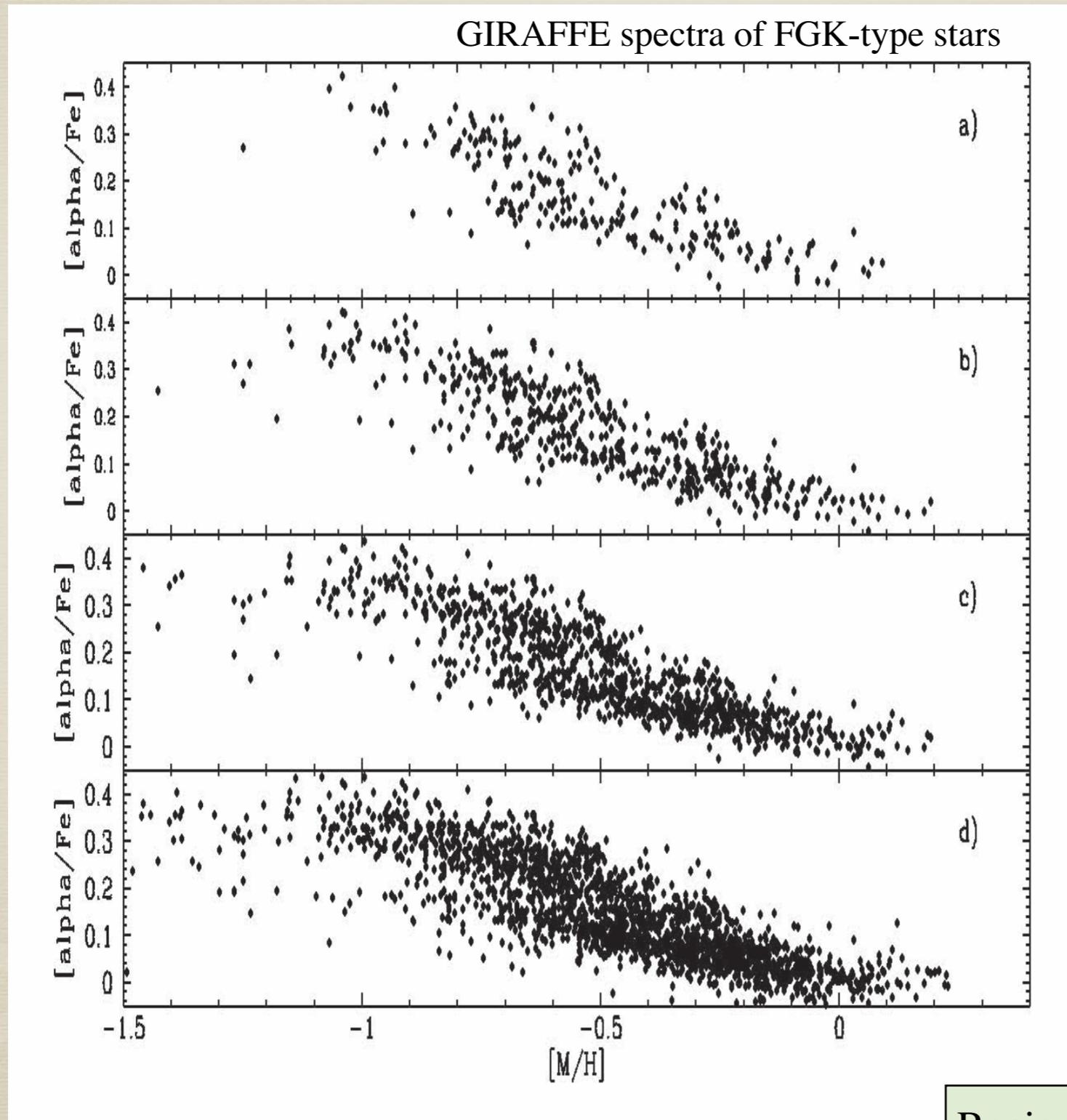
Ma et al. (2016)

Simulation from the FIRE project (GIZMO code)

The $[\text{Fe}/\text{H}]-[\alpha/\text{Fe}]$ relation

Gaia-ESO data

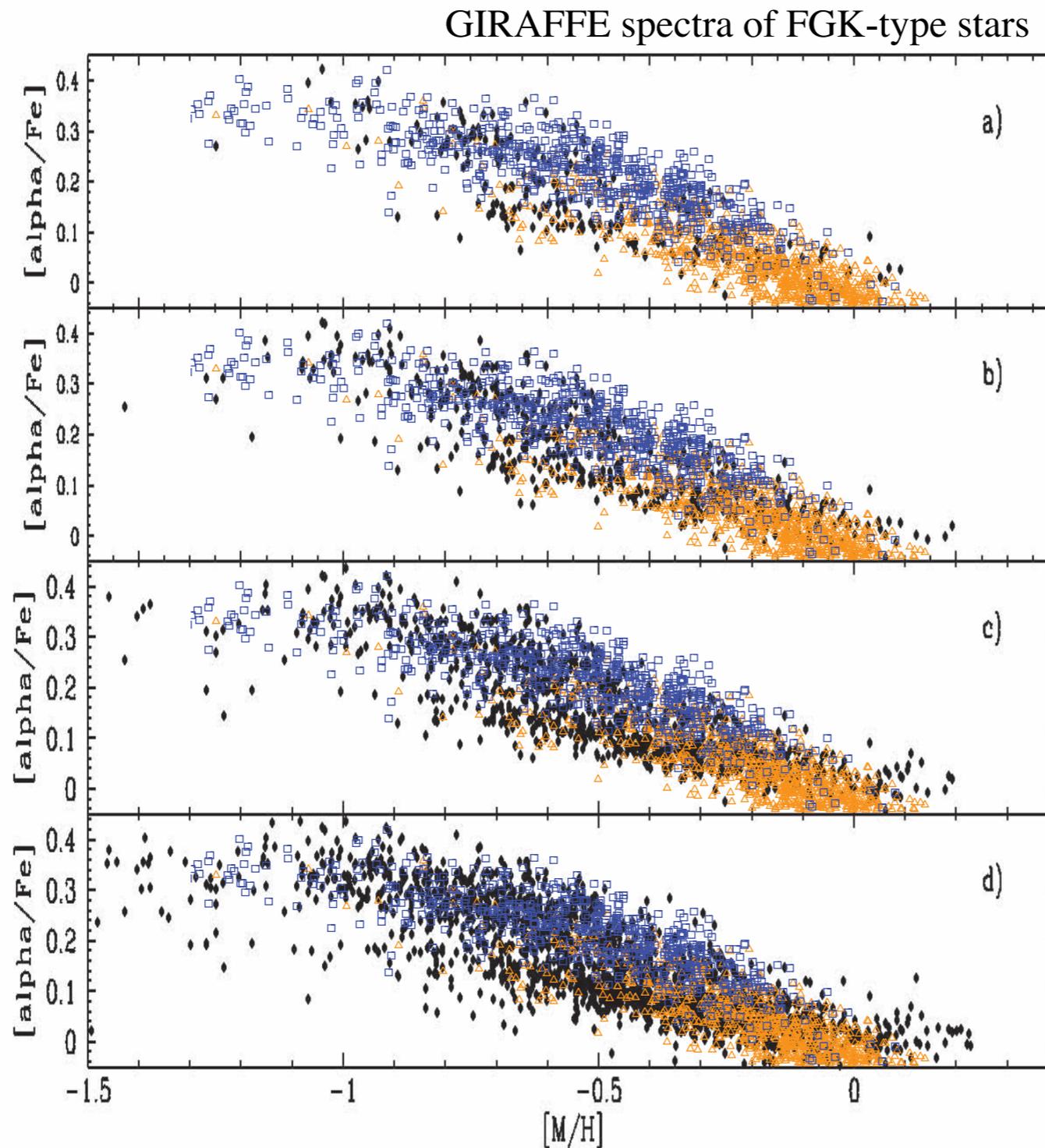
←----- Uncertainties



Recio-Blanco et al. (2014)

The $[\text{Fe}/\text{H}]-[\alpha/\text{Fe}]$ relation

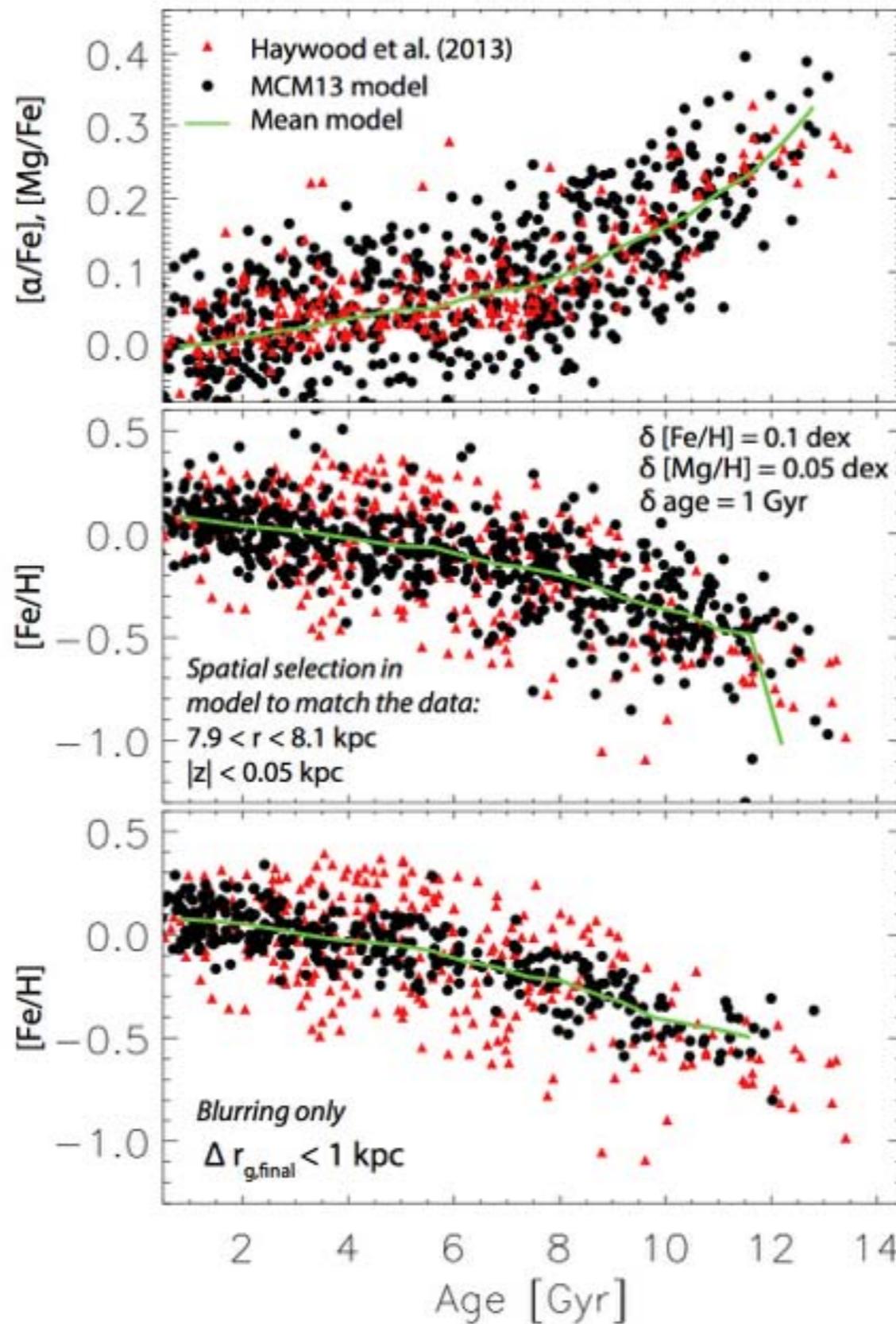
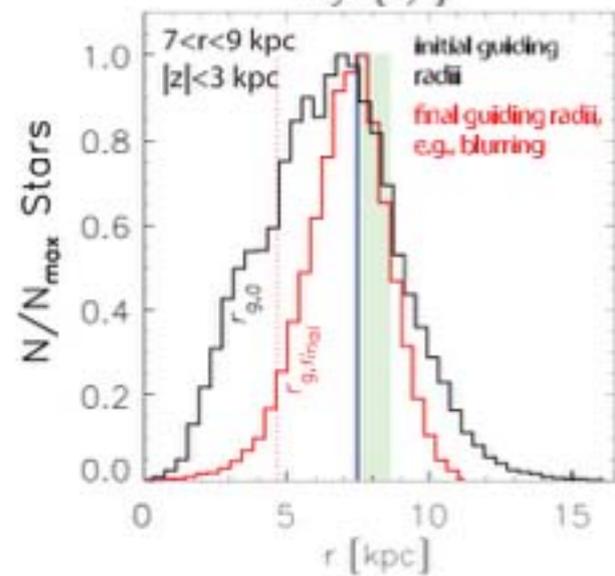
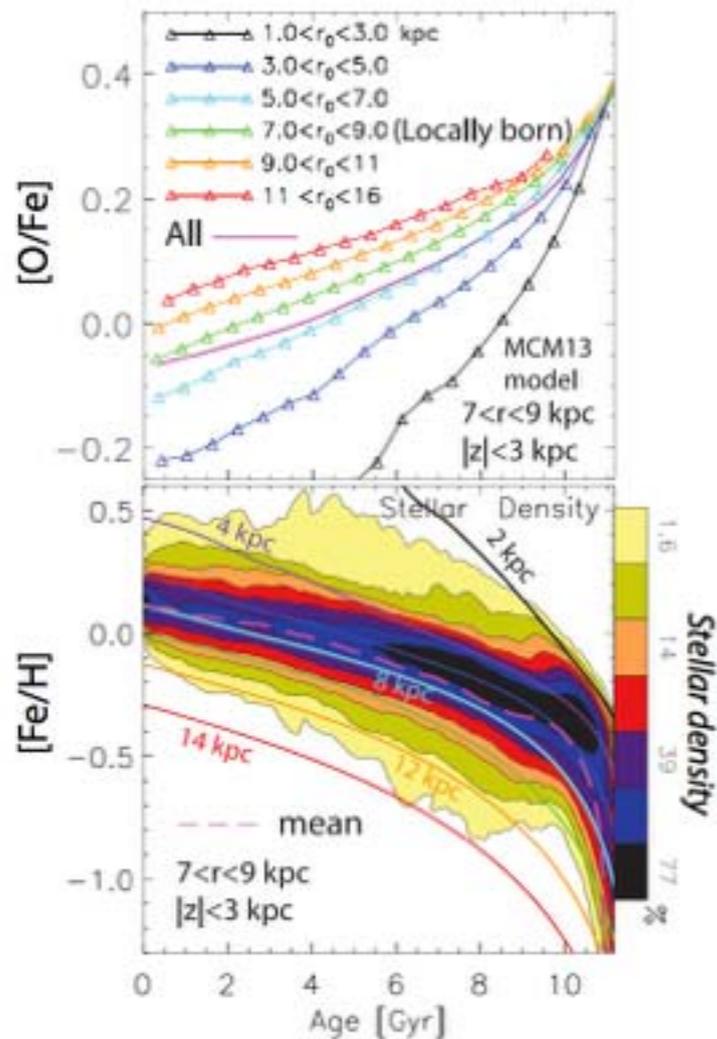
Gaia-ESO data



←----- Uncertainties

Recio-Blanco et al. (2014)

The age- $[\alpha/\text{Fe}]$ and age- $[\text{Fe}/\text{H}]$ relations

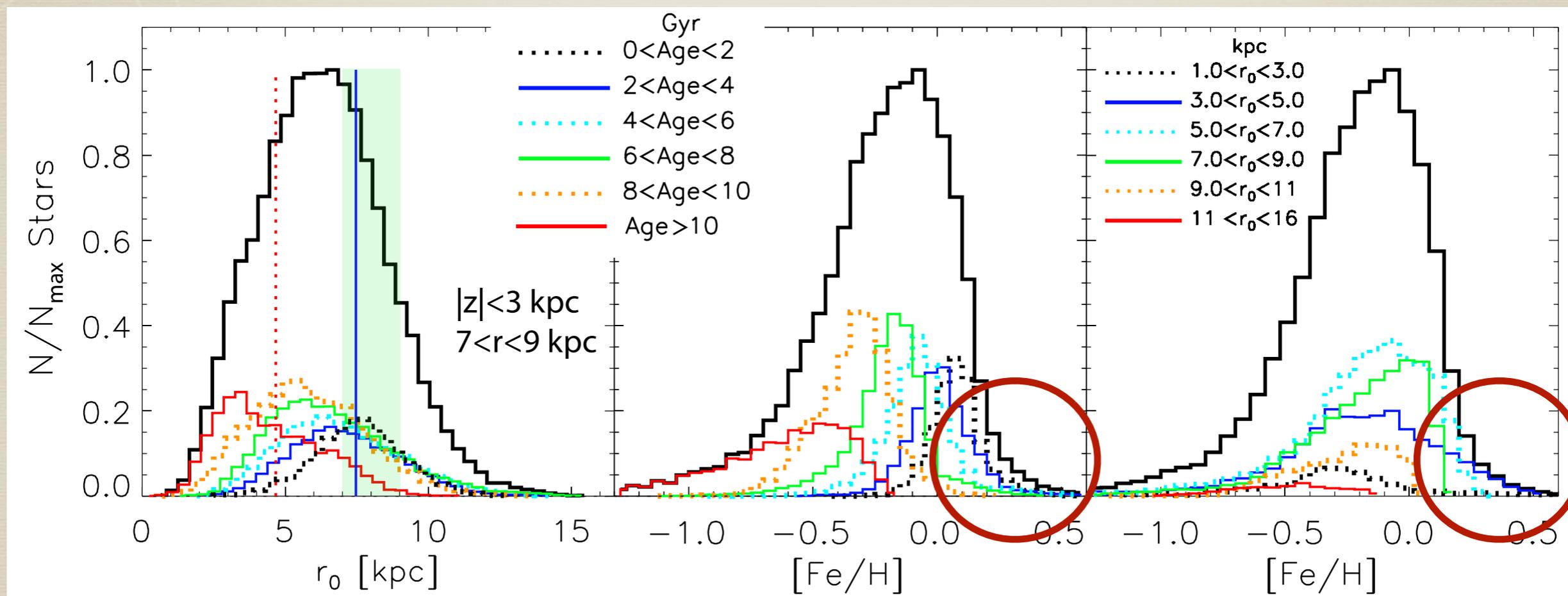


Comparison to the Adibekyan (HARPS) + Haywood (ages) sample

Artificial errors added similar to the observations. Yet, scatter in model AMR less than in data

Hot orbits only (blurring) insufficient to explain AMR

Origin and metallicity distribution of local stars

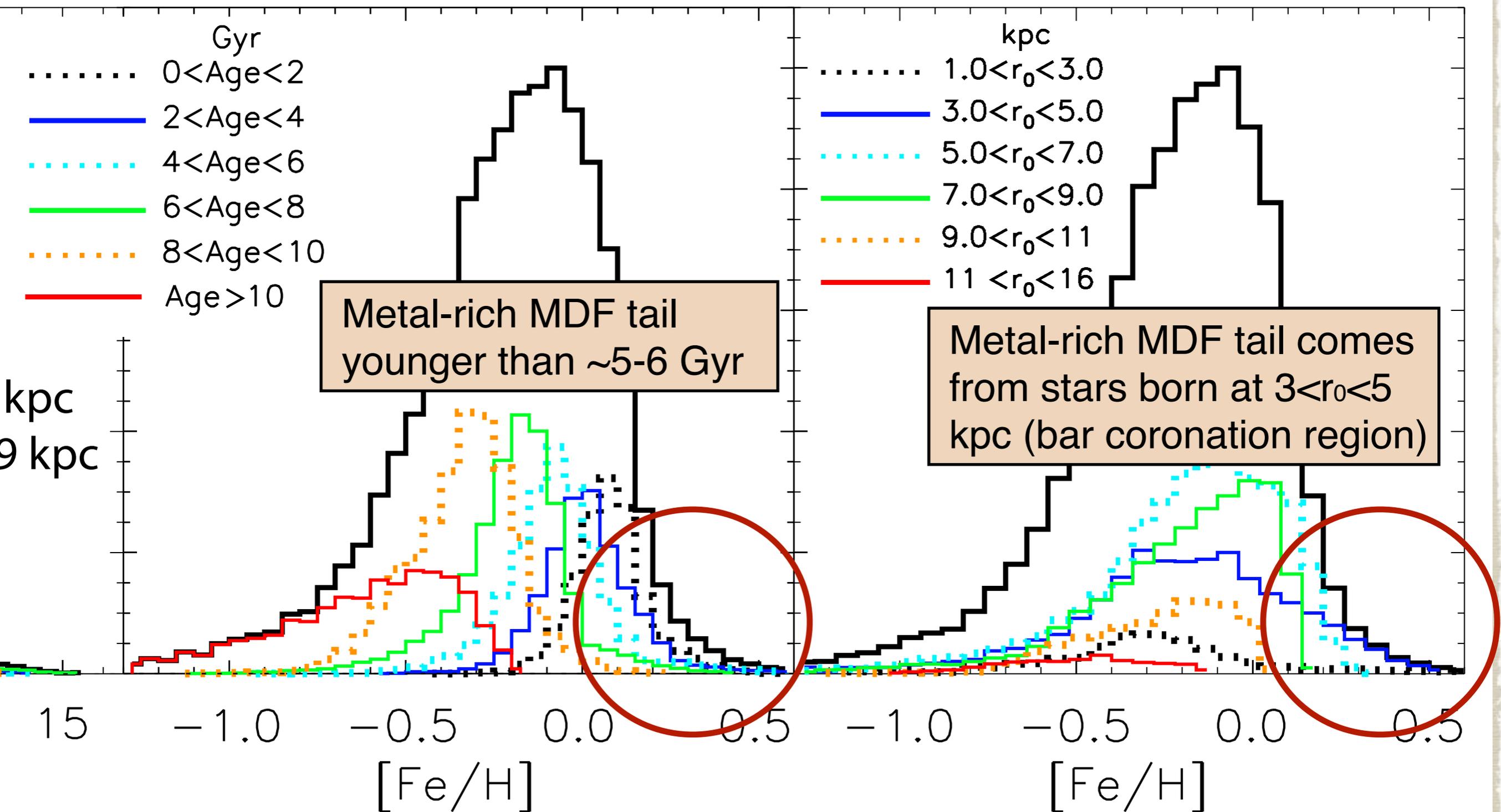


Minchev, Chiappini & Martig (2013)

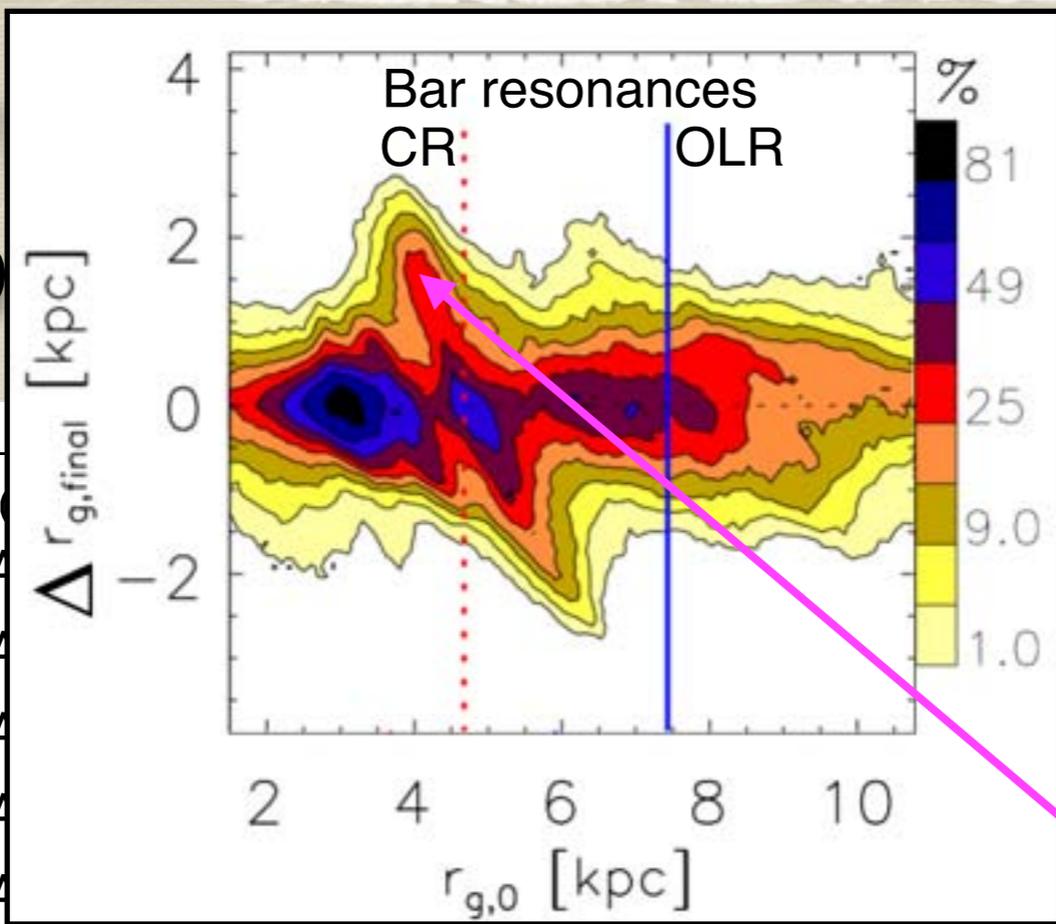
Older populations arrive from progressively smaller galactic radii due to their longer exposure to migration.

Kordopatis will tell us more about the MDF

Origin and metallicity distribution of local stars



Age distribution

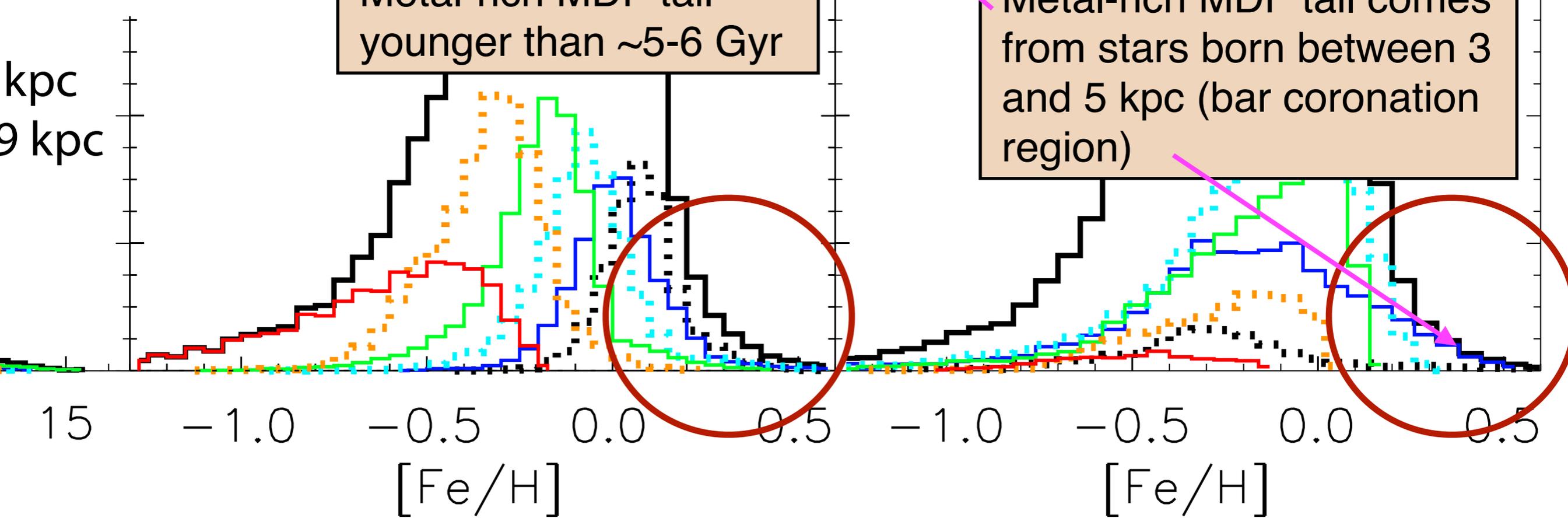


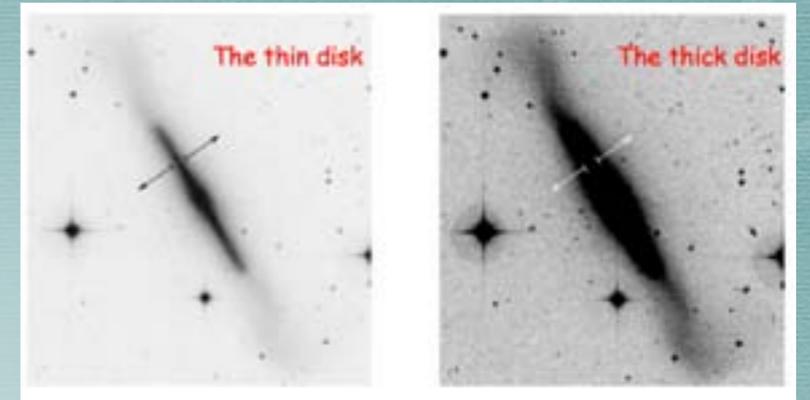
- $0 < A < 2$
- $2 < A < 4$
- $4 < A < 6$
- $6 < A < 8$
- $8 < A < 10$
- $Age > 10$

- $1.0 < r_0 < 3.0$
- $3.0 < r_0 < 5.0$
- $5.0 < r_0 < 7.0$
- $7.0 < r_0 < 9.0$
- $9.0 < r_0 < 11$
- $11 < r_0 < 16$

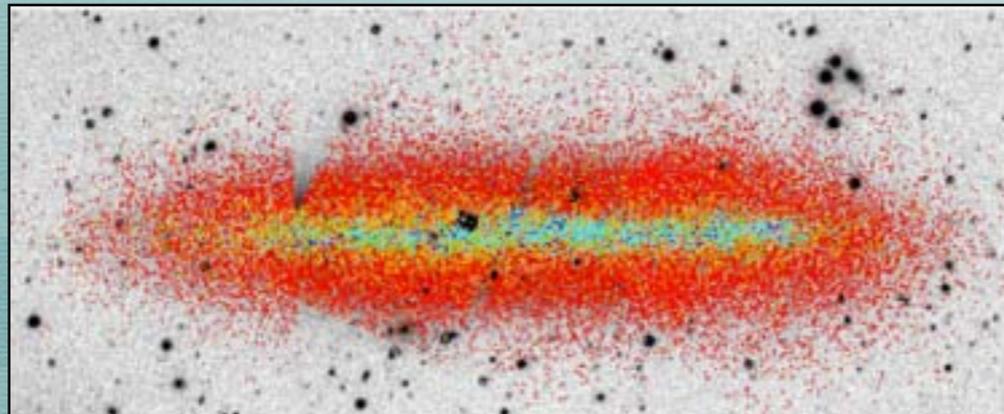
Metal-rich MDF tail younger than $\sim 5-6$ Gyr

Metal-rich MDF tail comes from stars born between 3 and 5 kpc (bar coronation region)



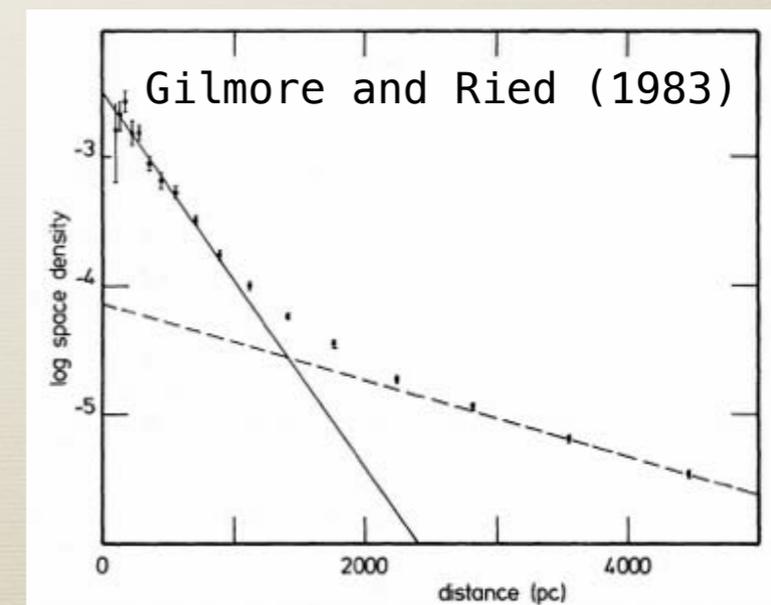
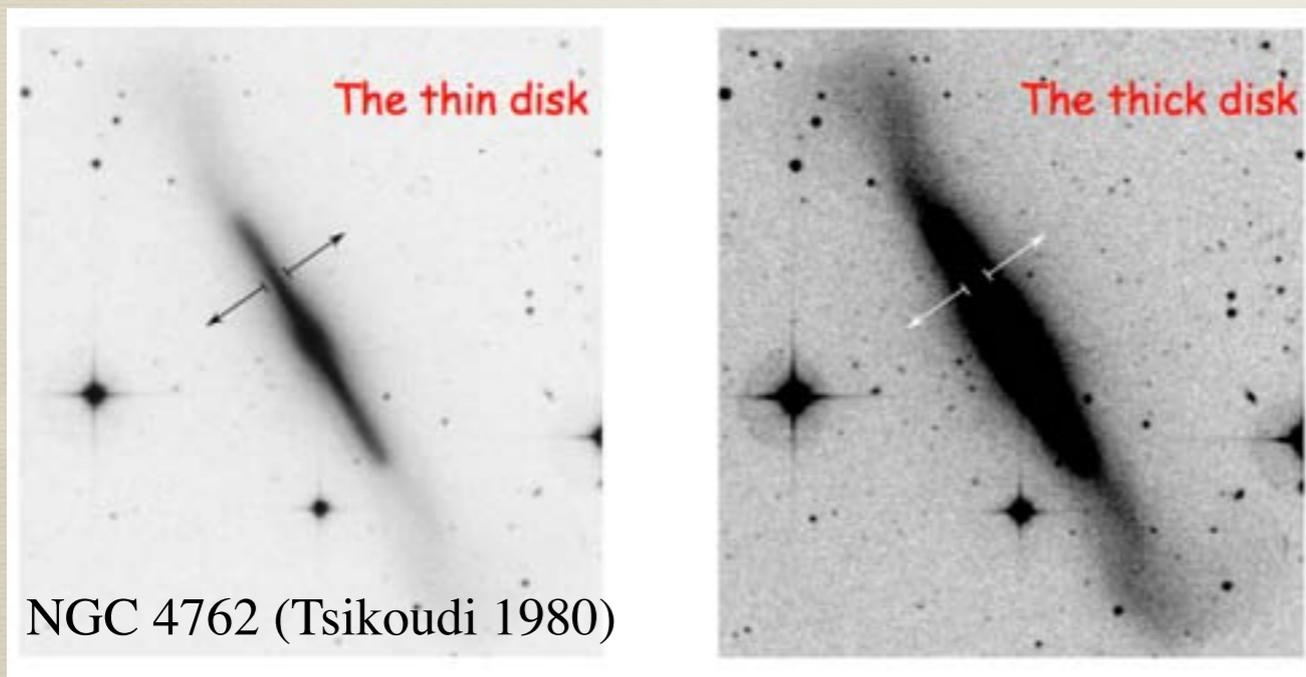


On the formation of galactic thick disks



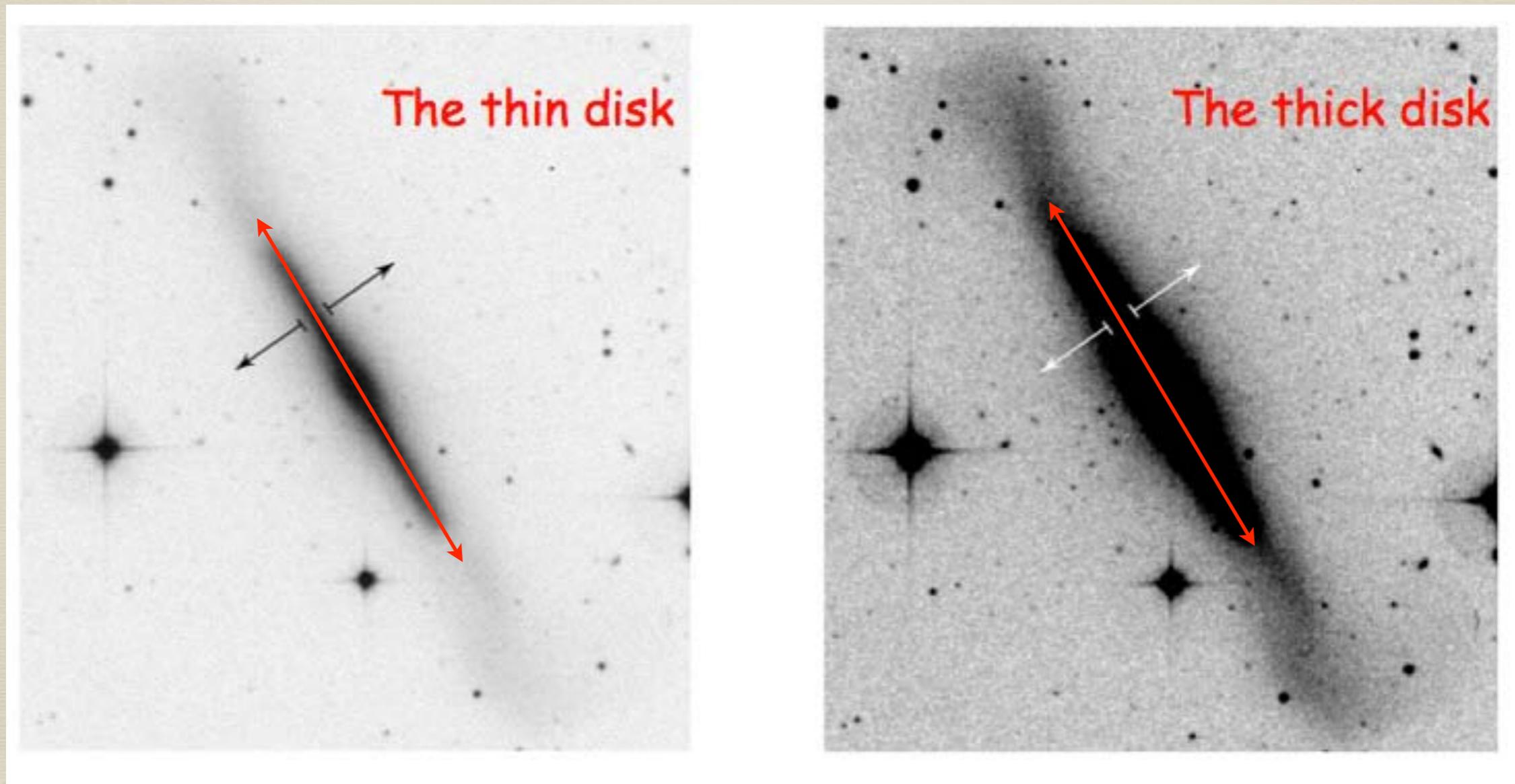
Thick disks formation mechanisms

- Turbulent gas-rich clouds at high redshift (e.g., Bournaud et al. 2009) - seen at high redshift
- Gas-rich mergers (Brook et al. 2004, 2005) - seen in most/all cosmological simulations
- Accretion of satellites (Meza et al. 2005, Abadi et al. 2003) - possibly ruled out at this point for the Milky Way
- Perturbations by merging satellites on an initially thin disk (Quinn et al. 2004, Villalobos and Helmi 2008, Di Matteo et al. 2011)
- Some combination of the above (see next)



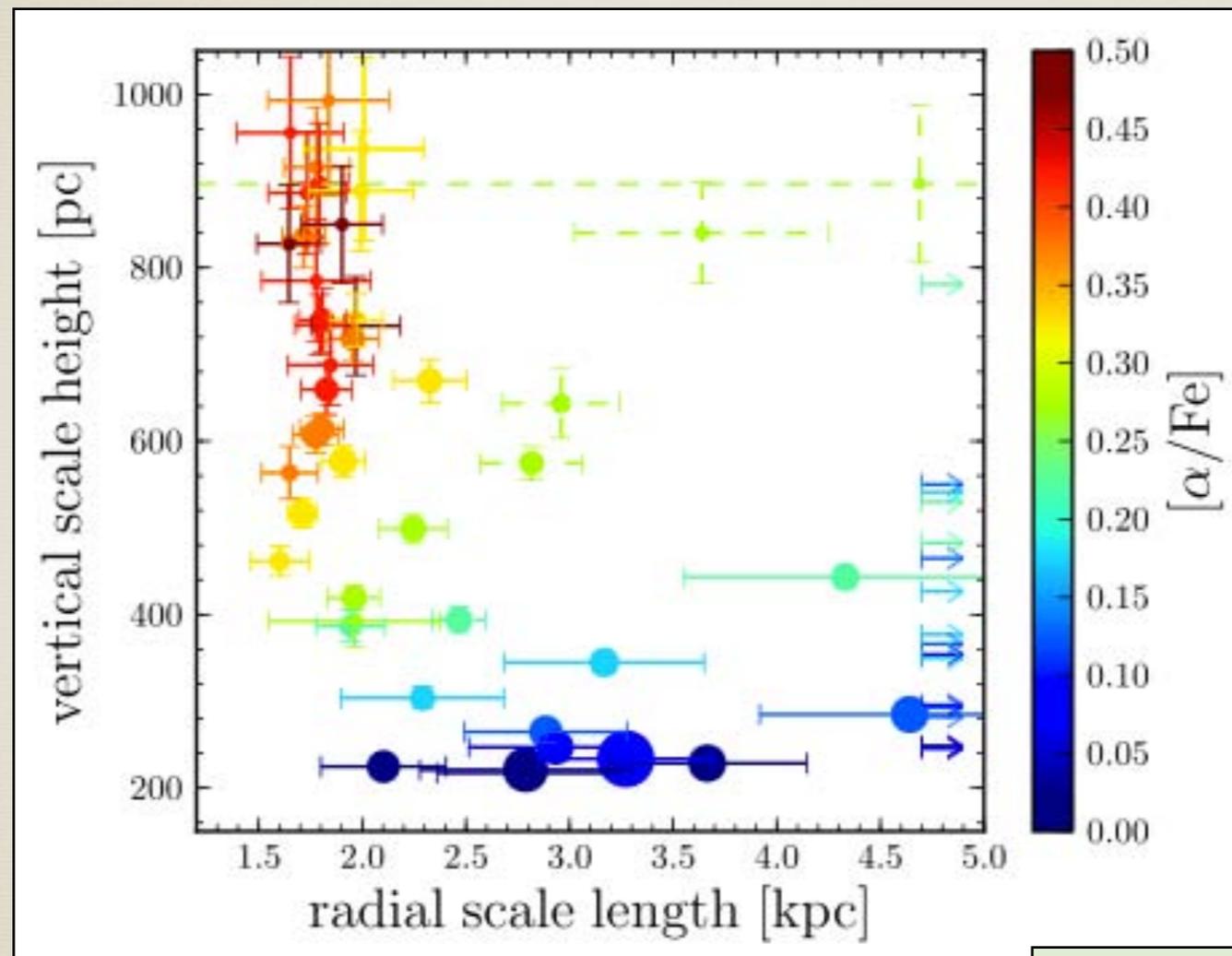
Thick disks are **extended** (when morphologically defined)

NGC 4762 (Tsikoudi 1980)



Also argued by Yoachim and Dalcanton (2006); Pohlen et al. (2007);
Comerón et al. (2012)

Chemically/Age defined Milky Way thick disk centrally concentrated (e.g., not extended)

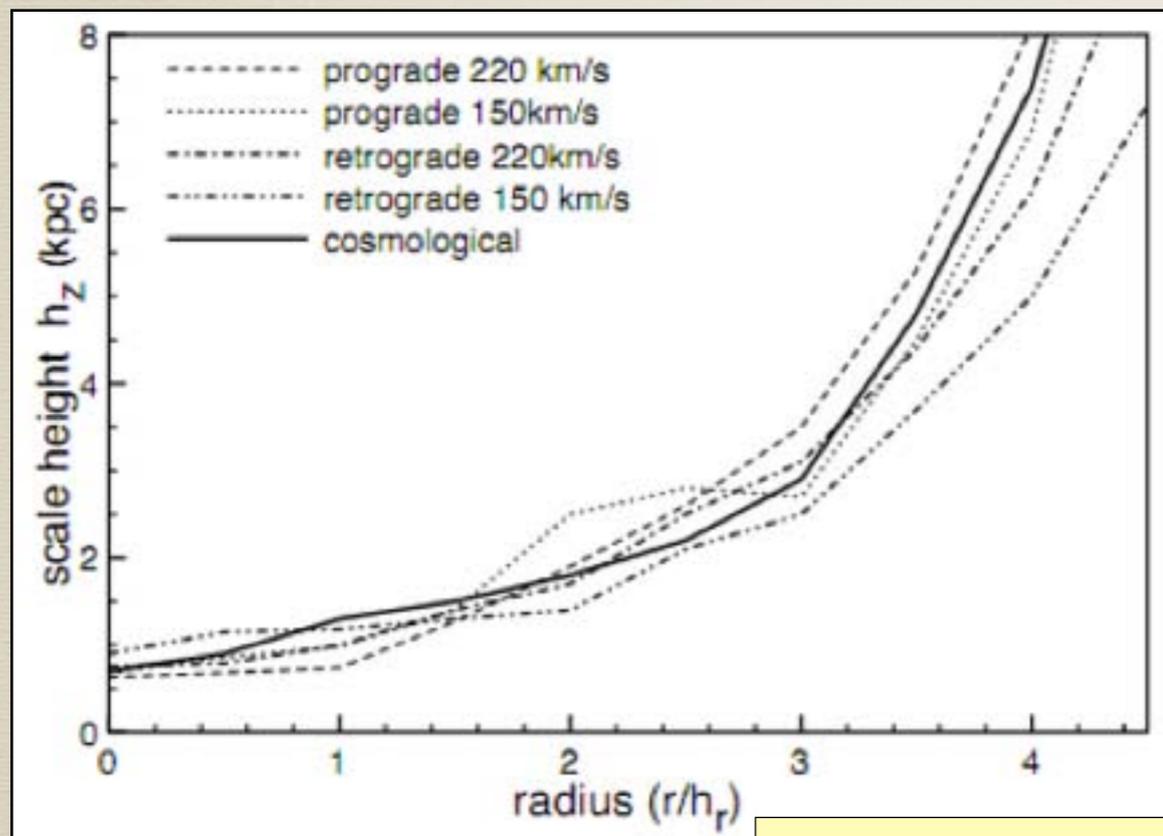


Bovy et al. (2012)

Found also in Bensby et al. (2011) data and SEGUE data (Cheng et al. 2012)

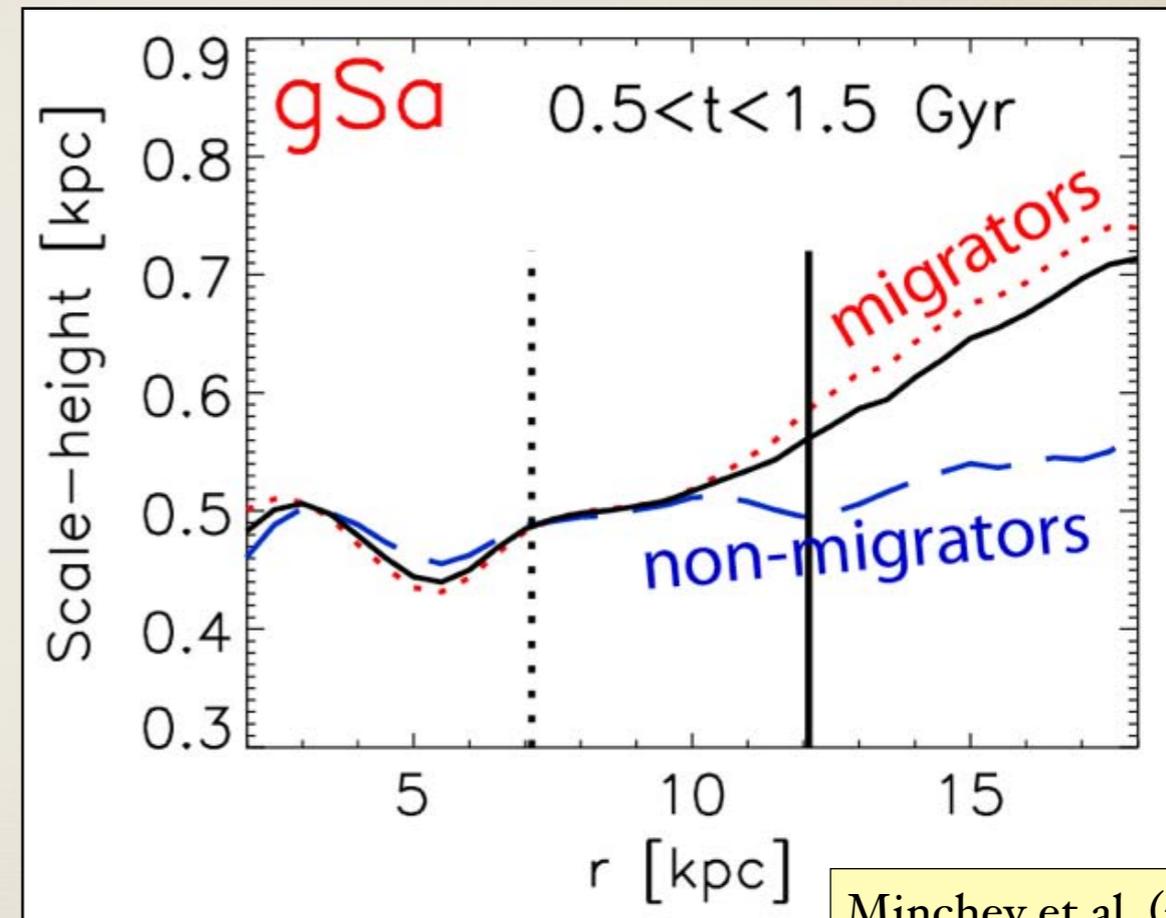
Simulated disks **always flare** (for a single stellar population)

Mergers flare disks



Bournaud et al. 2009

Migration flares disks



Minchev et al. (2012)

But observed edge-on disks do not flare
(de Grijs 1998; Comerón et al. 2011)

Disk flaring in inside-out galaxy formation

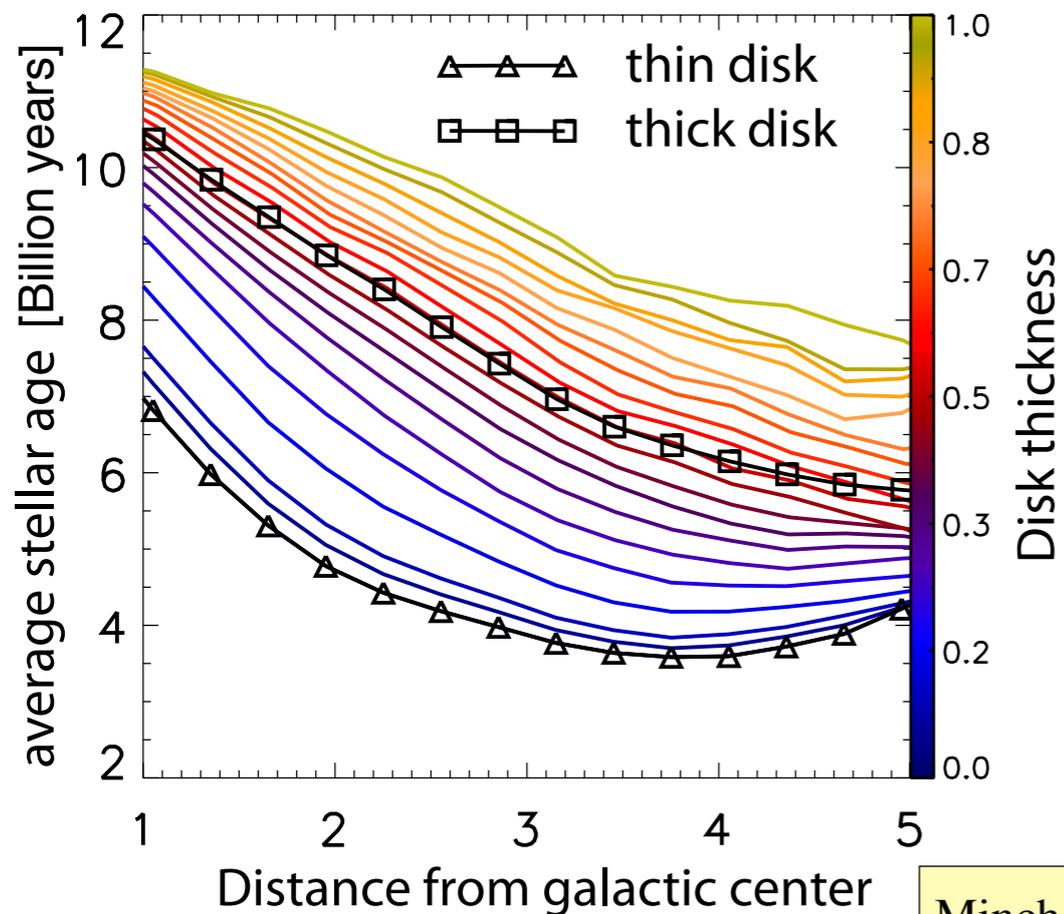
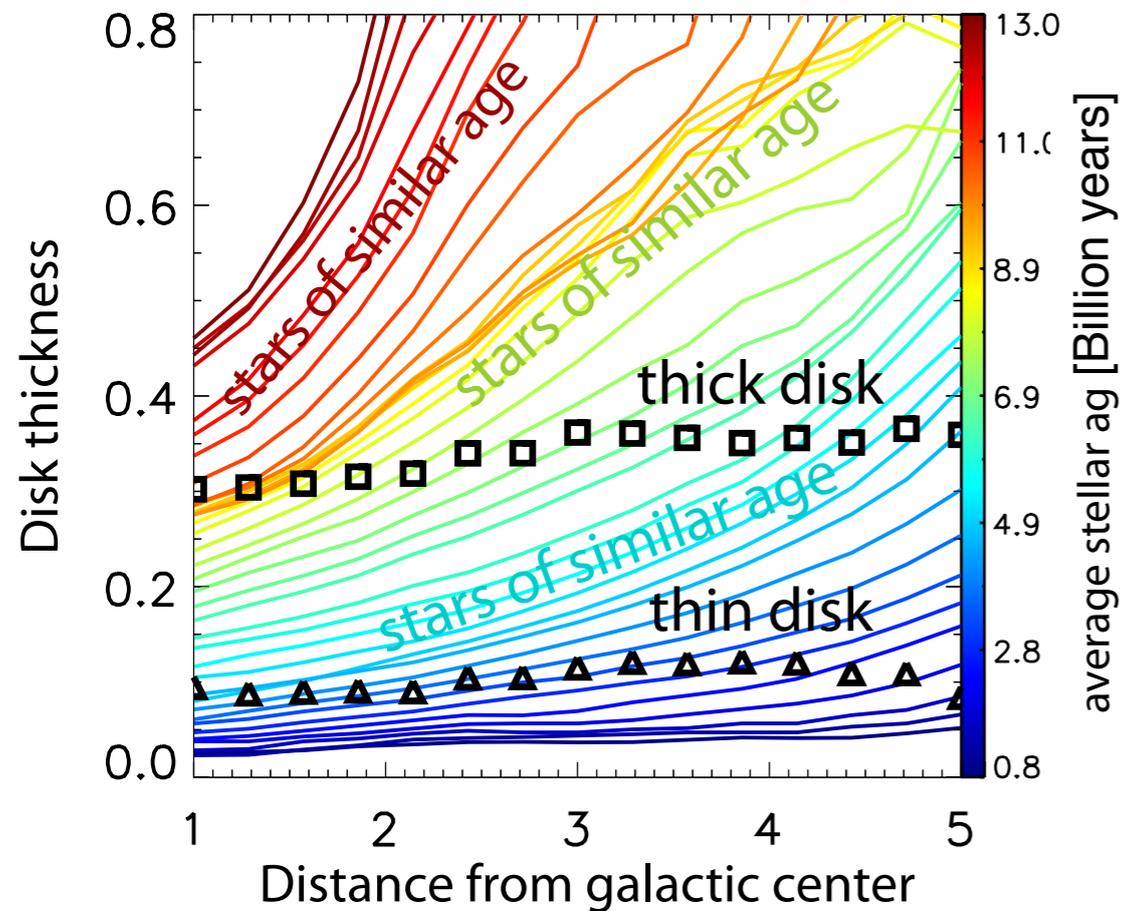
Seen in 2 simulation suites: by Martig and by Aumer/Scannapieco

Flaring also reported in FIRE (Ma et al. 2016) and Auriga simulations (Grand et al. 2016)

See also poster by A. Spagna

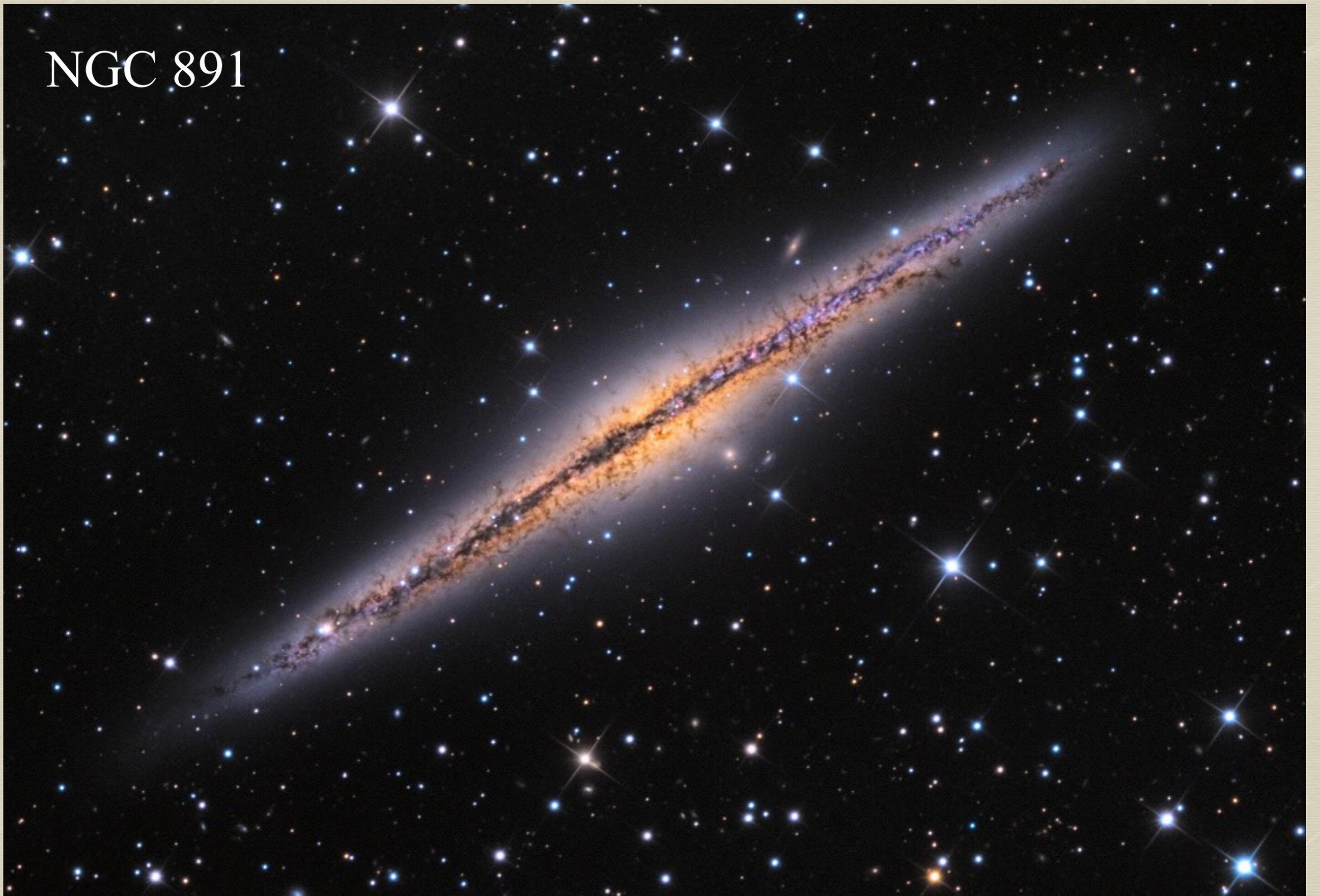
Age gradient in thick disk predicted

Chemical thick disk \neq
Morphological thick disk



Minchev et al. (2015)

NGC 891



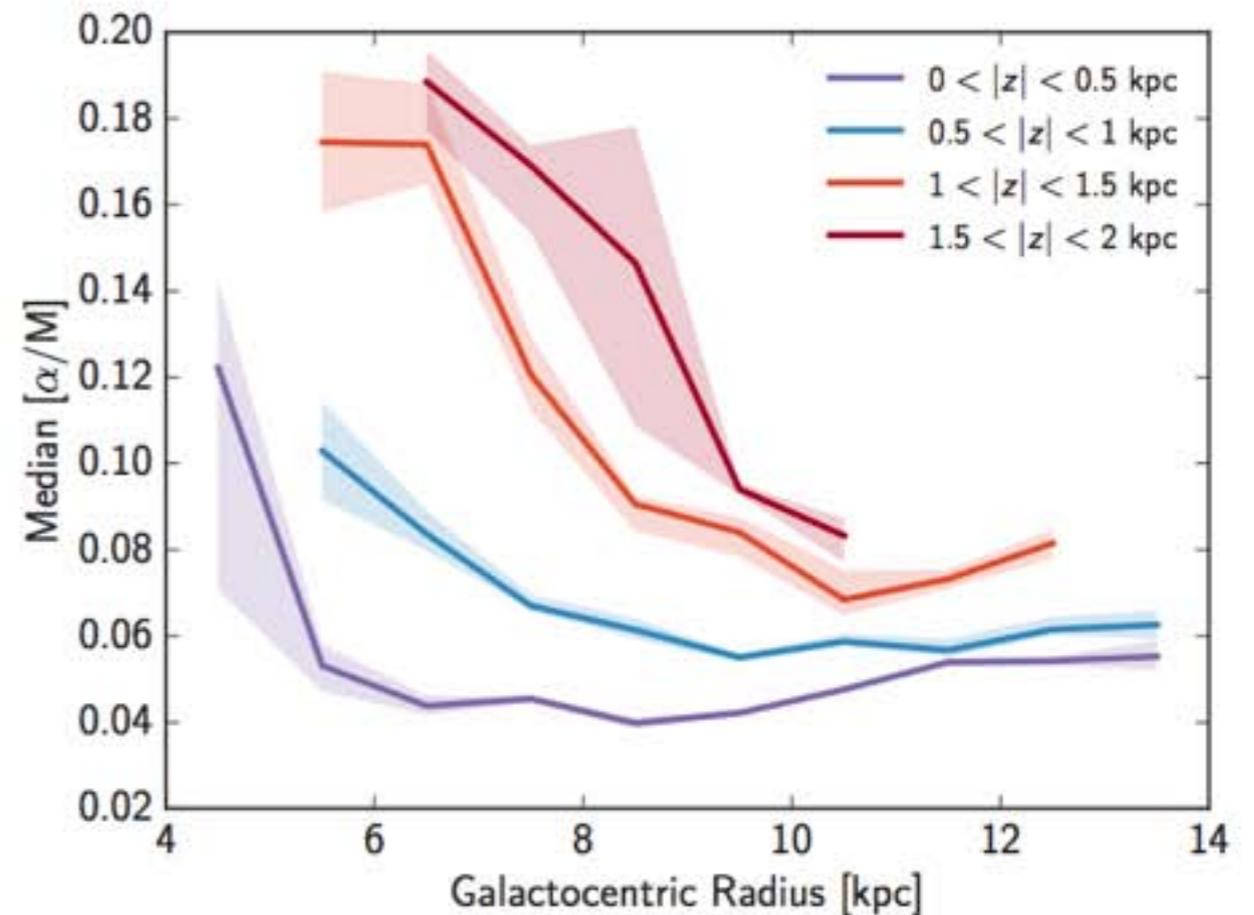
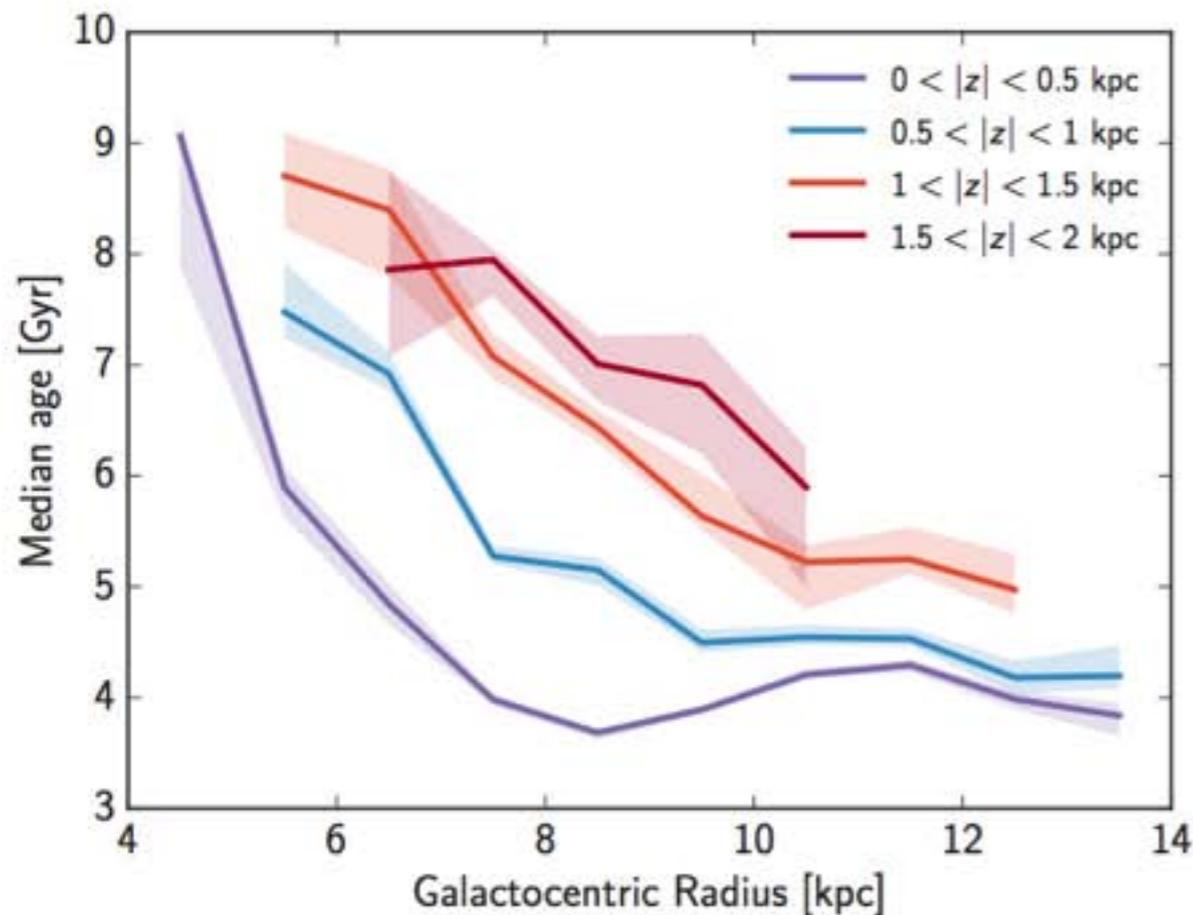
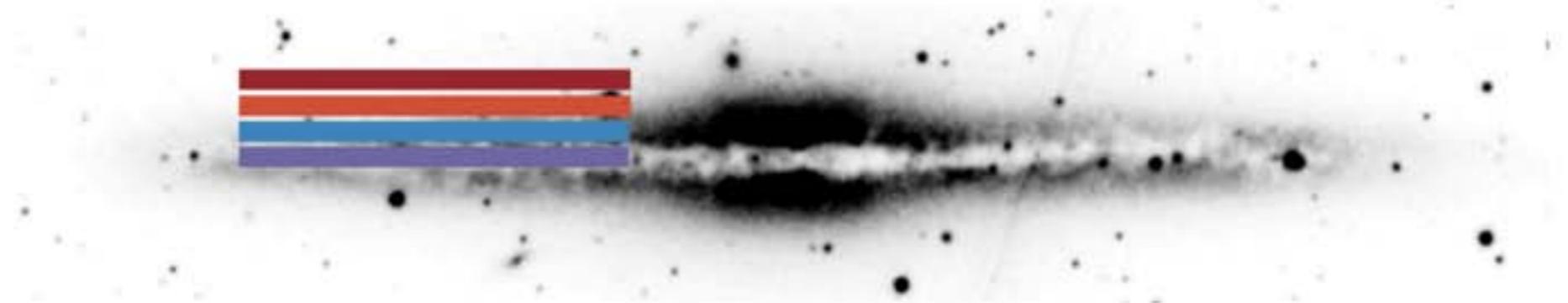
NGC 891



Thick disks result from the nested flares of mono-age stellar populations

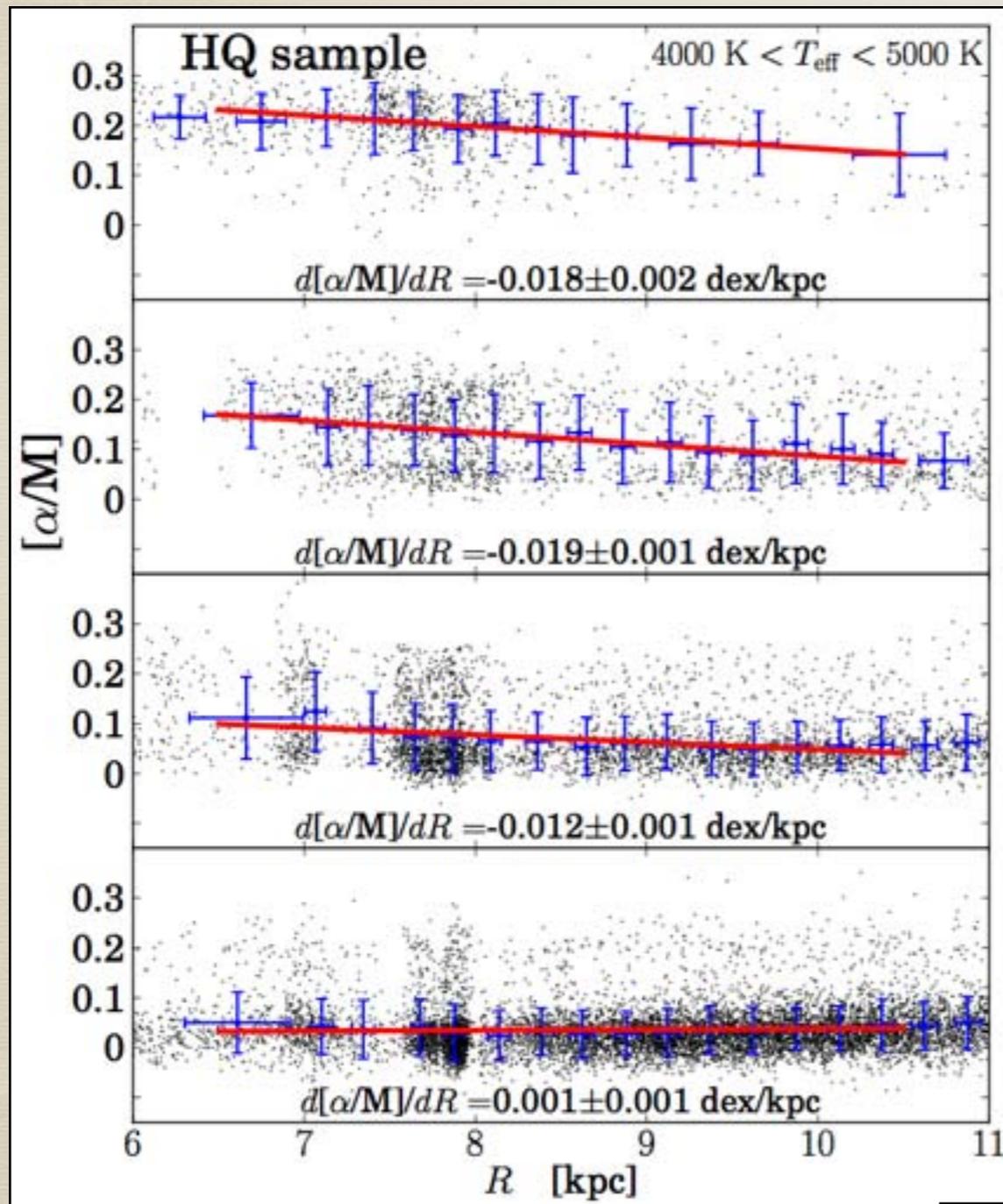
Negative age and $[\alpha/\text{Fe}]$ gradients at high $|z|$ in APOGEE

Consistent with flaring of mono-age populations



Martig, Minchev et al. (2016)

Consistent with: Inversion in $[\alpha/\text{Fe}]$ gradient away from disk plane



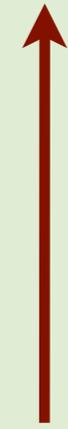
APOGEE data

$1.5 < |z| < 3.0 \text{ kpc}$

$0.8 < |z| < 1.5 \text{ kpc}$

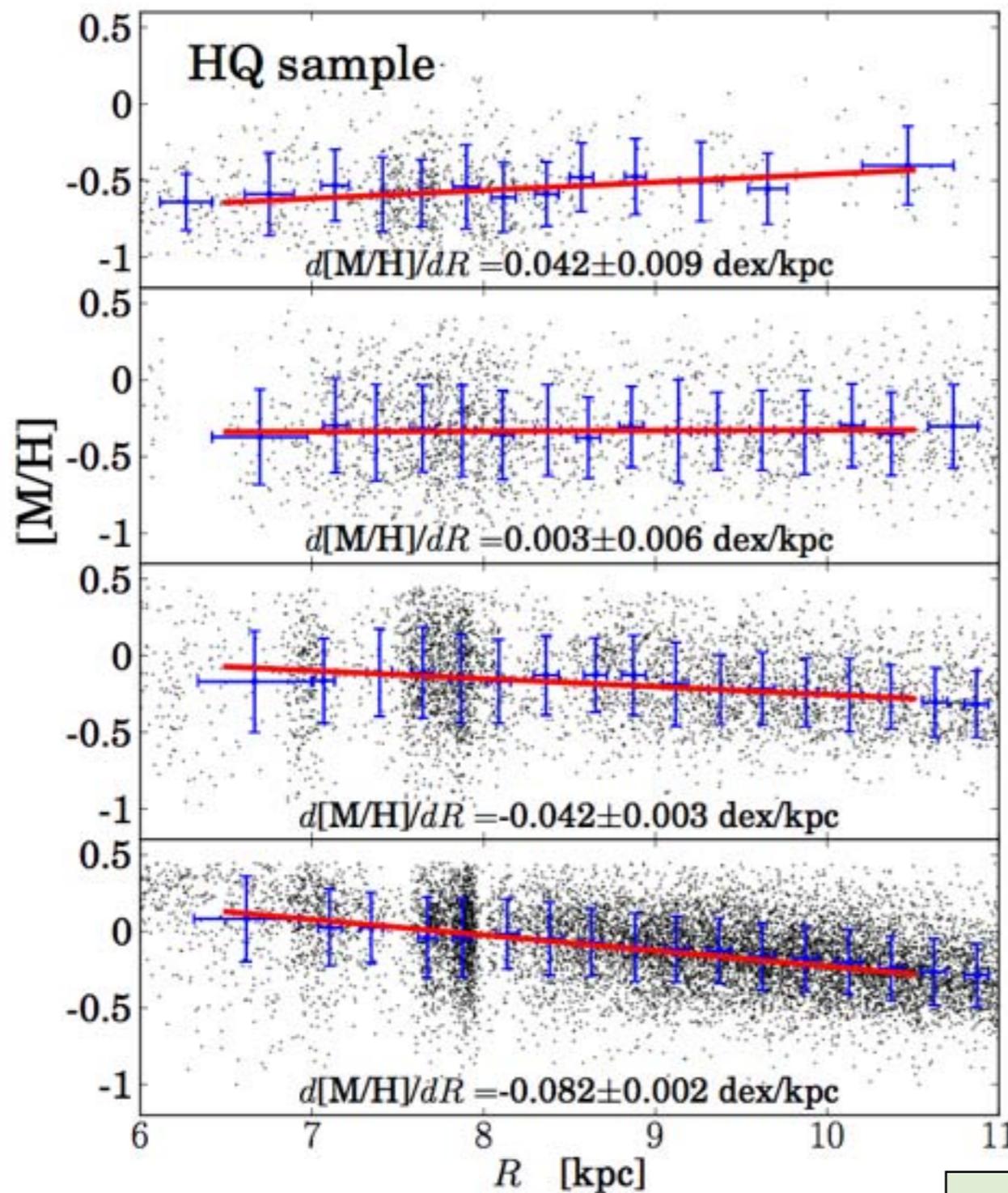
$0.4 < |z| < 0.8 \text{ kpc}$

$0.0 < |z| < 0.4 \text{ kpc}$

Distance from disk plane 

Anders et al. (2014)

Consistent with: Inversion in [M/Fe] gradient away from disk plane



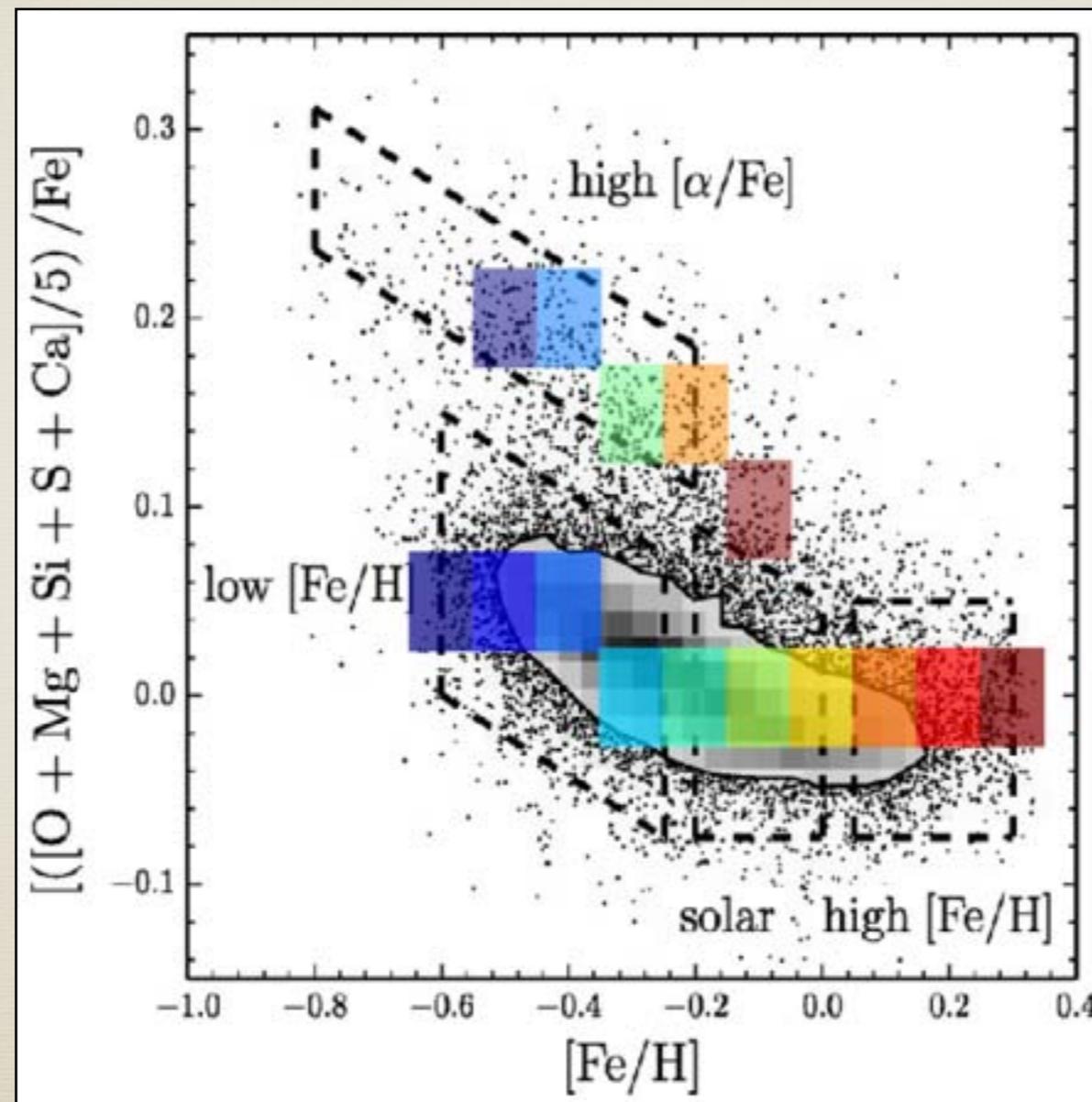
Distance from disk plane ↑

APOGEE data

Also seen in RAVE (Boeche + RAVE. 2014)
and in SEGUE (Cheng et al. 2012)

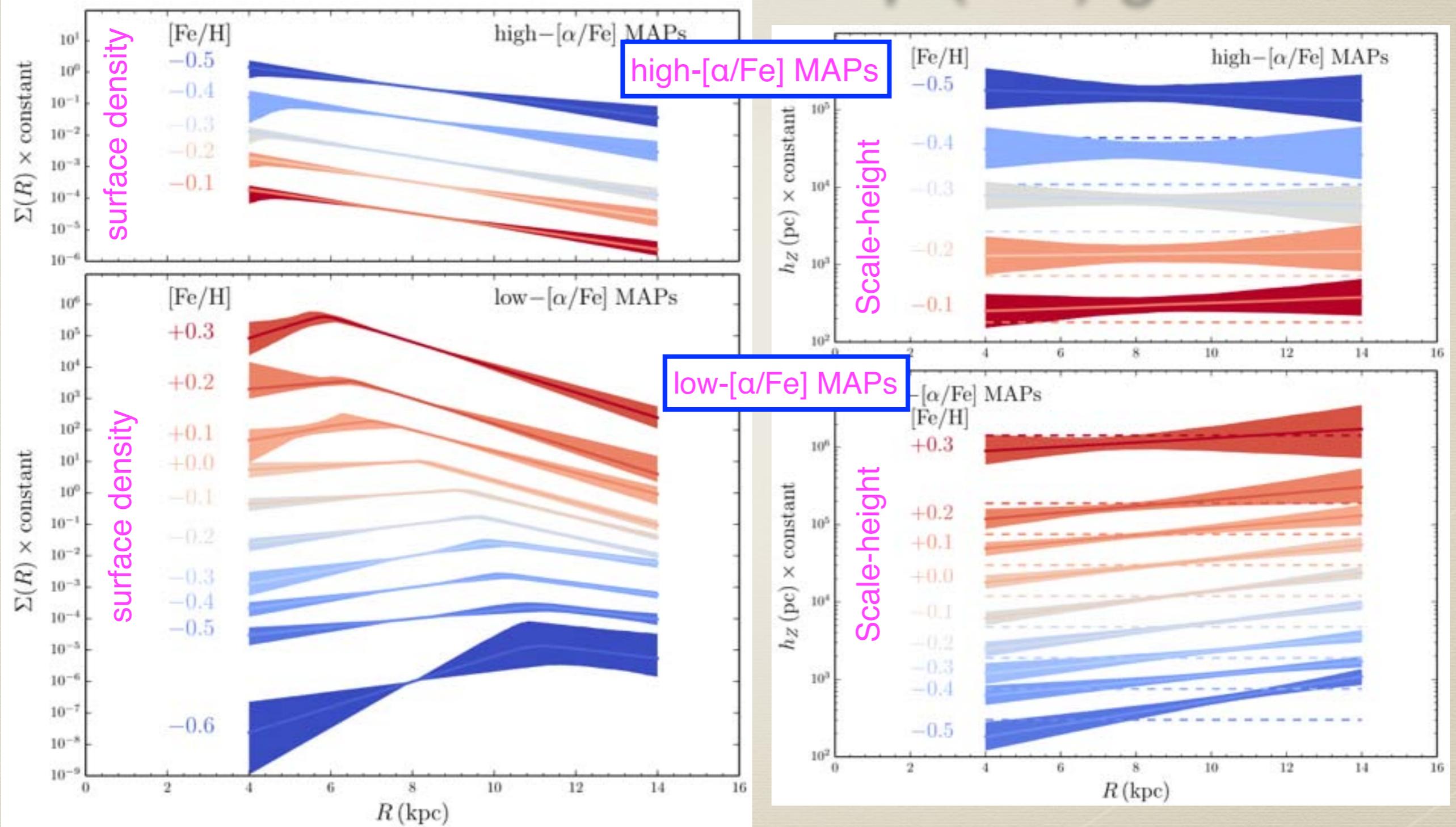
Anders et al. (2014)

Mono-abundance populations (MAPs) in APOGEE red clump (RC) giants



Bovy et al. (2016)

Mono-abundance populations (MAPs) in APOGEE red clump (RC) giants

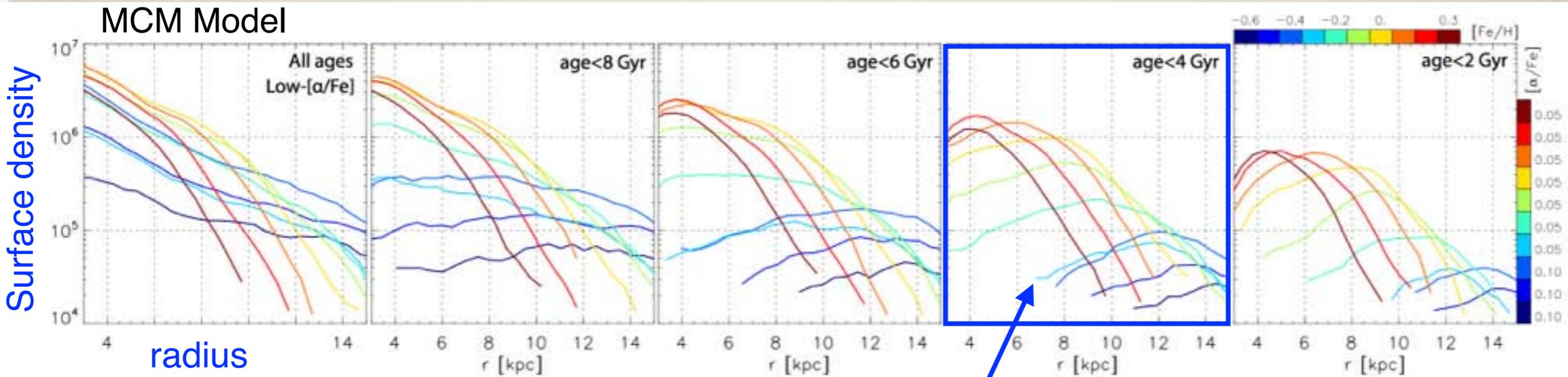


Variation in the shape of MAPs surface density with age

age decreases

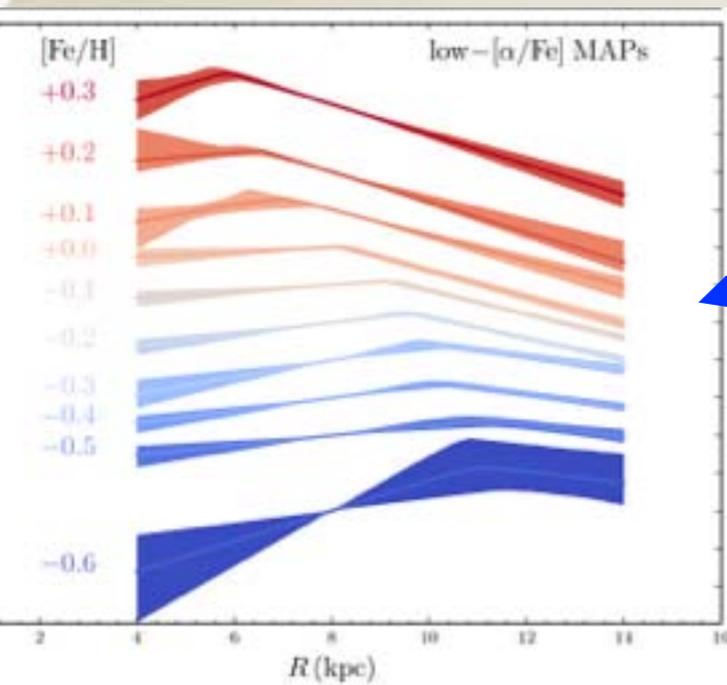


MCM Model



Surface density

radius

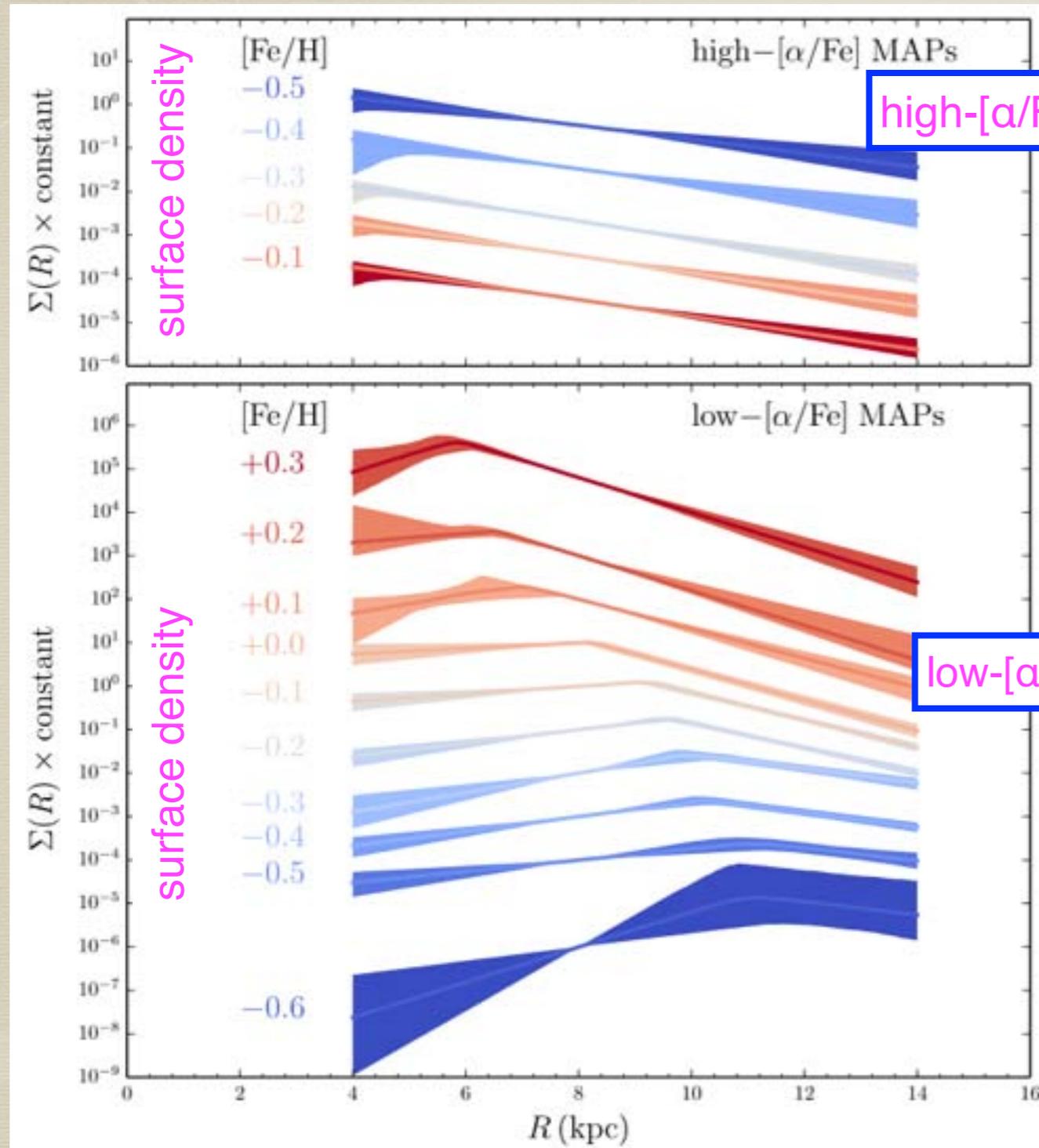


Red-clump sample peaks at age = 2-4 Gyr

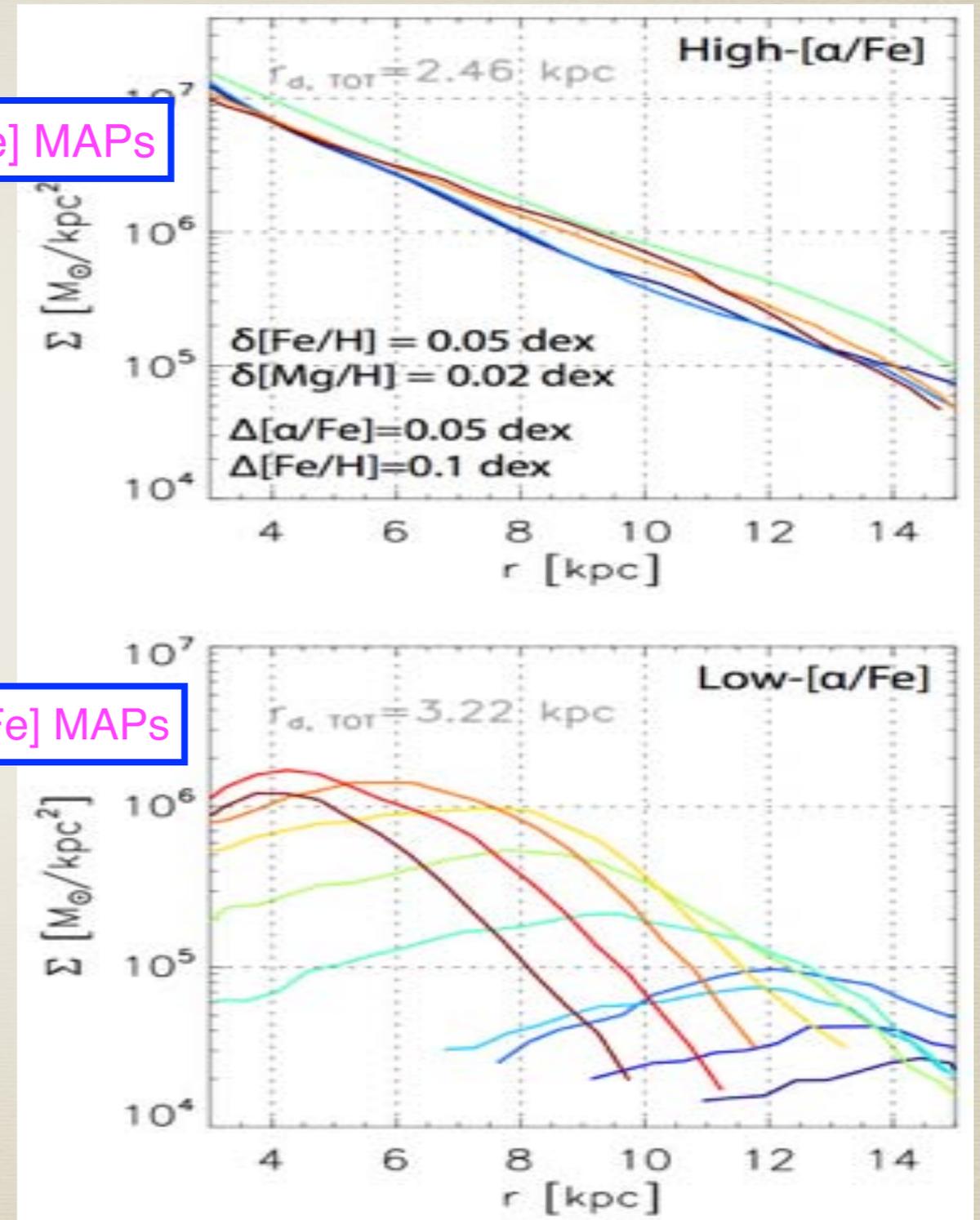


MAPs probably not mono-age!

Matching APOGEE density profiles



Bovy et al. (2016)



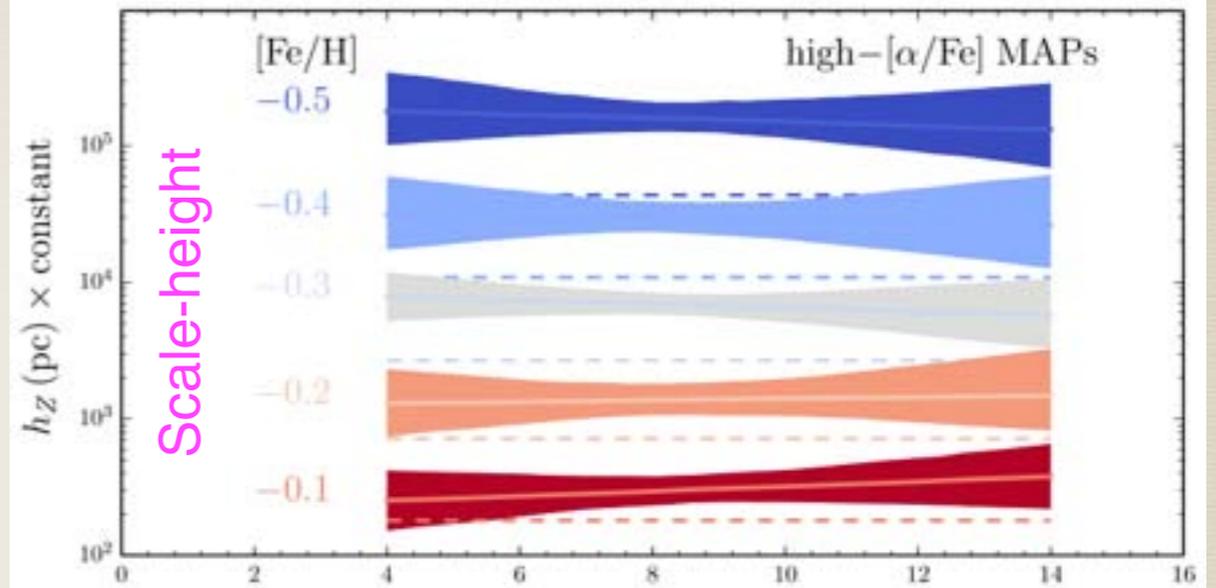
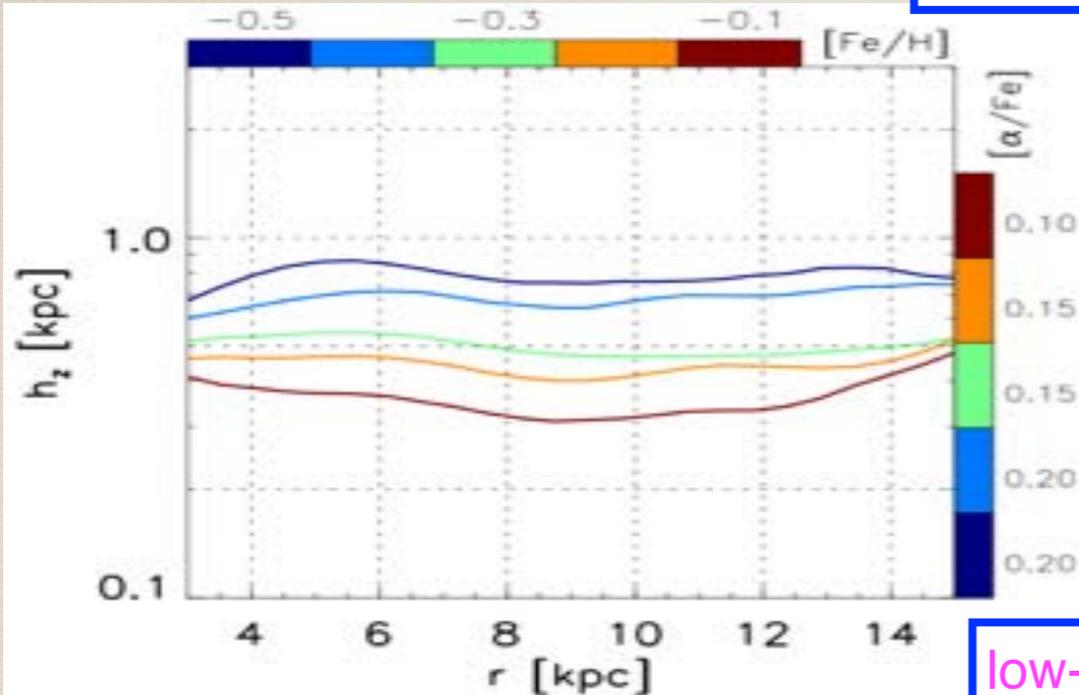
Minchev et al. (2016), model

Matching APOGEE disk thickness variation with radius

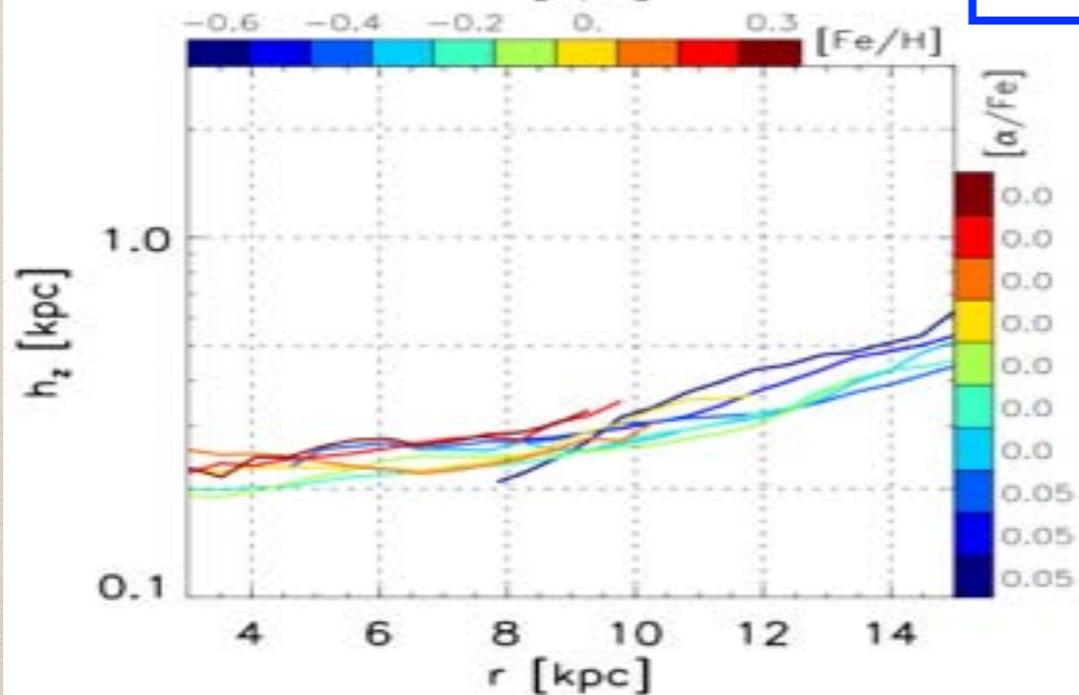
Flaring lost in model high- $[\alpha/\text{Fe}]$ MAPs, although present for all mono-ages!!

high- $[\alpha/\text{Fe}]$ MAPs

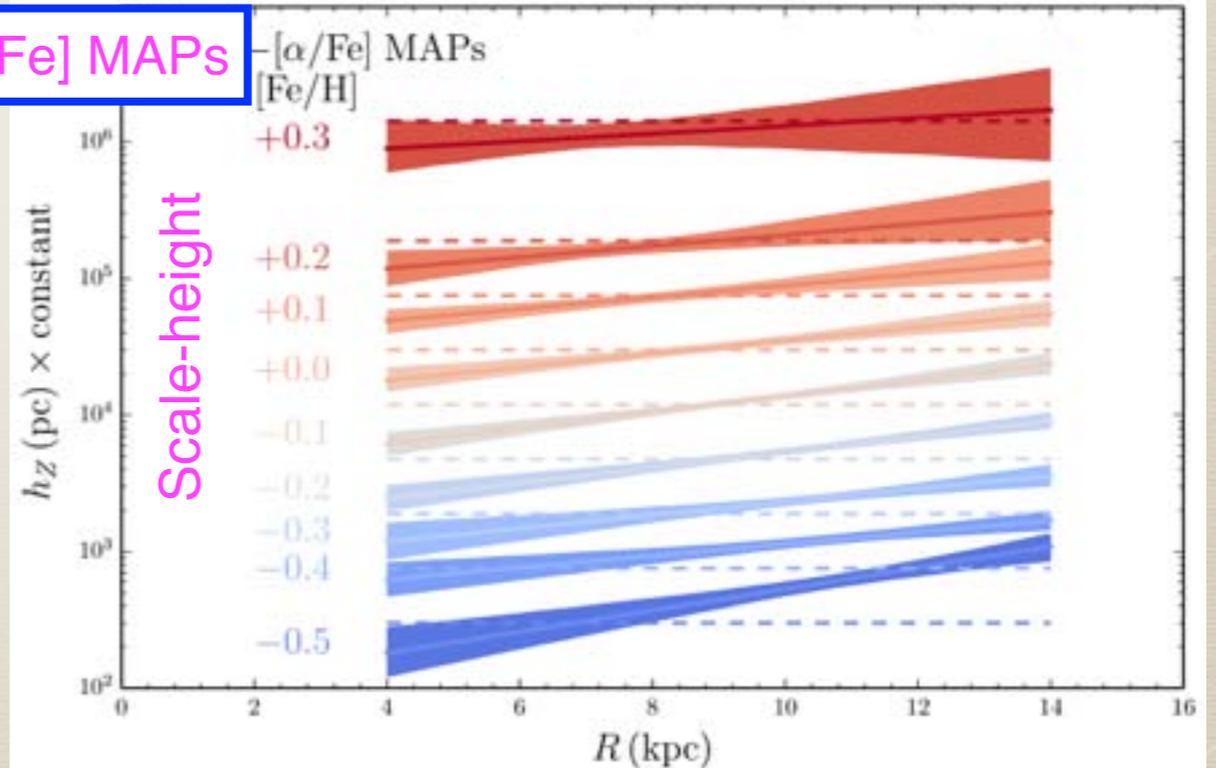
Scale-height



Scale-height



low- $[\alpha/\text{Fe}]$ MAPs



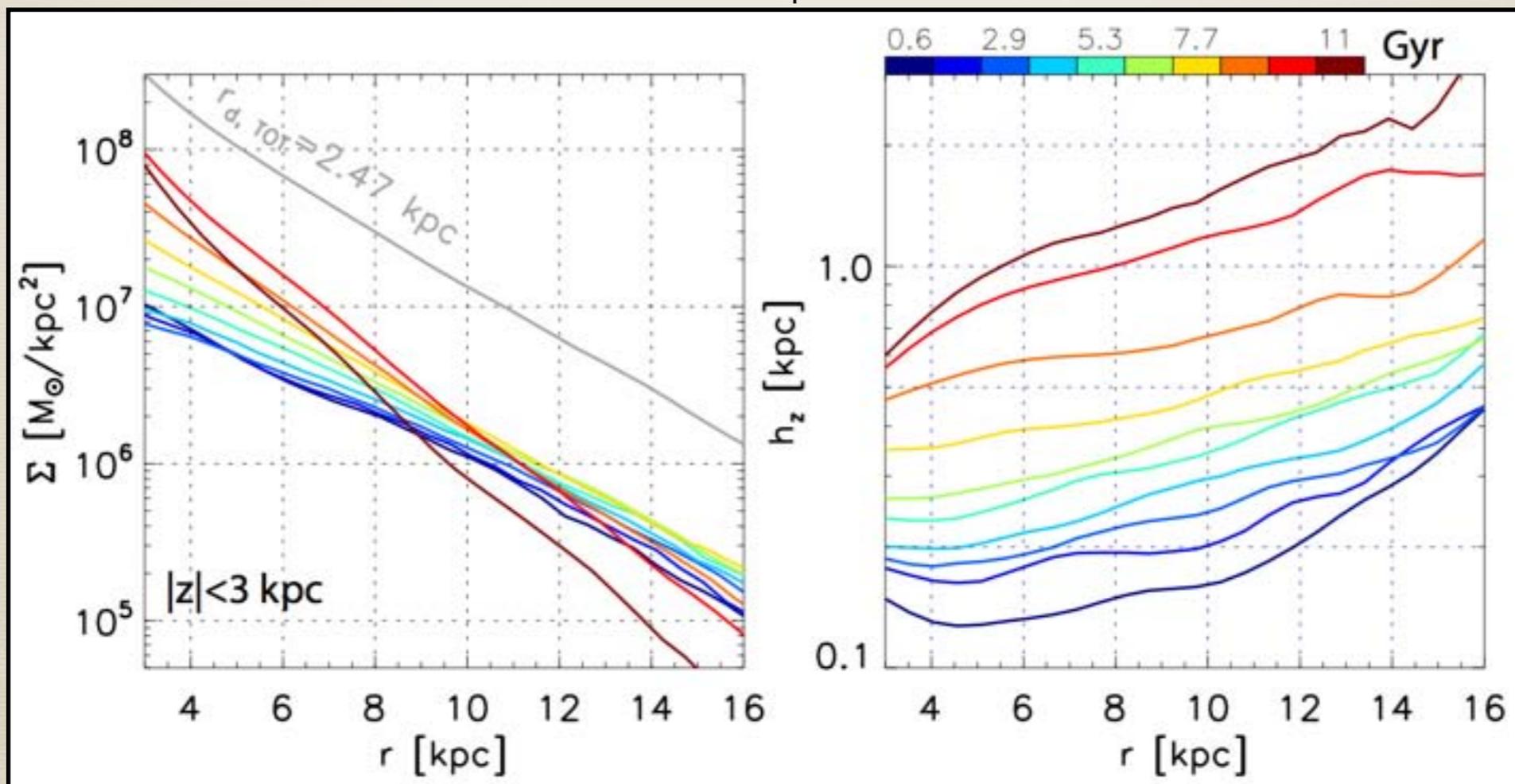
Minchev et al. (2016), model

Bovy et al. (2016)

Disk structure in our model at the final simulation time

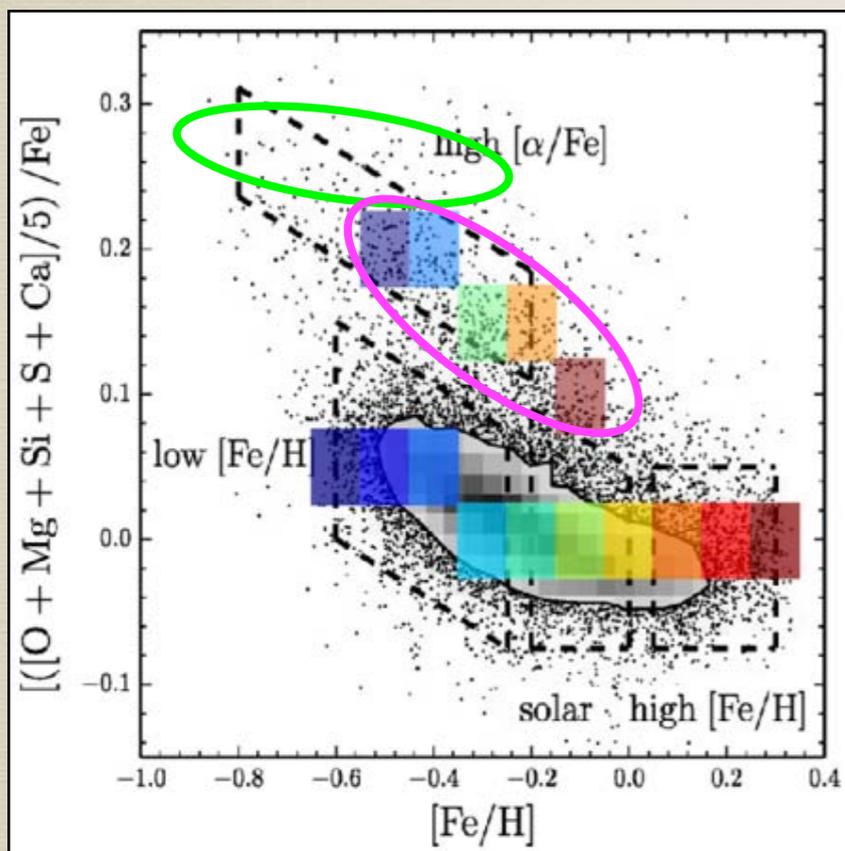
- Older populations more centrally concentrated as expected for the Milky Way
- Flaring present for all mono-age populations

Note that flaring is always present in mono-ages, although lost in model MAPs (previous slide)

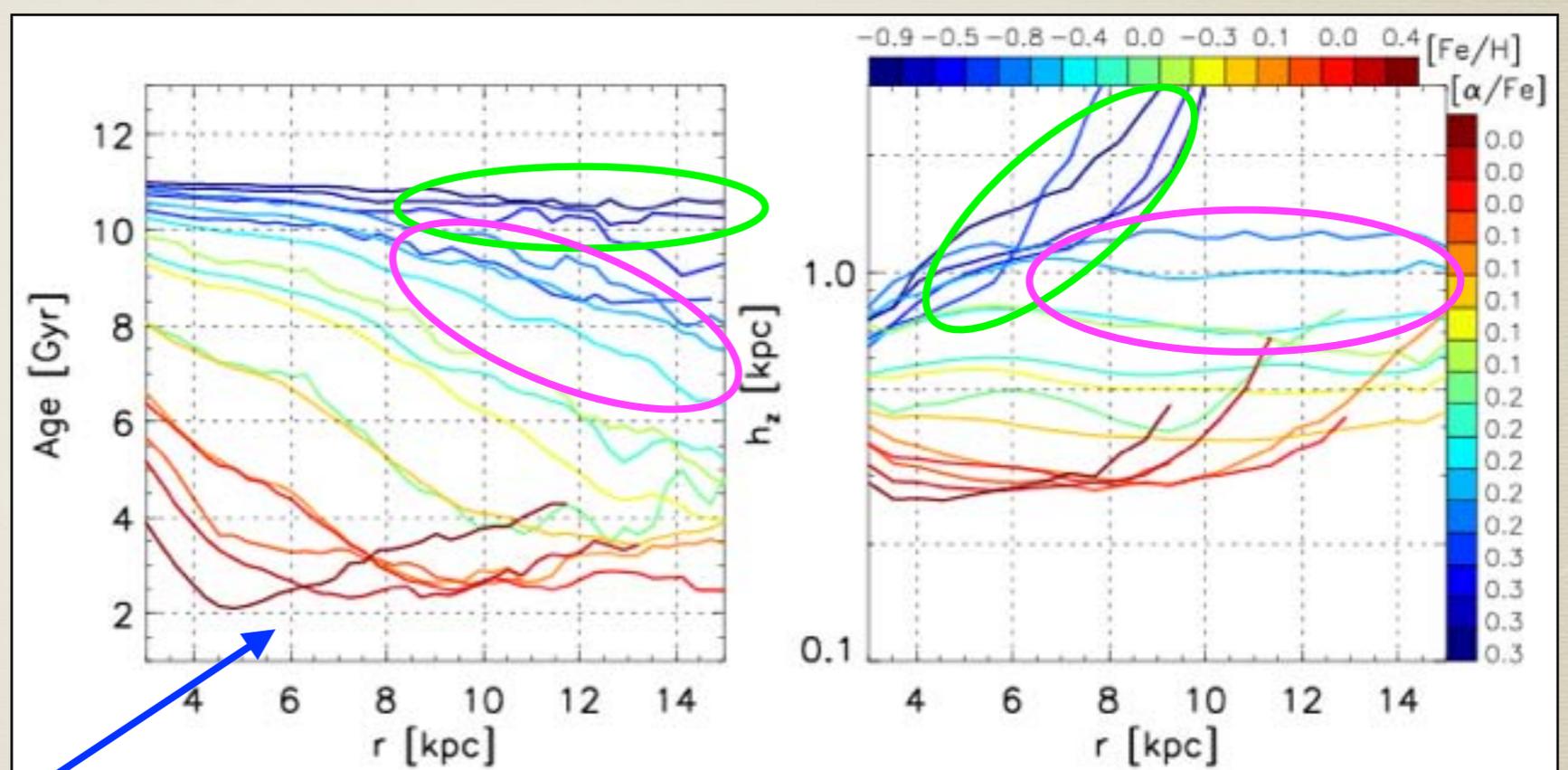


Why is flaring lost in model when MAPs considered?

- Note that APOGEE RC MAPs limited to $[\alpha/\text{Fe}] < 0.2$ and $[\text{Fe}/\text{H}] < 0.5$ dex
- Negative age gradient of high- $[\alpha/\text{Fe}]$ MAPs causes the lack of flaring



Bovy et al. (2016)

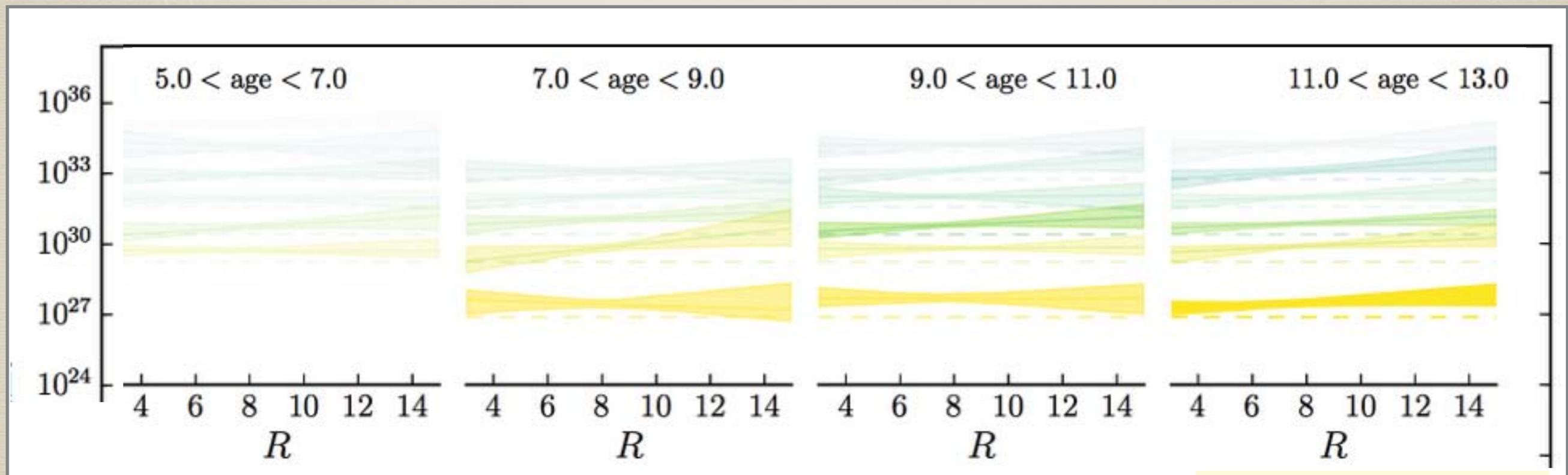


Minchev et al. (2016), MCM model

- Due to a mixture of ages, flaring in low- $[\alpha/\text{Fe}]$ MAPs not easily interpreted.
- We predict flaring in the highest $[\alpha/\text{Fe}]$ MAPs - larger sample needed (APOGEE-2?).

APOGEE mono-age populations show flaring in old stars!

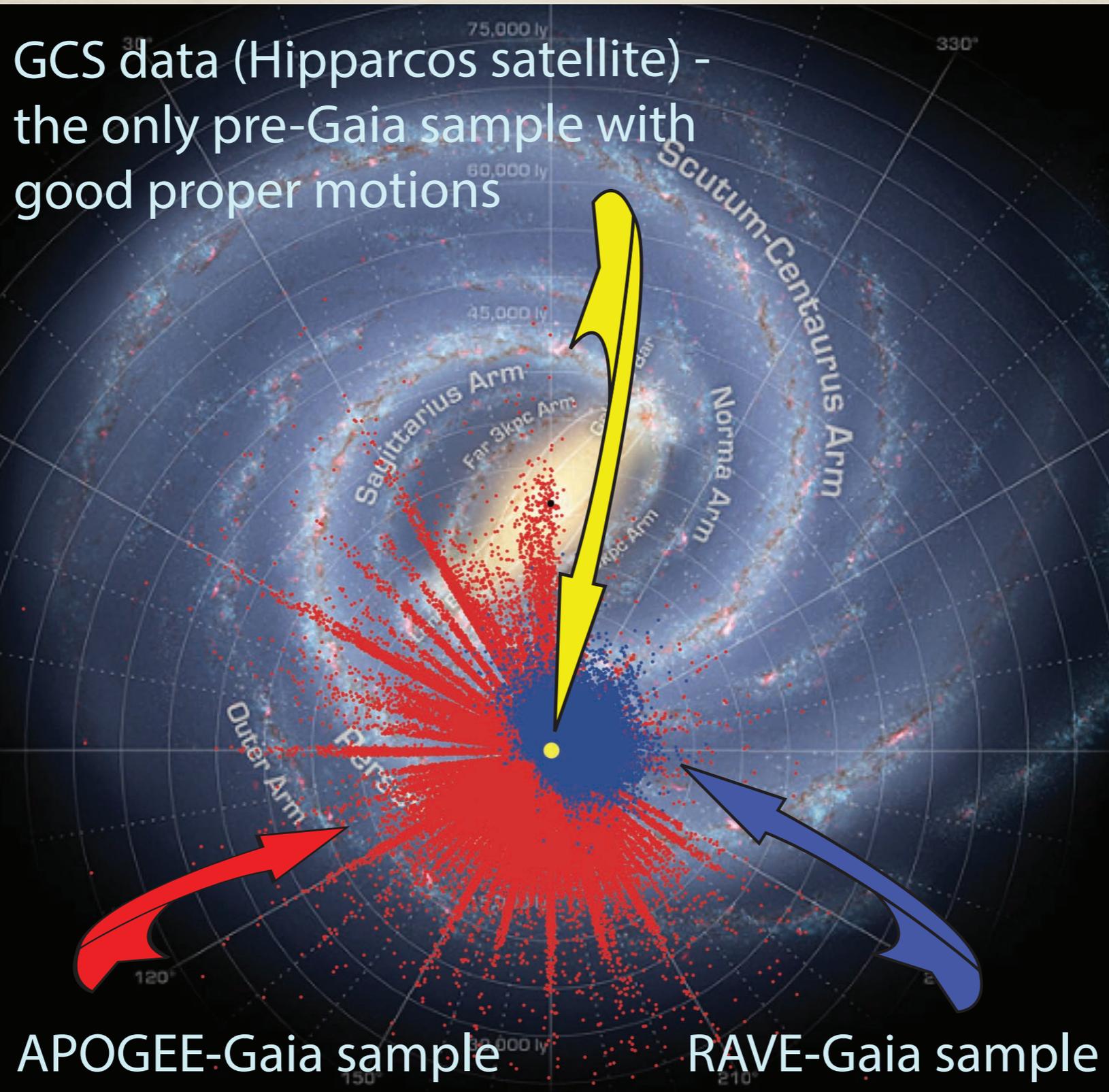
When APOGEE RC data are binned by age, **flaring does appear**



APOGEE ages based on C/N ratio,
calibrated by asteroseismology from
Martig et al. (2015)

Mackereth, Bovy et al.,
submitted

Gaia+APOGEE and Gaia+RAVE samples (at the end of Gaia mission)



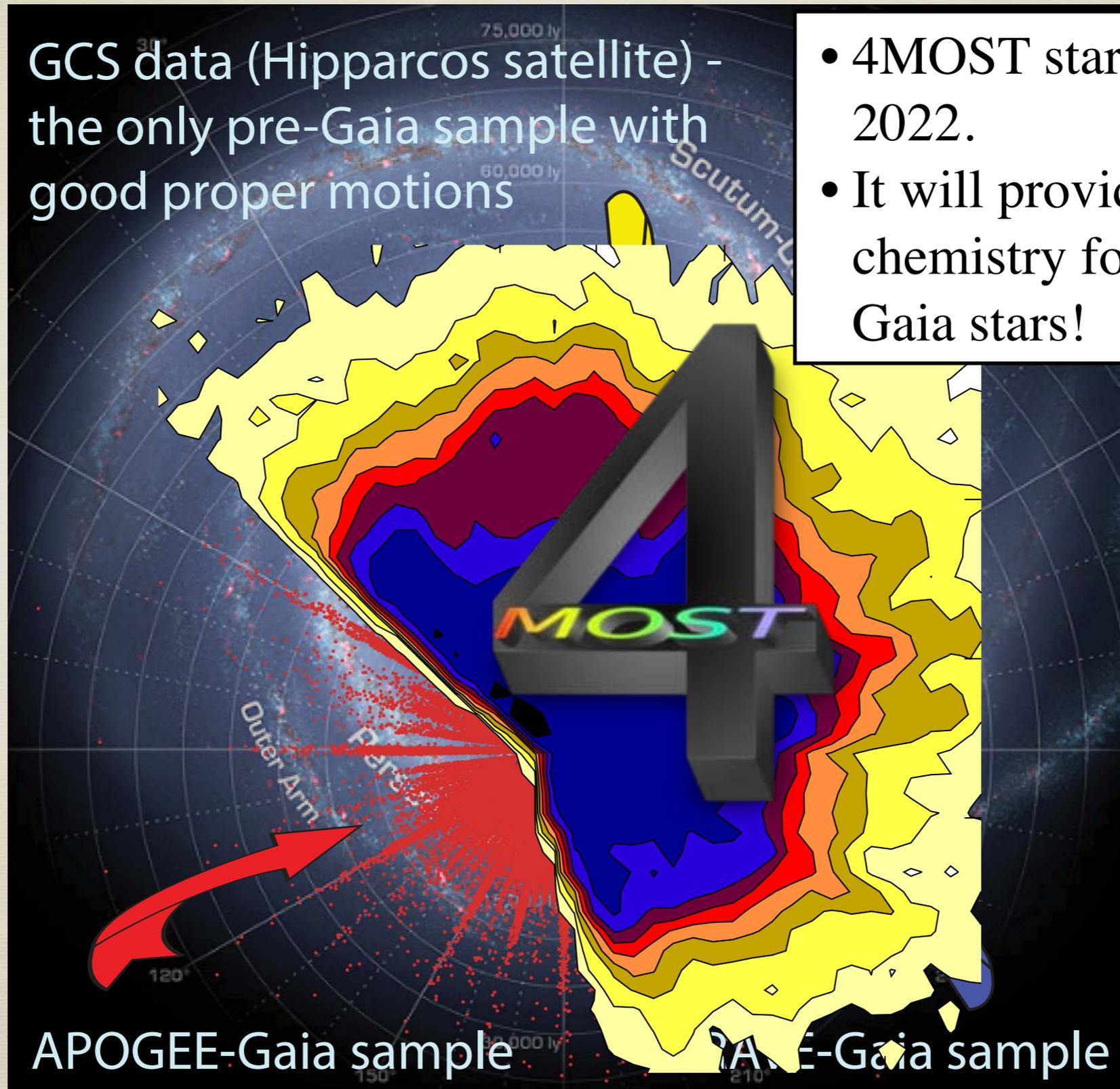
Gaia+APOGEE and Gaia+RAVE samples (at the end of Gaia mission)

GCS data (Hipparcos satellite) -
the only pre-Gaia sample with
good proper motions

- 4MOST starts operation in 2022.
- It will provide RVs and chemistry for 10-15 Million Gaia stars!

APOGEE-Gaia sample

RAVE-Gaia sample



Summary of the effects of radial migration

- **Radial migration can:**
 - Flare disks during quiescent times
 - Suppress disk flaring during mergers
 - Introduce scatter in the AMR
 - Explain the high metallicity tail
- **Radial migration cannot:**
 - Explain the thick disks
 - Create a gap in the $[\alpha/\text{Fe}]$ - $[\text{Fe}/\text{H}]$ relation
 - Compete with inside out formation
 - Cannot be avoided - gotta deal with it!

Conclusions

- In order to interpret the unprecedented Gaia + follow-up surveys data, **simulation in cosmological context are needed!**
- Improvements in simulations needed with respect to resolution and chemical treatment.
- **Radial migration unavoidable!** Have to deal with it.
- **Thick disk composed of the nested flares of mono-age populations**
 - disk flaring unavoidable!
 - total mass does not flare if inside-out formation
 - results in inversion of the metallicity, $[\alpha/\text{Fe}]$, and age gradients with increasing distance from the disk midplane.
- Mono-abundance populations (MAPs) **most likely not mono-age.**
- **Age information is crucial for understanding the Milky Way disk structure and evolution** - great expectations from Kepler, PLATO and TESS in the near future!