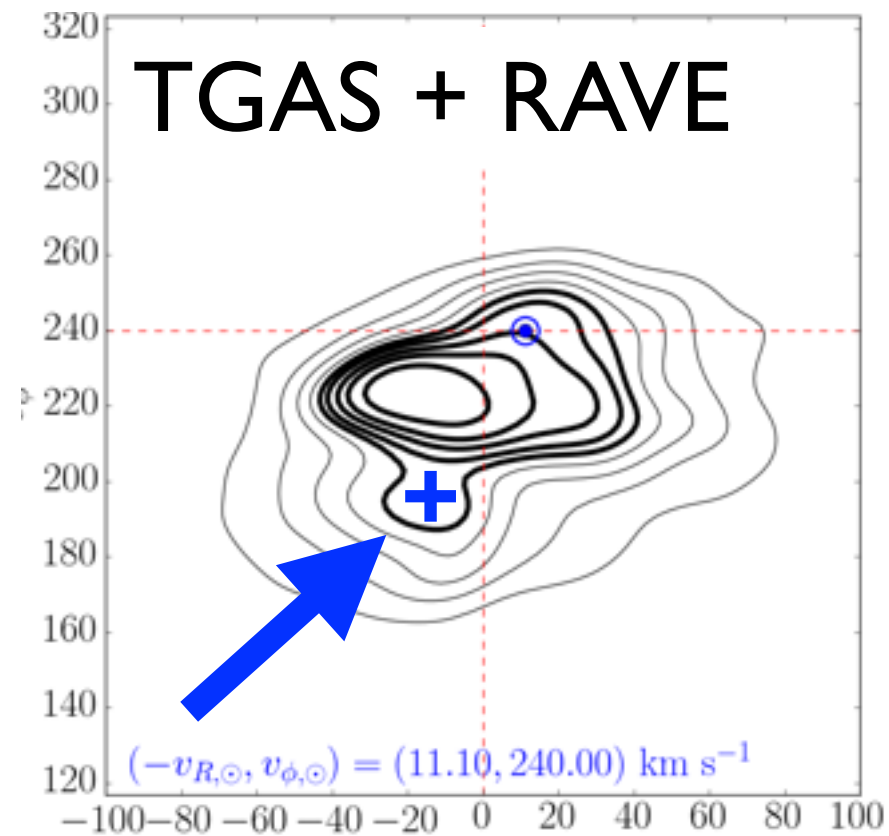
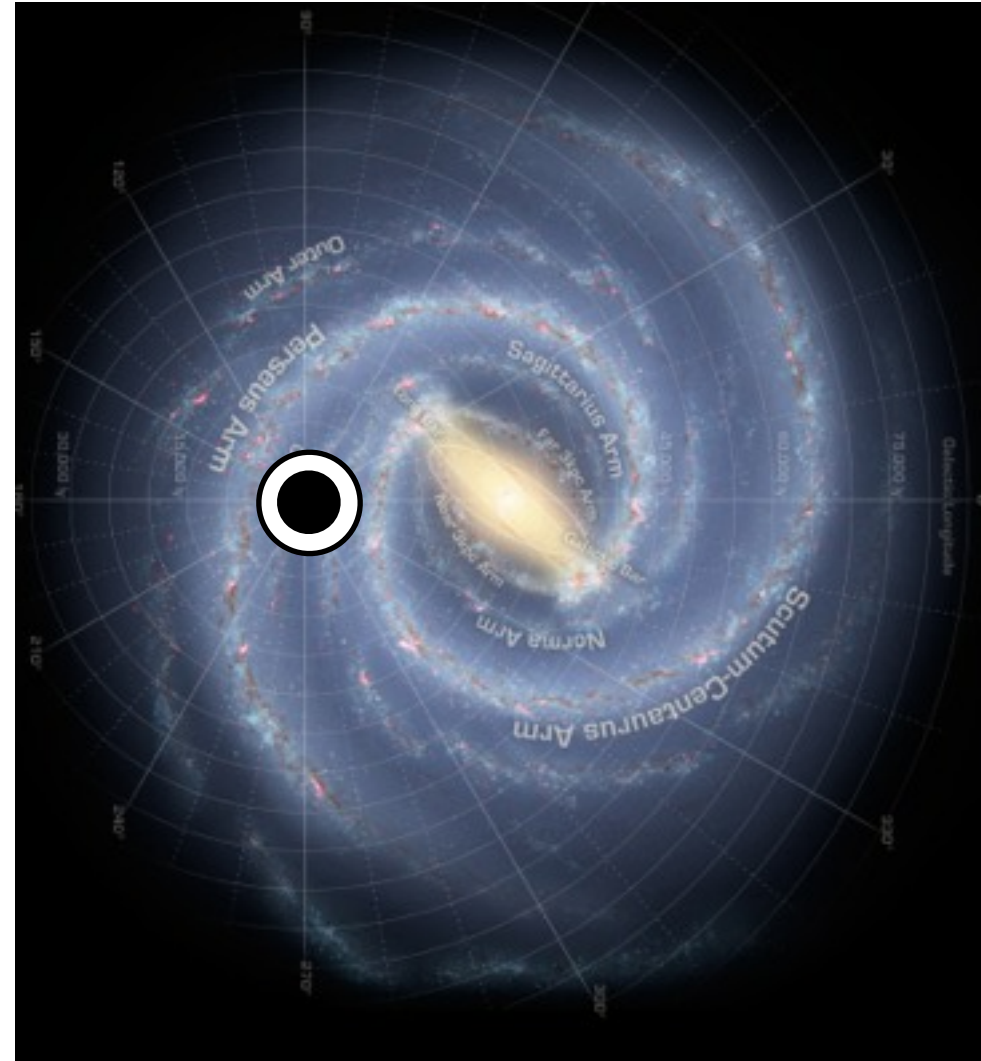


Dynamical effects of the **spiral arms** on the velocity distribution of disc stars

$$v_{\phi}$$



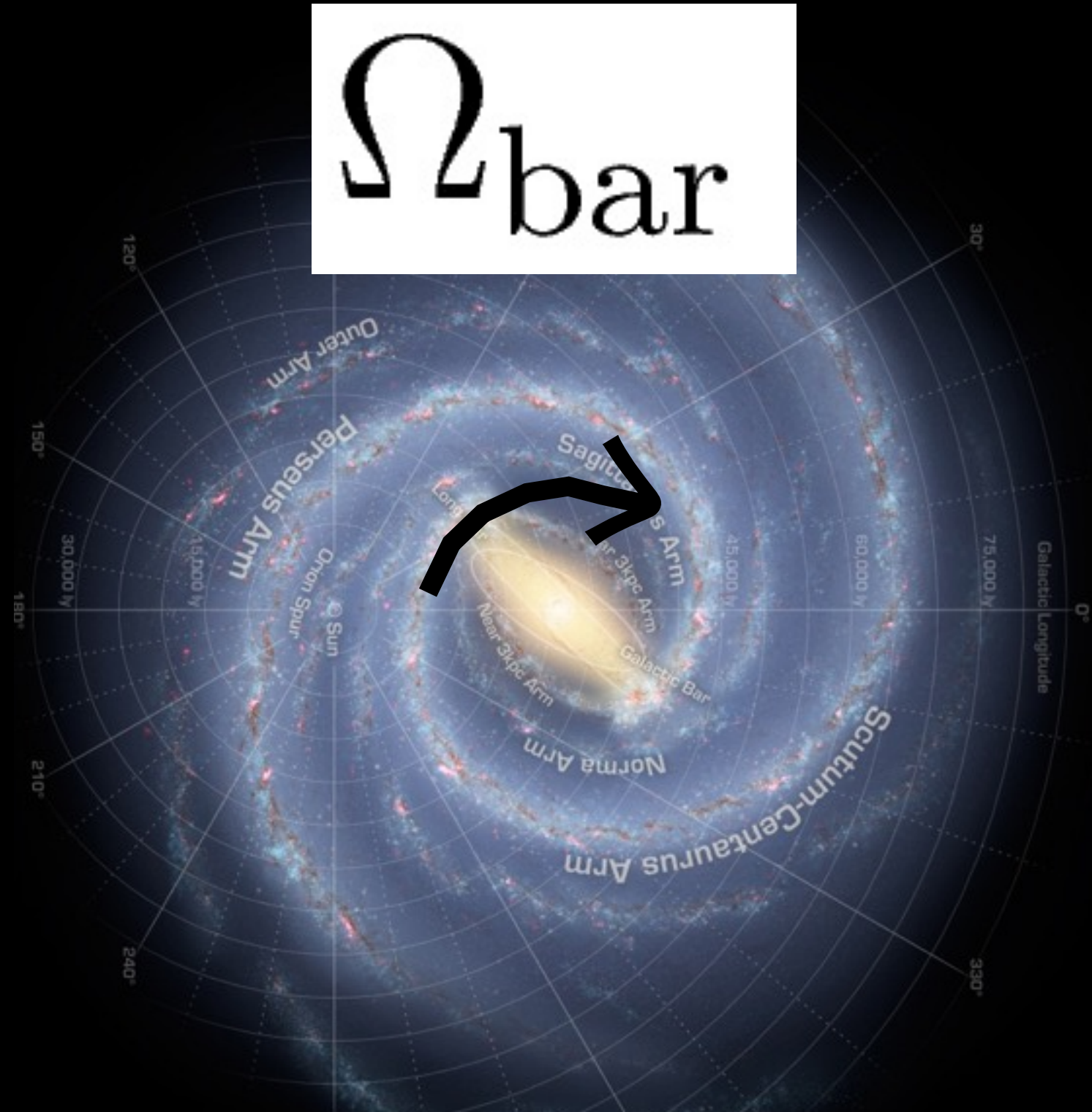
$$-v_R$$



Kohei Hattori (Michigan)

N. Gouda, T. Yano, N. Sakai, H. Tagawa (NAOJ)

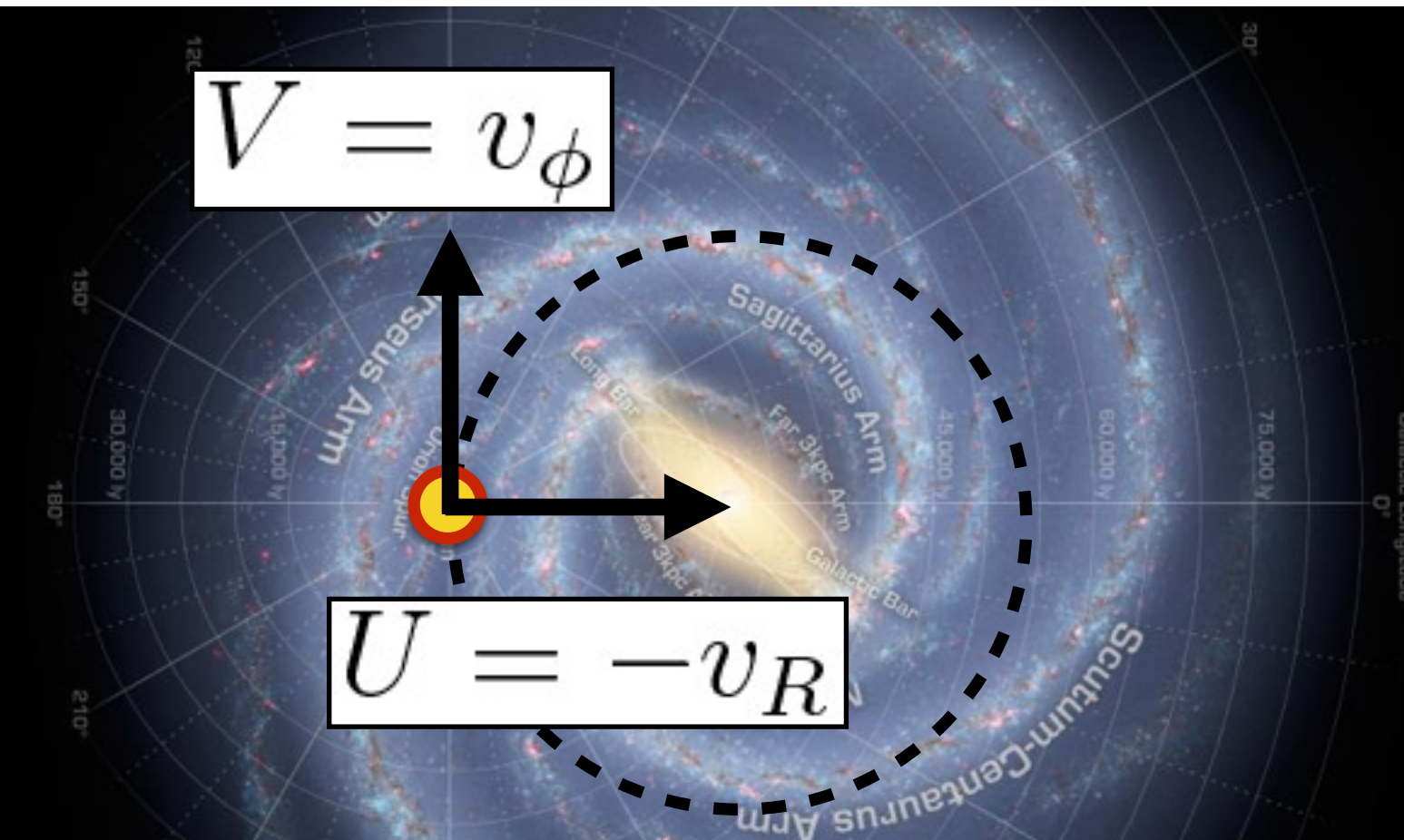
$\bar{\Omega}$



velocity substructure @ Sun

due to **bar** ?

$$V = v_\phi$$

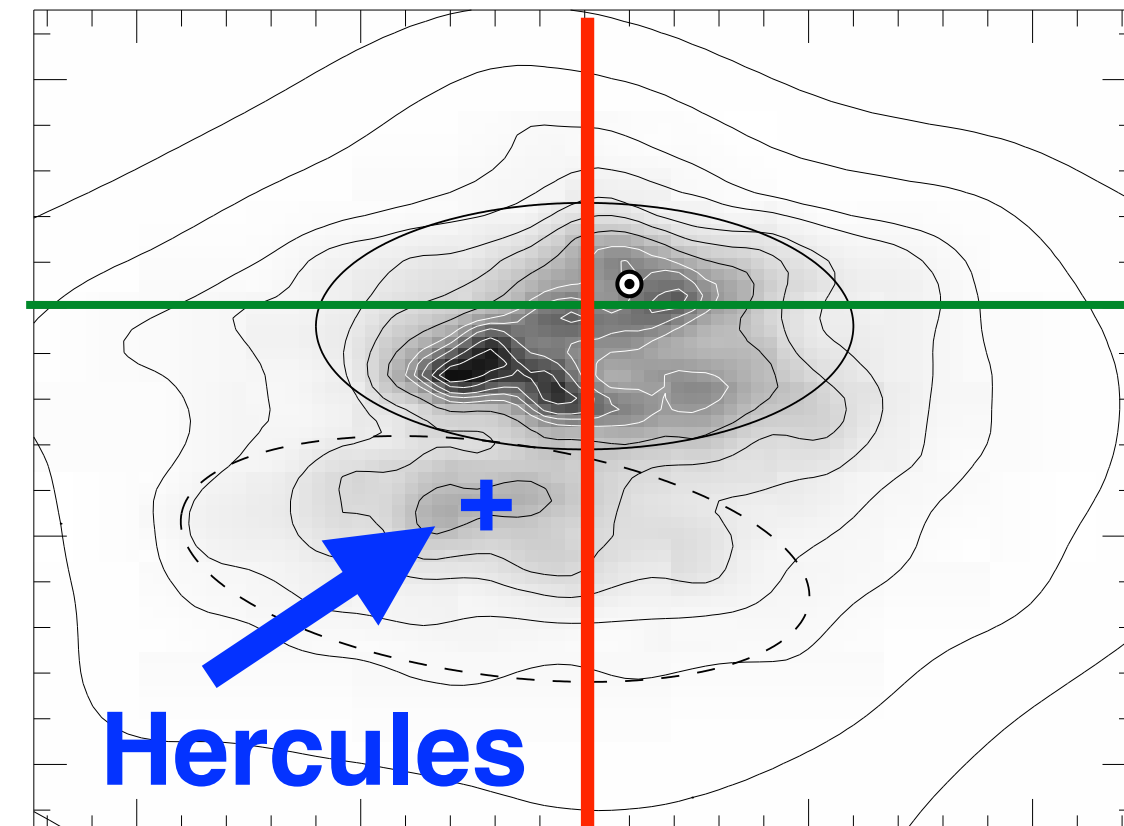


270

220

170

120



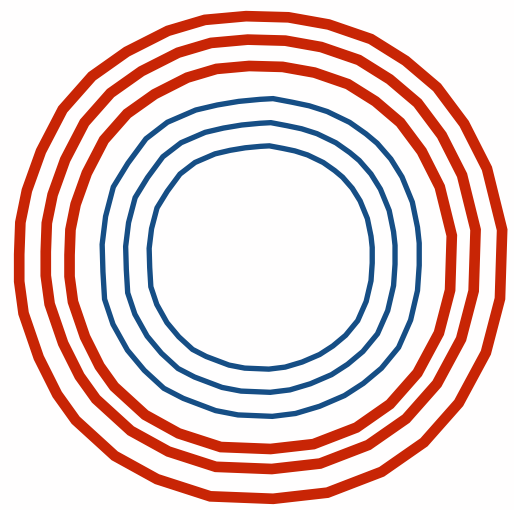
-100 -50 0 50 100 [km/s]

$$U = -v_R$$

Dehnen (2000)

axisymmetric

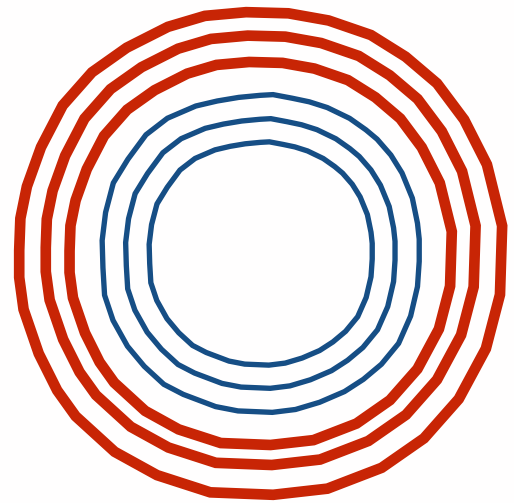
time



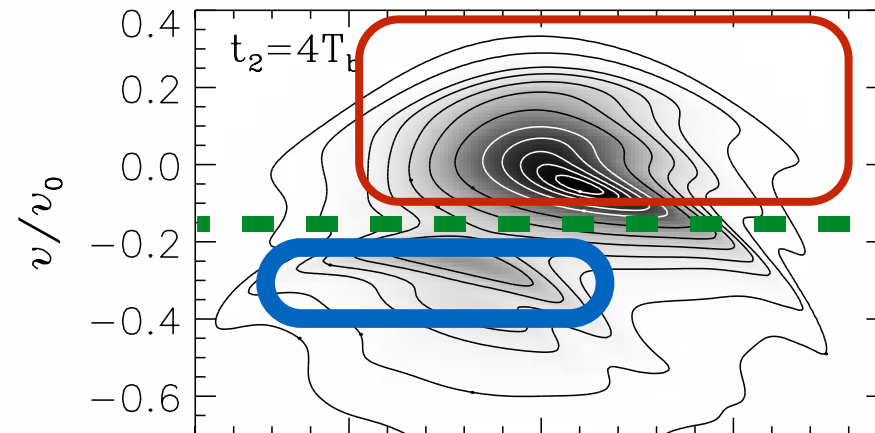
axisymmetric

time

bar formation

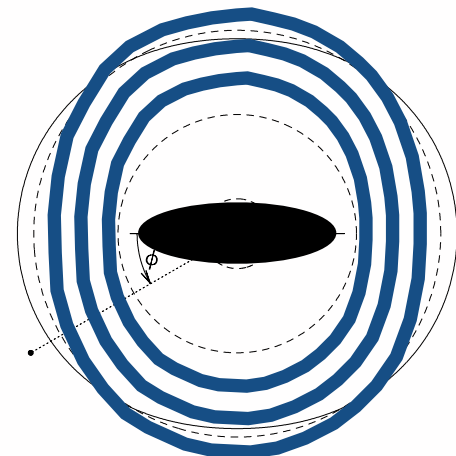


$$R > R(OLR)$$



Outer Lindblad Resonance

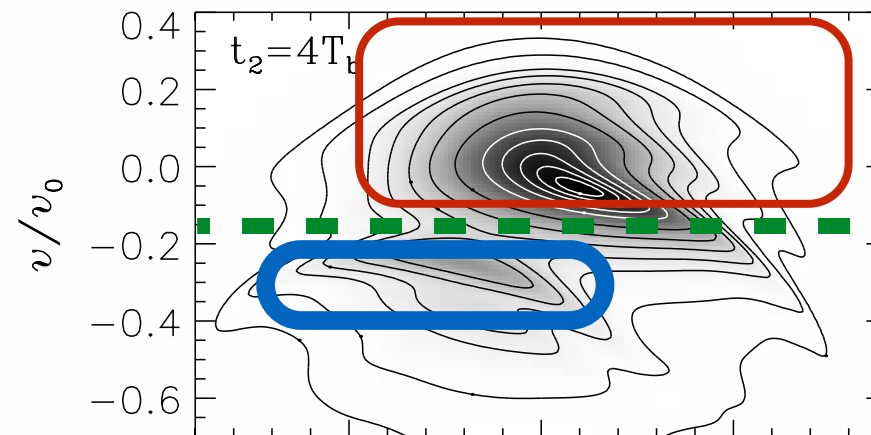
$$R(OLR) = \left(1 + \frac{1}{\sqrt{2}}\right) \frac{v_0}{\Omega_{\text{bar}}}$$



$$R < R(OLR)$$

Dehnen (1999)

$$\Omega_{\text{bar}} = 53 \pm 3 \text{ km/s/kpc}$$



**Outer Lindblad
Resonance**

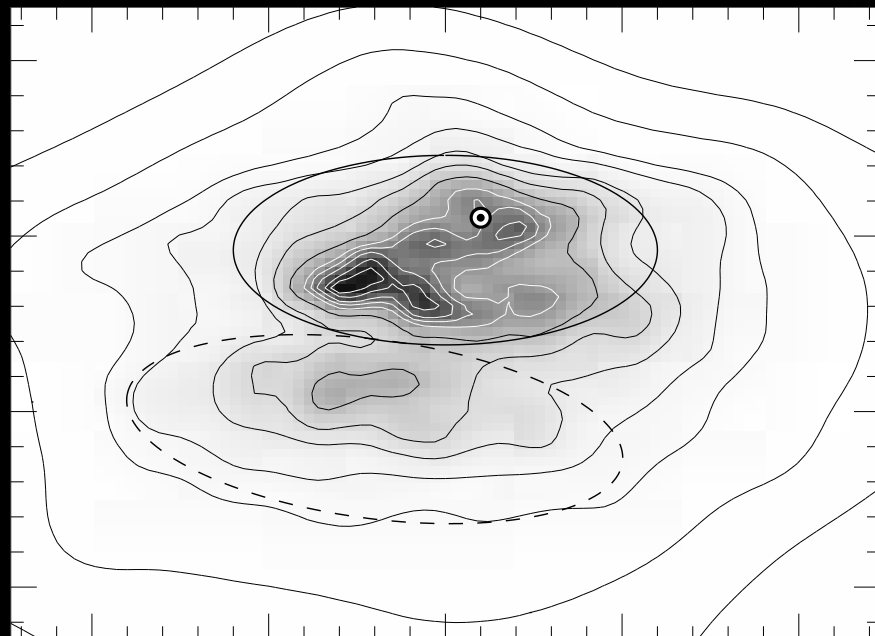
$$R(OLR) = \left(1 + \frac{1}{\sqrt{2}}\right) \frac{v_0}{\Omega_{\text{bar}}}$$

Fast bar?

$$\Omega_{\text{bar}} =$$

53 km/s/kpc

local data



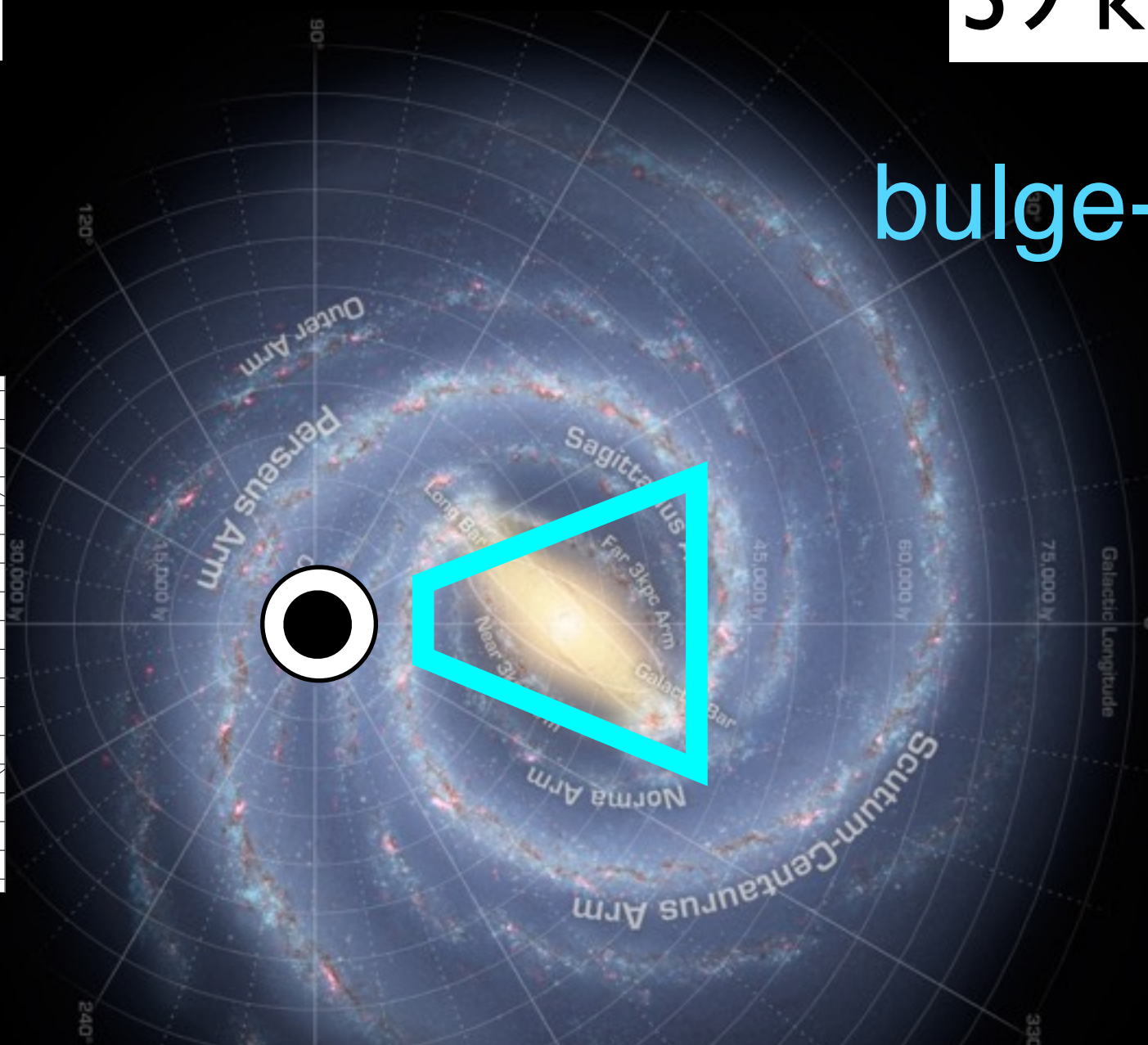
Dehnen (1999)

Minchev+(2009), Antoja+(2014), Monari+(2017)

Slow bar?

39 km/s/kpc

bulge-region data



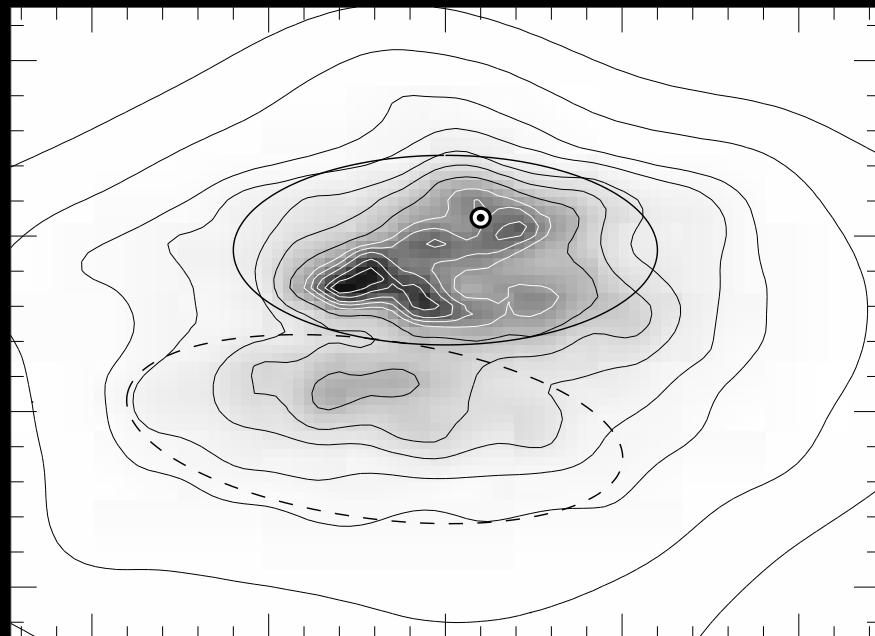
Portail et al. (2017)

Fast bar?

$$\Omega_{\text{bar}} =$$

53 km/s/kpc

local data



Slow bar?

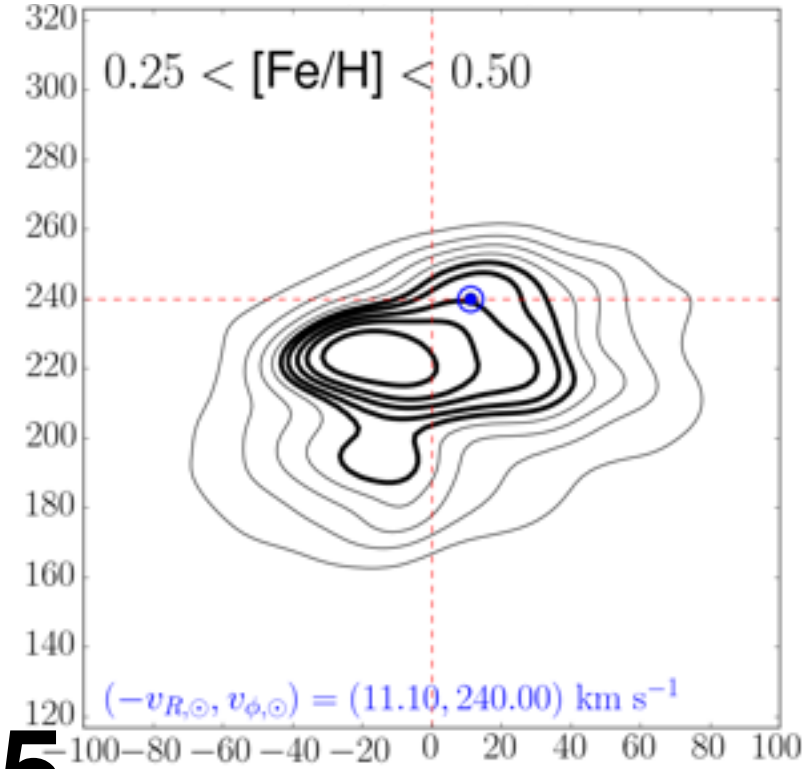
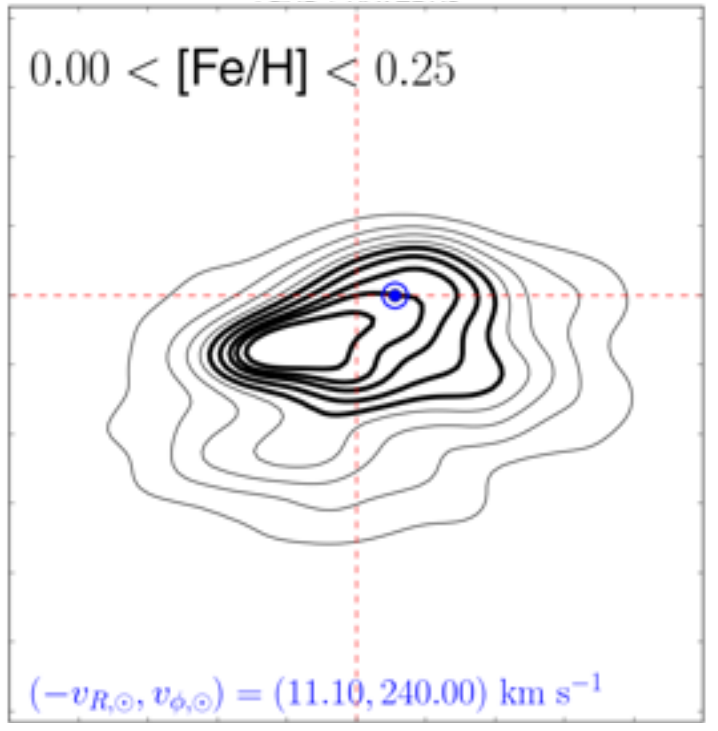
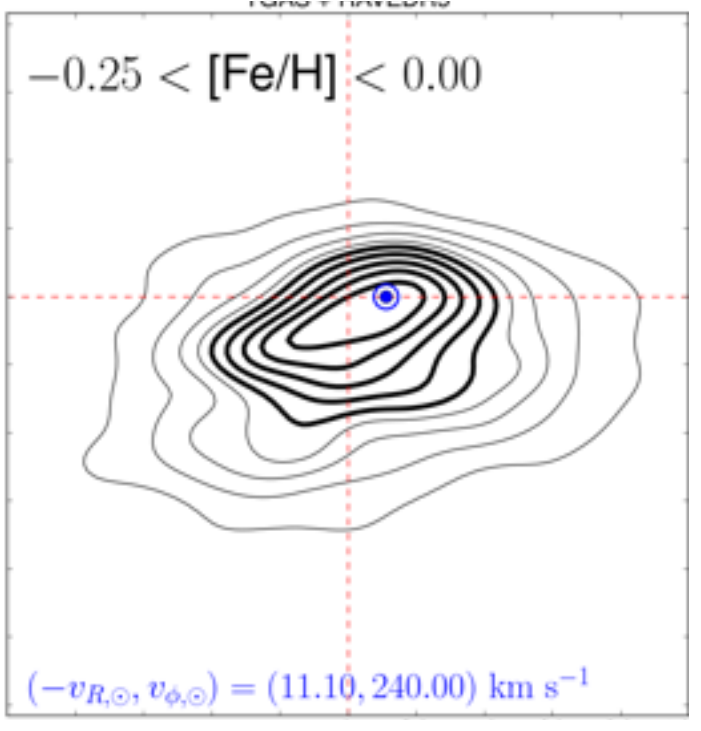
39 km/s/kpc

bulge-region data

**Hercules :
“slow bar + spirals” ?**

Similar idea : Antoja+(2009,2011)

**TGAS
+ RAVE**

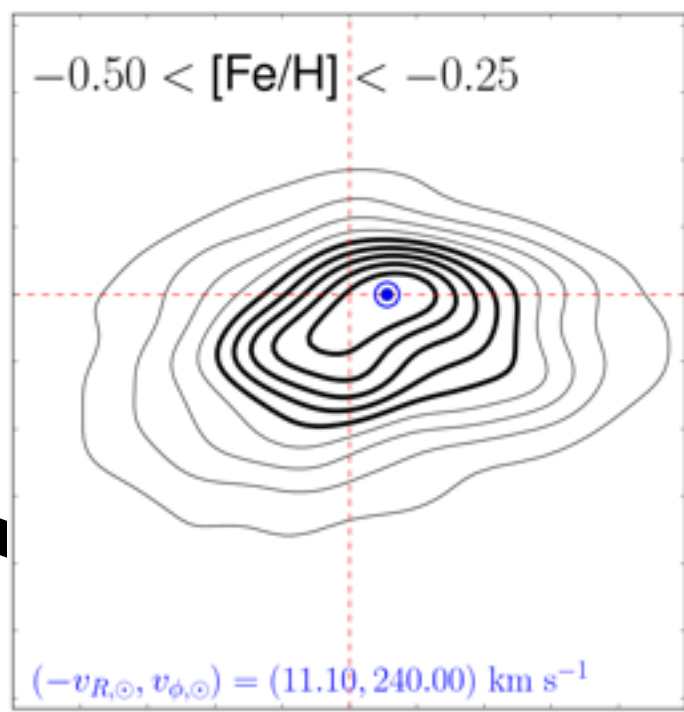
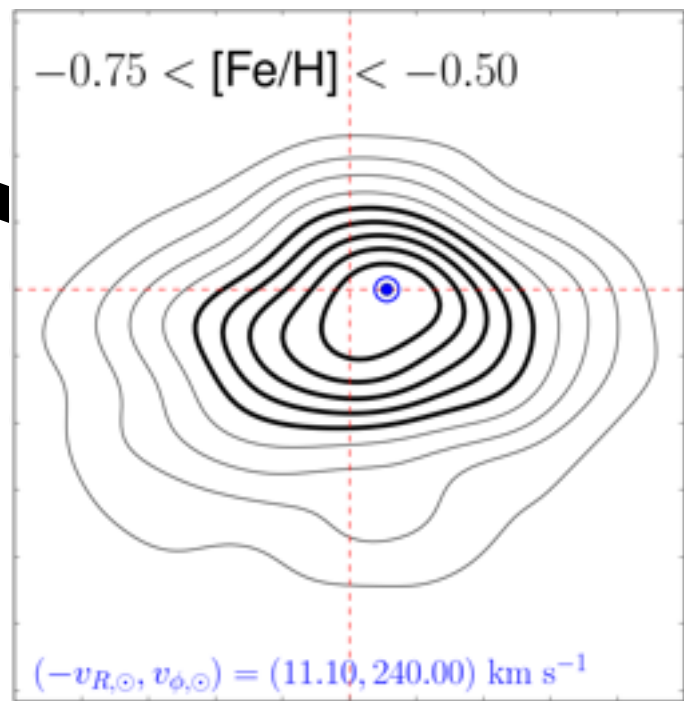
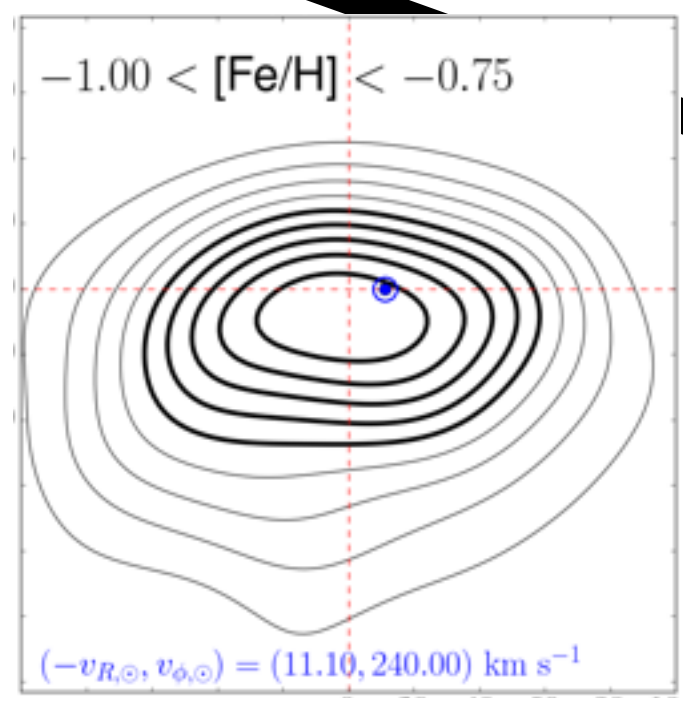


-0.25

0

0.25

[Fe/H]



Similar results :
Pérez-Villegas
+(2017)

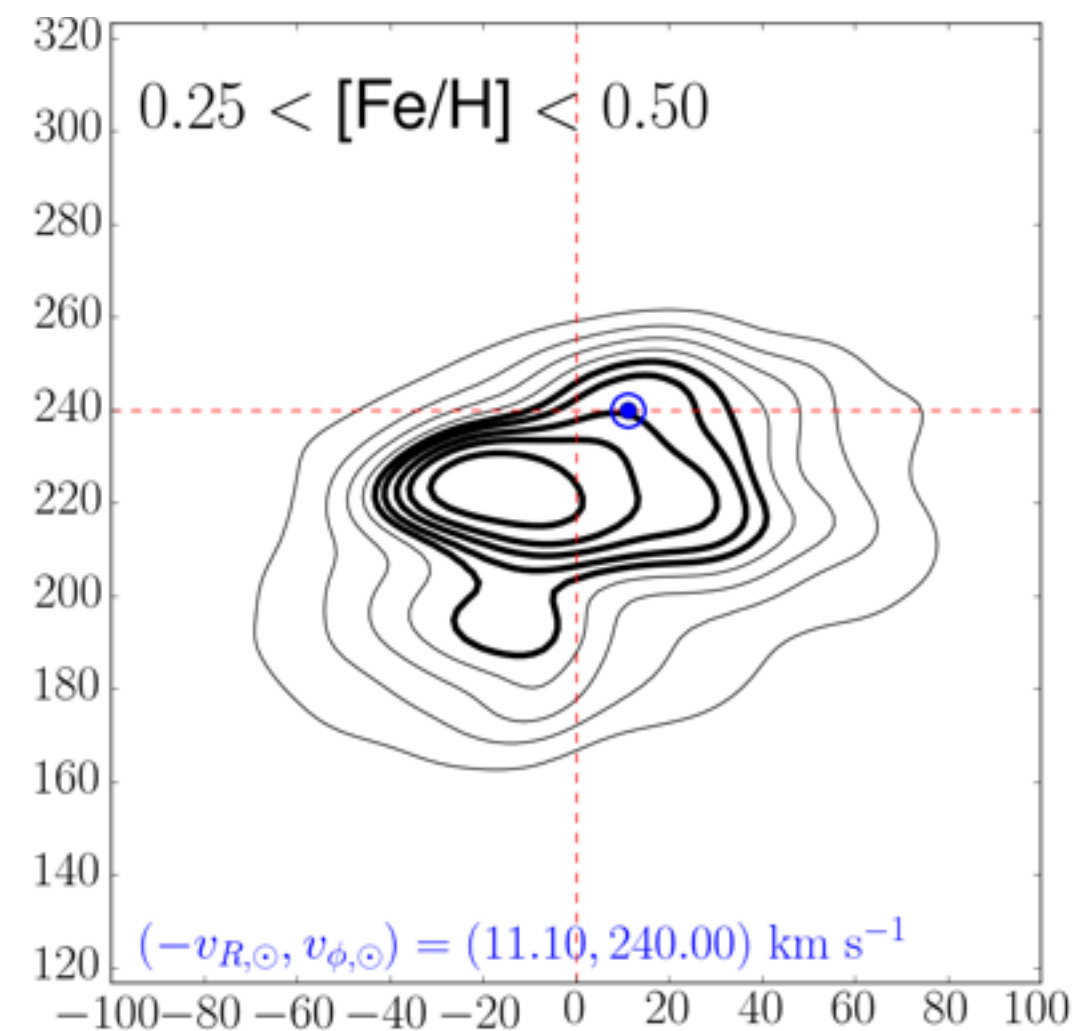
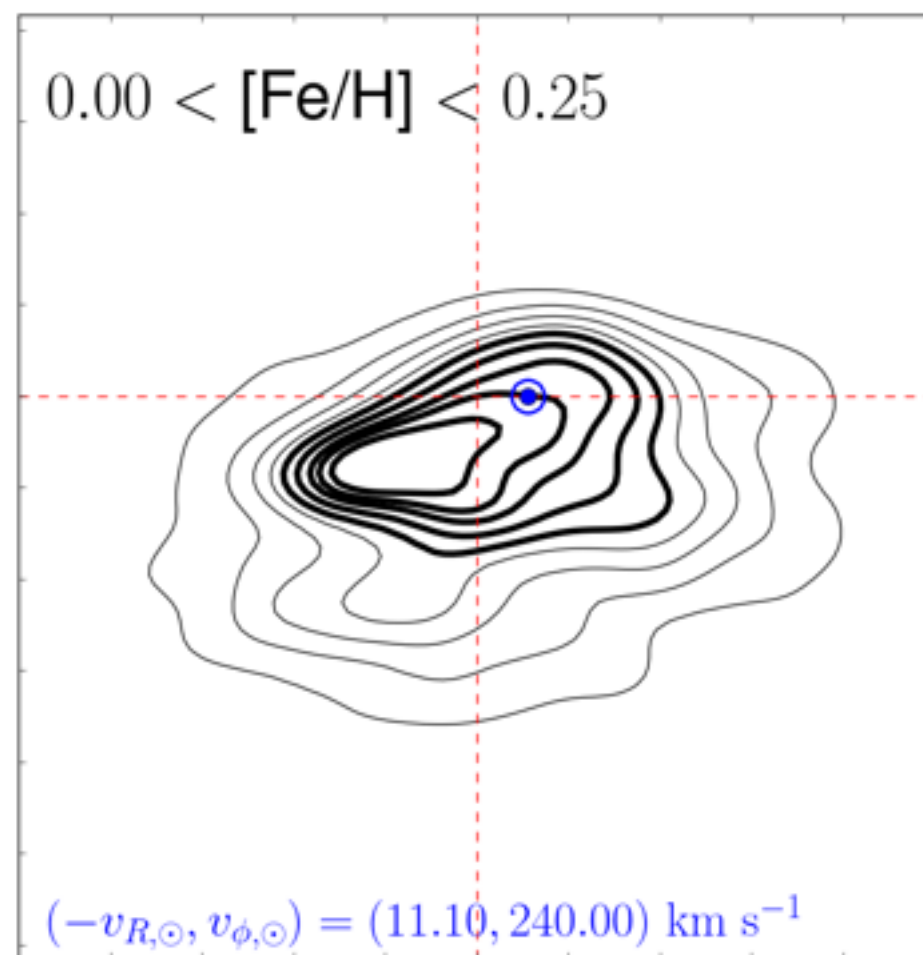
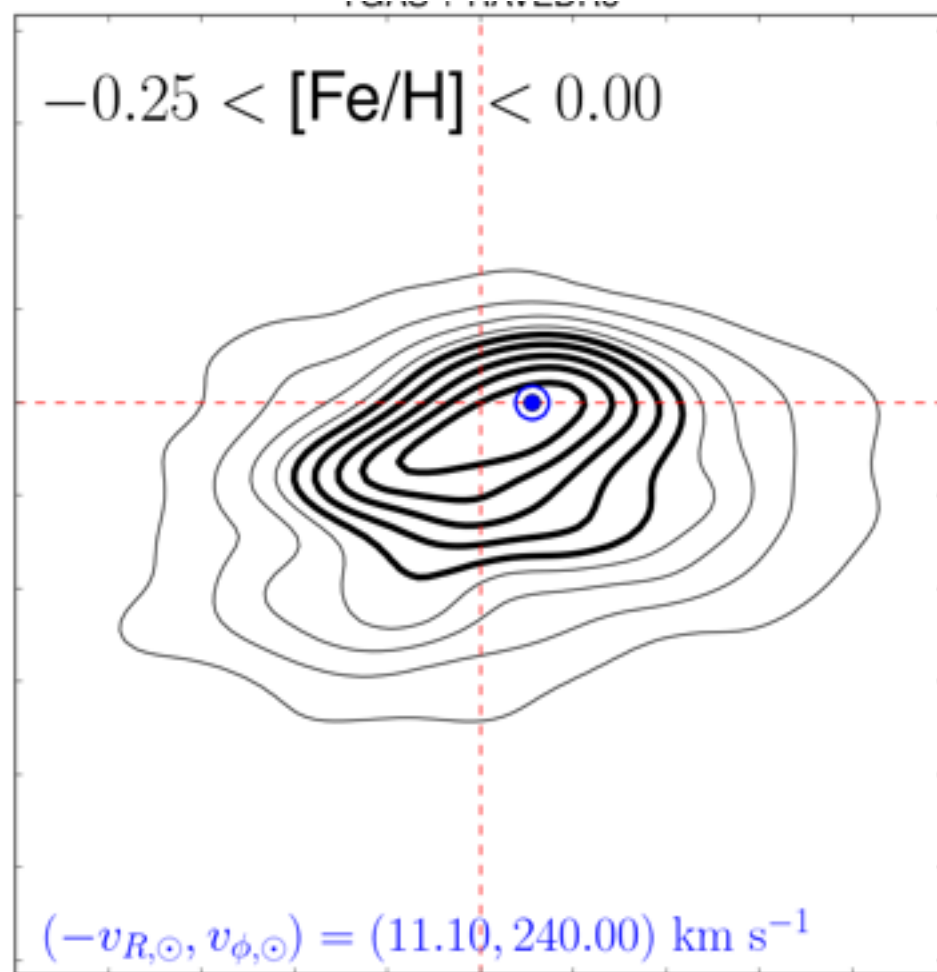
-1

-0.75

0.5

-0.25





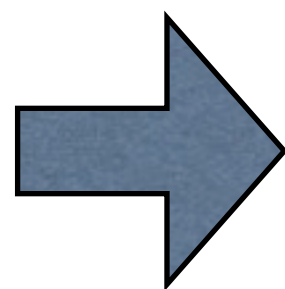
-0.25

0

0.25

[Fe/H]

(1) bar-only models
(2) bar+spiral models



[Fe/H]-dependence

Conclusion first !

Bar only

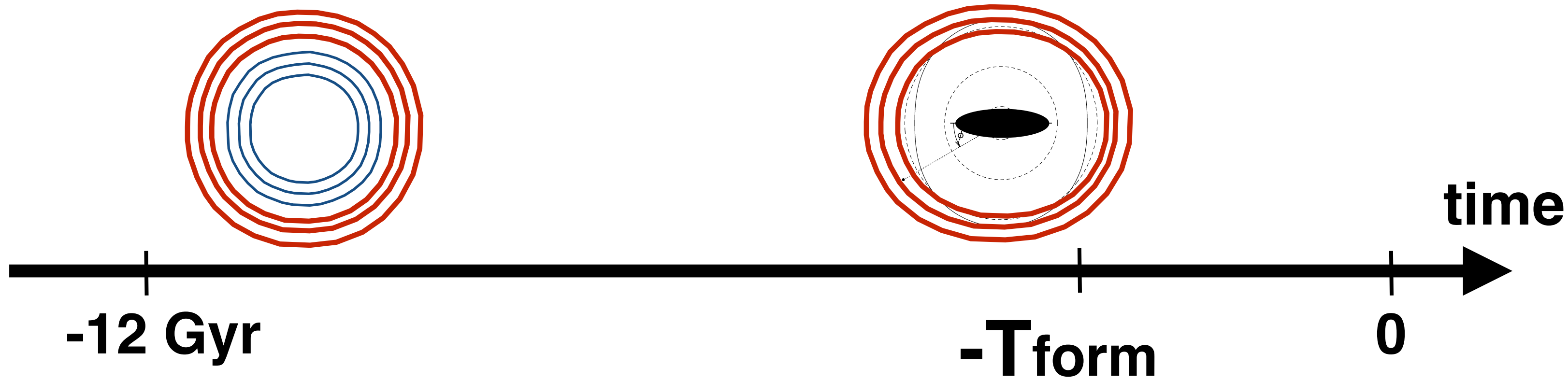
○ : Fast bar

✗ : Slow bar

Slow bar + spiral

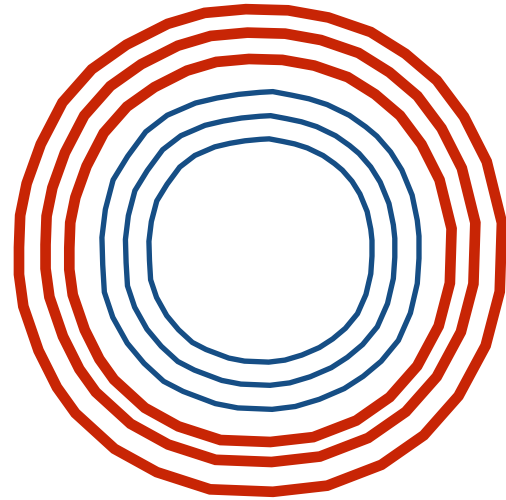
○ : slow bar + 4-armed **steady** spiral

○ : slow bar + 2-armed **transient** spiral



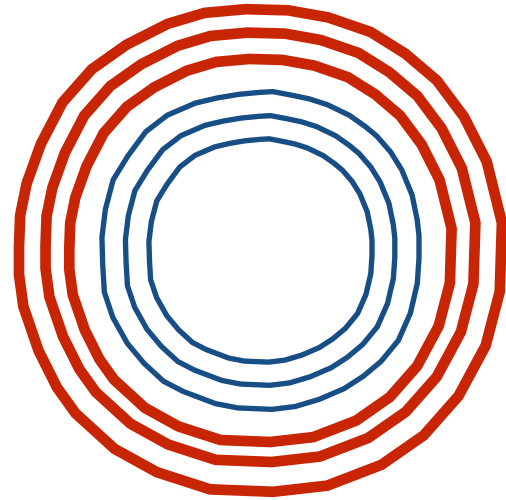
Method

axisymmetric

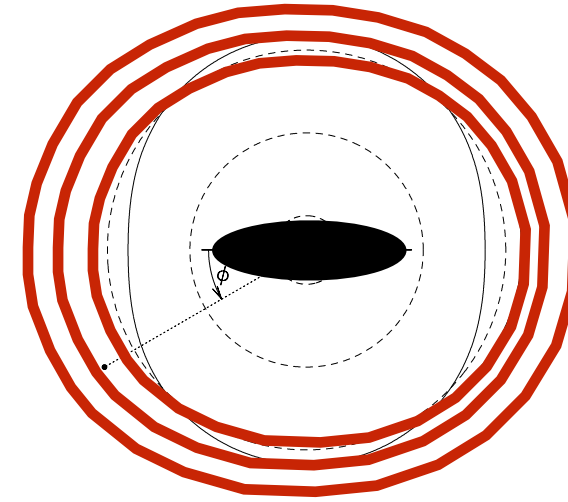


constant star formation

axisymmetric



bar formation



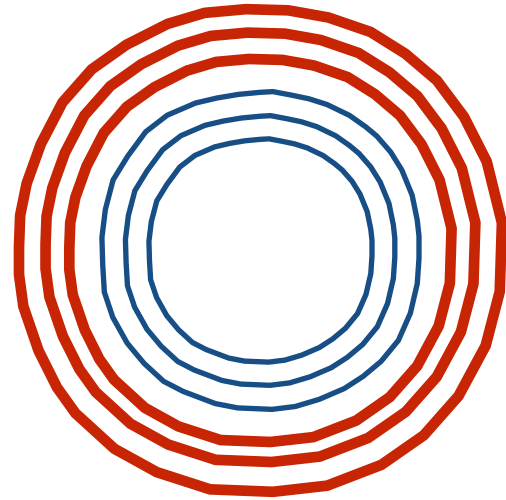
-12 Gyr

-T_{form}

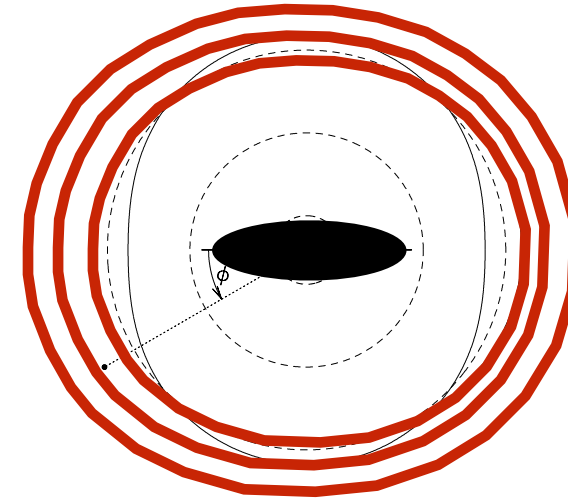
0

constant star formation

axisymmetric



bar formation



-12 Gyr

-T form

0

time

constant star formation

internal heating

**test particle
simulation**

Result

bar

shape

Dehnen (2000) bar

pattern
speed

Ω_b 39, 52 km/s/kpc

T_{form}

0.5 - 10 Gyr

$$\Omega_{\text{bar}} = 39 \pm 3.5 \text{ km/s/kpc}$$

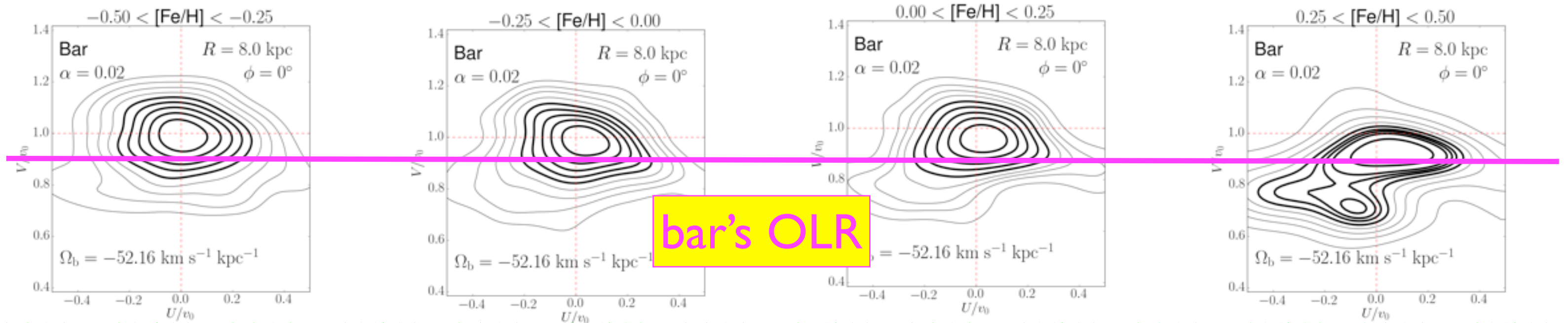
(Portail+2017)

$$\Omega_{\text{bar}} = 53 \pm 3 \text{ km/s/kpc}$$

(Dehnen 1999)

(1a) **fast** bar

$$\Omega_{\text{bar}} = 52, \quad T_{\text{form}} = 5 \text{ Gyr}$$



-0.5

-0.25

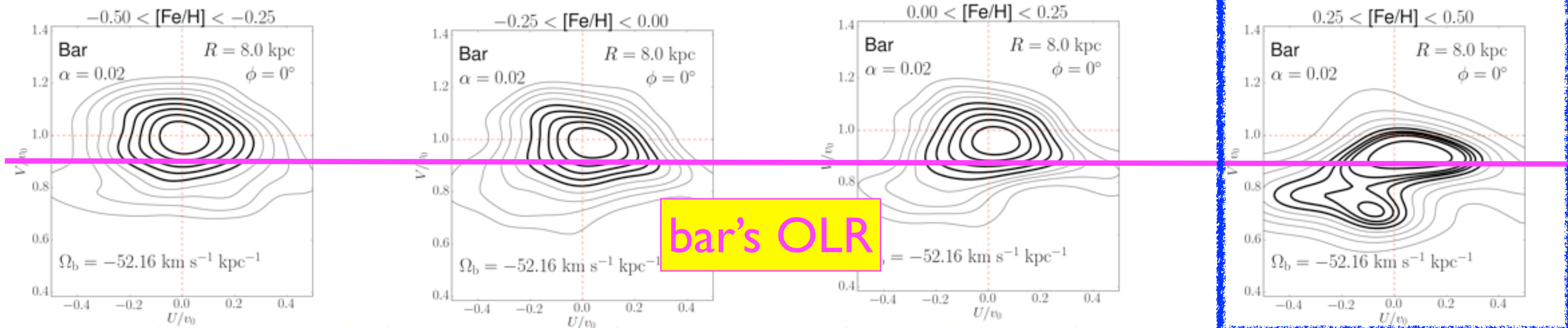
0

0.25

[Fe/H]

(1a) **fast** bar

$\Omega_{\text{bar}} = 52$, $T_{\text{form}} = 5$ Gyr



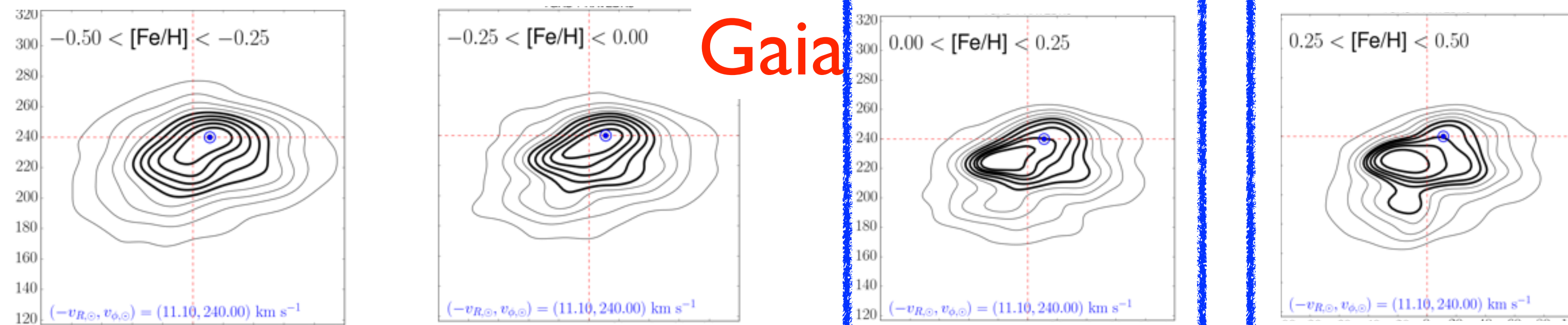
-0.5

-0.25

0

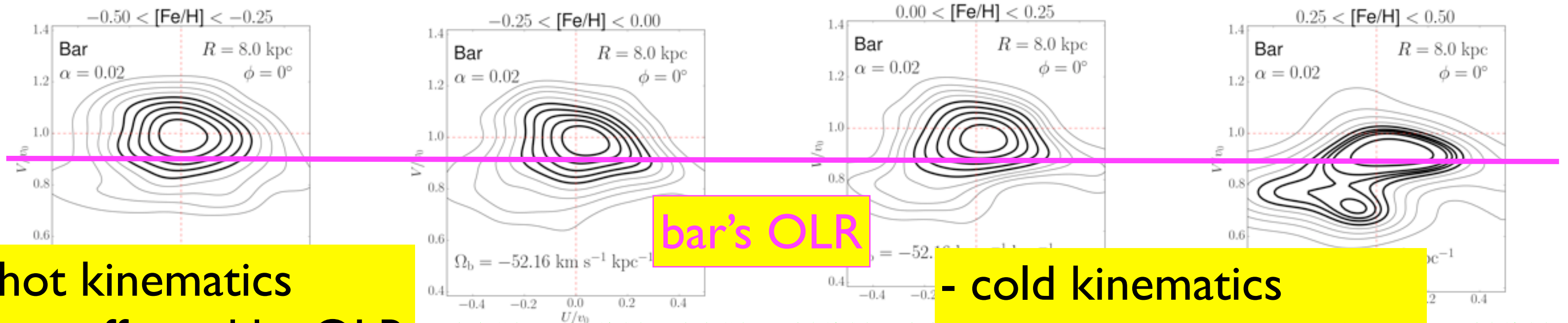
0.25

[Fe/H]



(1a) **fast** bar

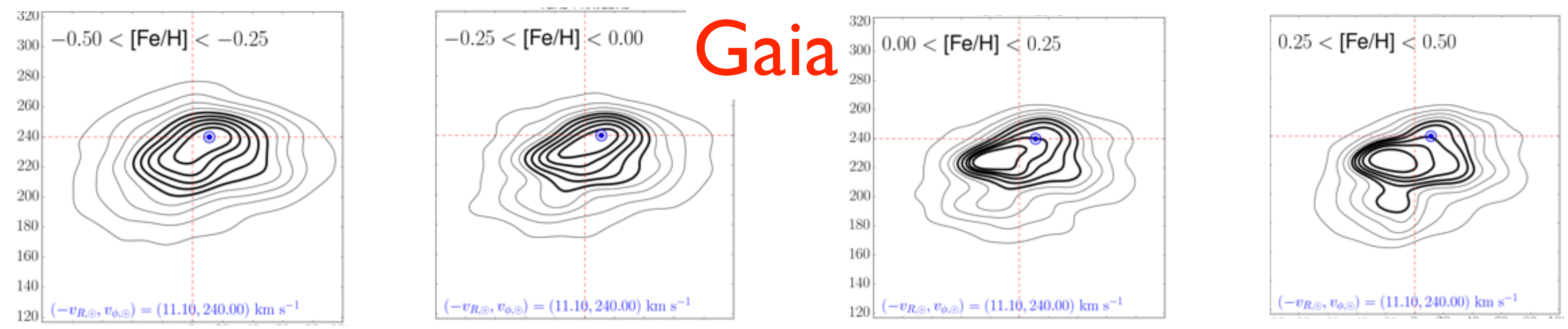
$$\Omega_{\text{bar}} = 52, \quad T_{\text{form}} = 5 \text{ Gyr}$$



- hot kinematics
- not affected by OLR

- cold kinematics
- easily affected by OLR

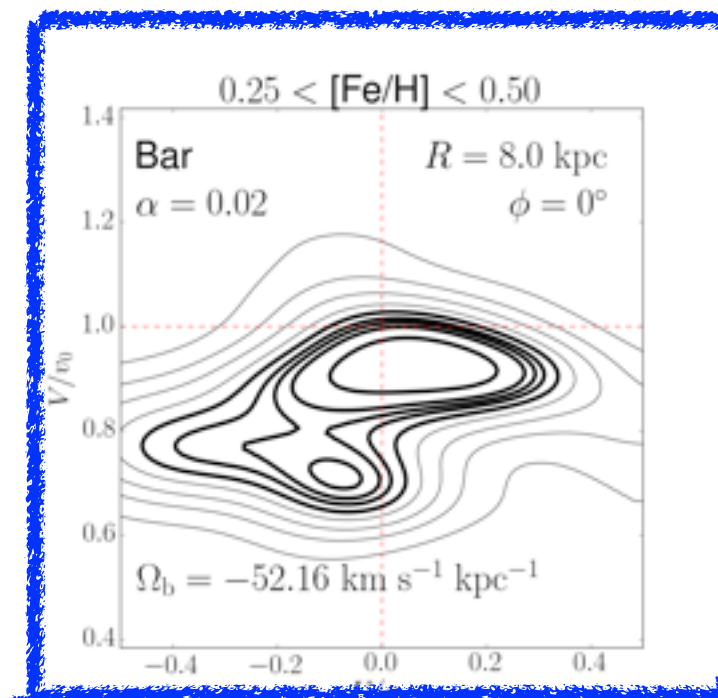
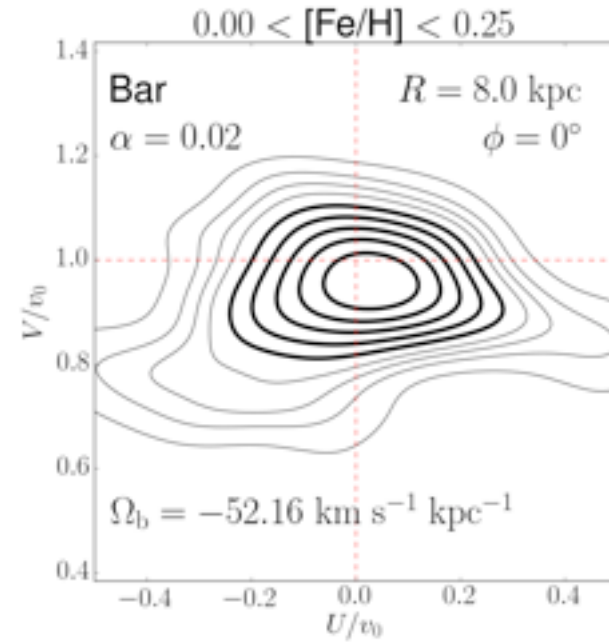
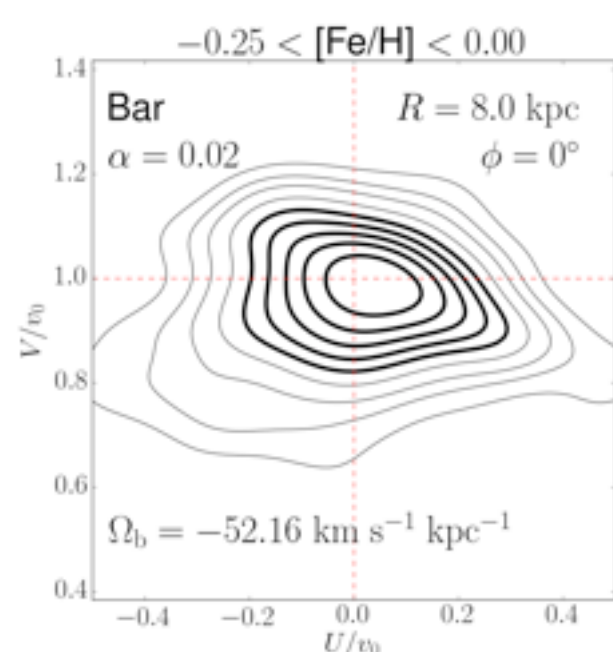
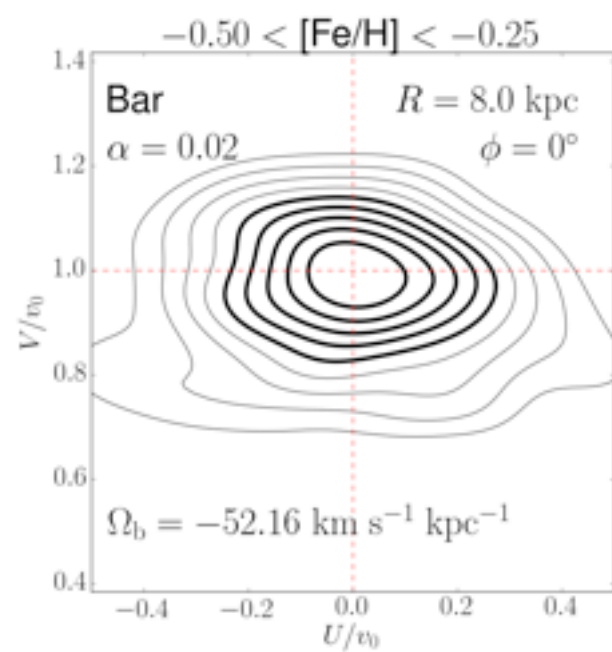
-0.5 -0.25 0 0.25 [Fe/H]



Gaia

(1a) fast bar

$\Omega_{\text{bar}} = 52, T_{\text{form}} = 5 \text{ Gyr}$



-0.5

-0.25

0

0.25

[Fe/H]

$T_{\text{form}} = 2 \text{ Gyr}$

O

5 Gyr

O

7 Gyr

X

9 Gyr

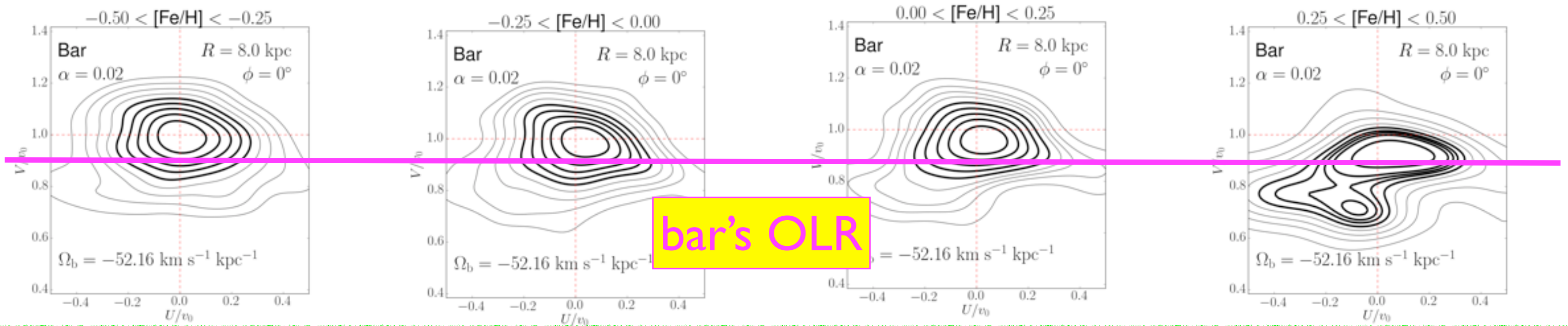
O

bar's OLR

Similar results : Monari et al. (2013)

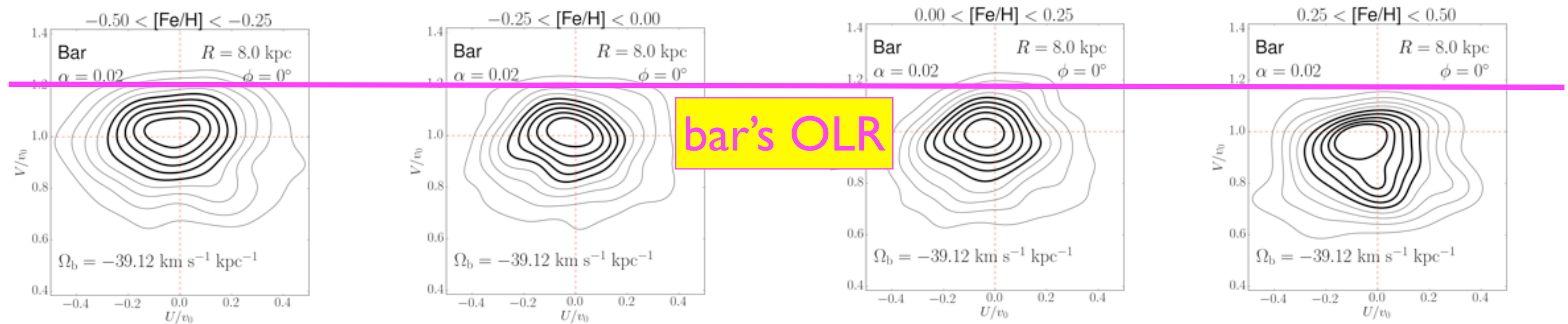
(1a) **fast** bar

$$\Omega_{\text{bar}} = 52, \quad T_{\text{form}} = 5 \text{ Gyr}$$



(1b) **slow** bar

$$\Omega_{\text{bar}} = 39, \quad T_{\text{form}} = 5 \text{ Gyr}$$



-0.5

-0.25

0

0.25

[Fe/H]

Conclusion first !

Bar only

○ : Fast bar

Naturally explains [Fe/H]-dependence of Hercules stream.

✗ : Slow bar

No Bimodal structure.

Slow bar + spiral

○ : slow bar + 4-armed **steady** spiral

○ : slow bar + 2-armed **transient** spiral

Conclusion first !

Bar only

○ : Fast bar

Naturally explains [Fe/H]-dependence of Hercules stream.

✗ : Slow bar

No Bimodal structure.

Slow bar + spiral

○ : slow bar + 4-armed **steady** spiral

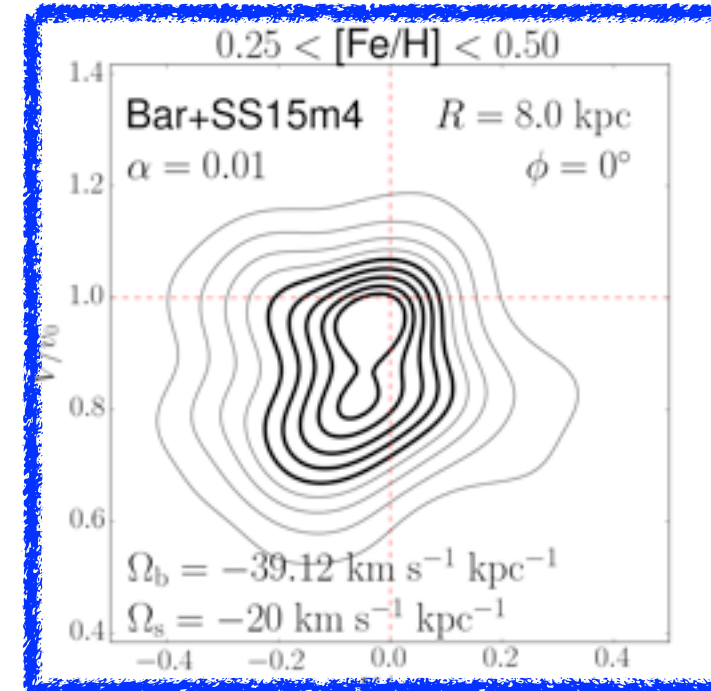
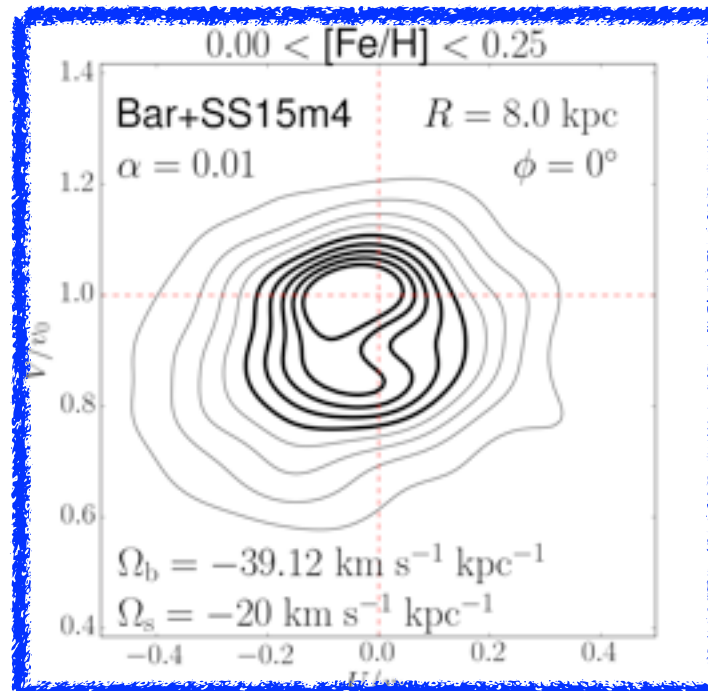
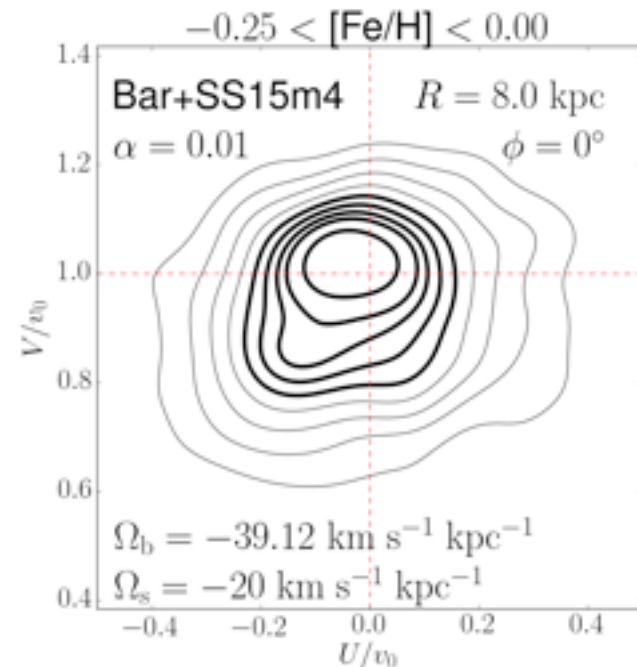
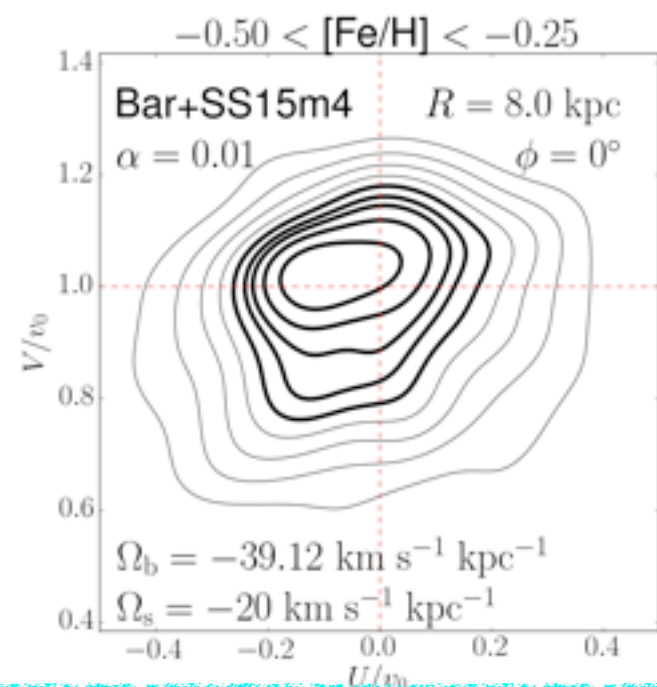
○ : slow bar + 2-armed **transient** spiral

(2) slow bar + steady spiral (m=4)

$$\Omega_{\text{bar}} = 39,$$

$$\Omega_s = 20,$$

$$T_{\text{form}} = 8 \text{ Gyr}$$



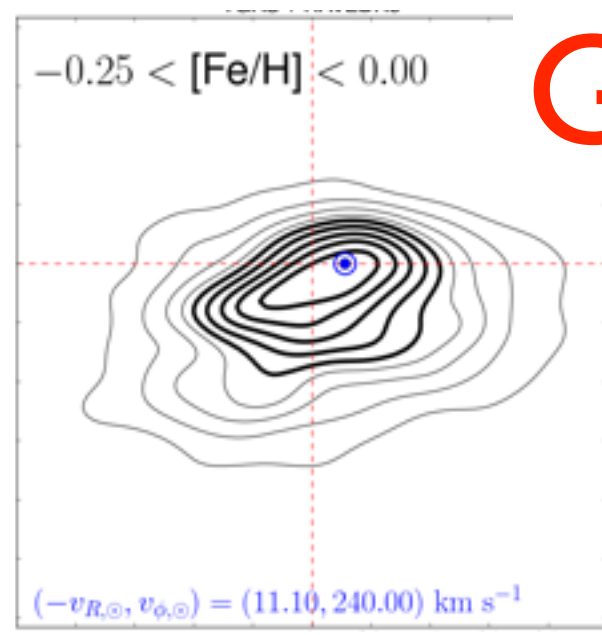
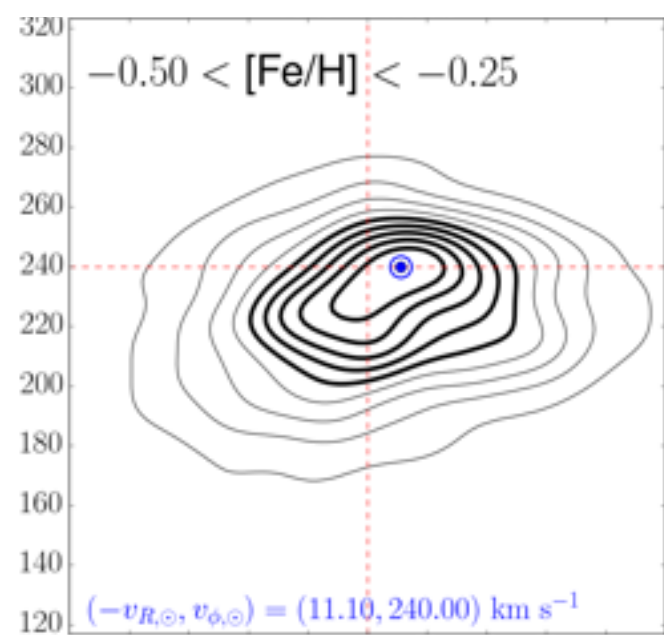
-0.5

-0.25

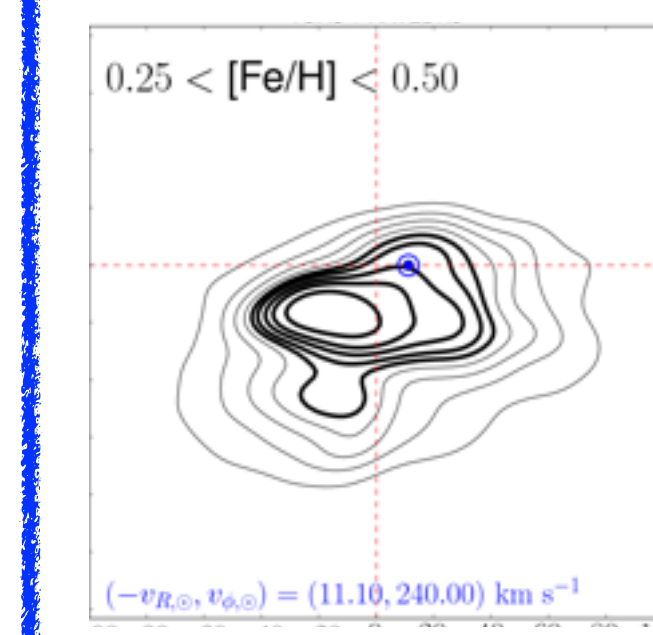
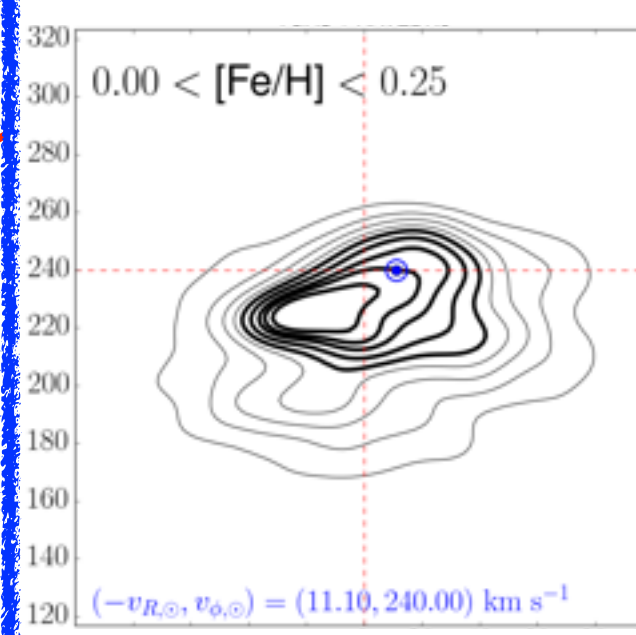
0

0.25

[Fe/H]



Gaia

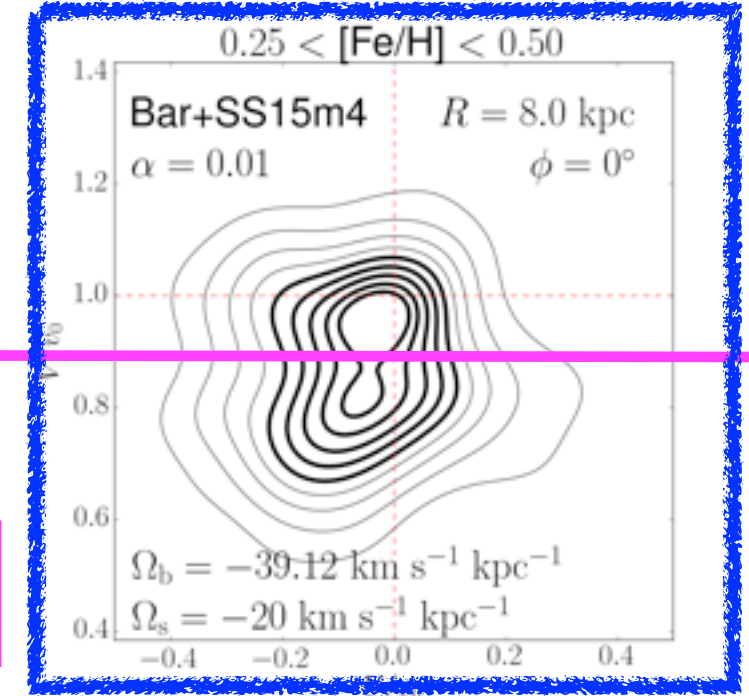
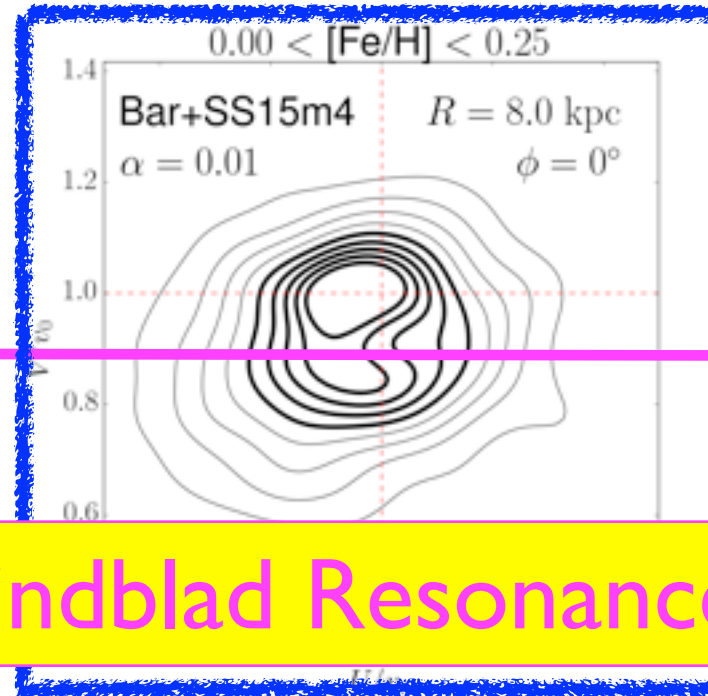
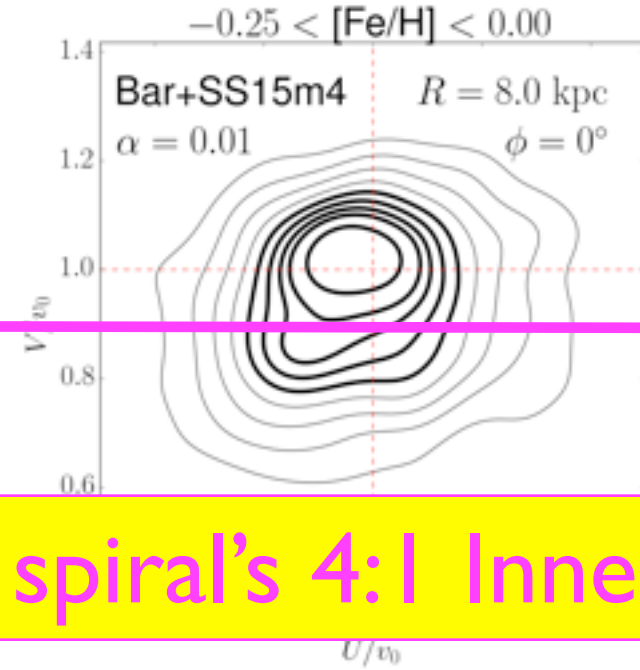
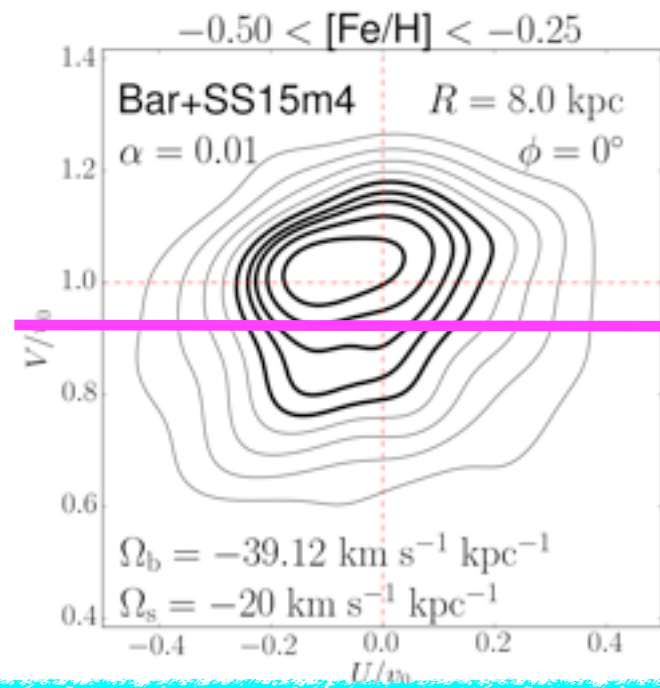


(2) slow bar + steady spiral (m=4)

$$\Omega_{\text{bar}} = 39,$$

$$\Omega_s = 20,$$

$$T_{\text{form}} = 8 \text{ Gyr}$$



spiral's 4:1 Inner Lindblad Resonance

-0.5

-0.25

0

0.25

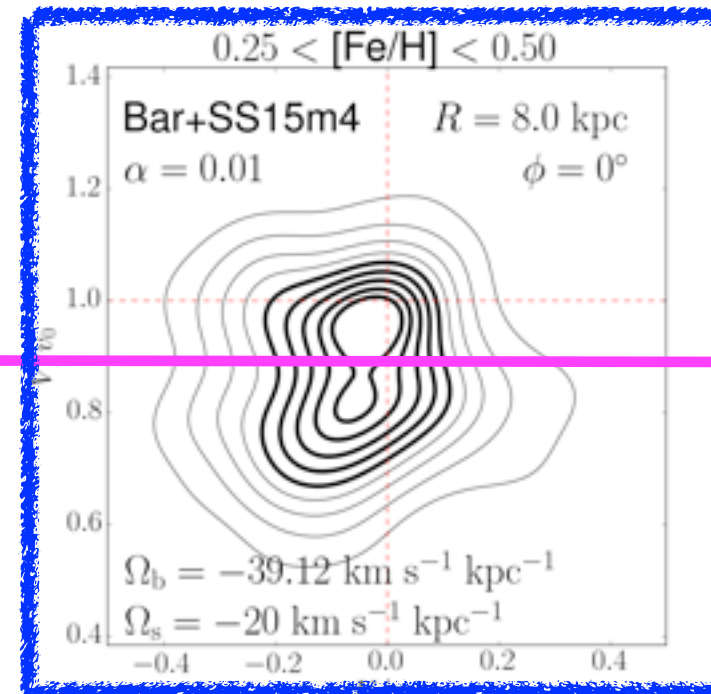
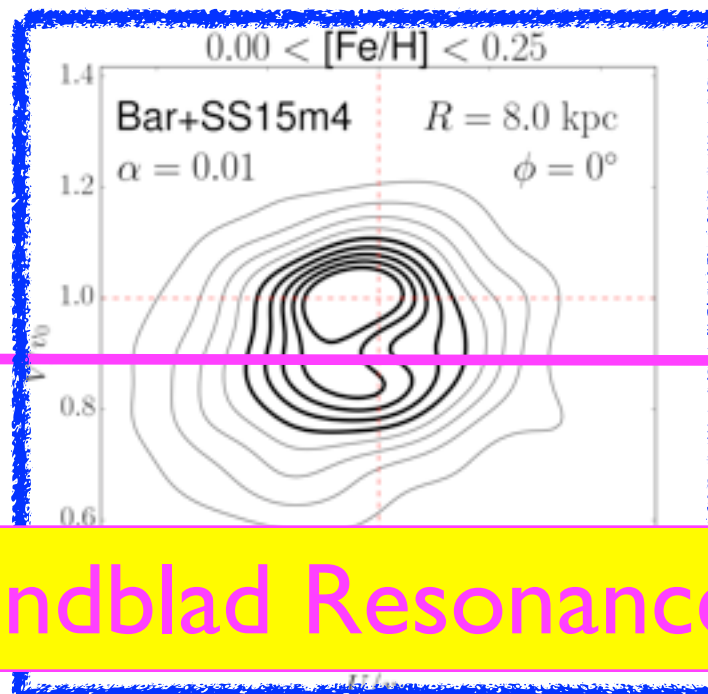
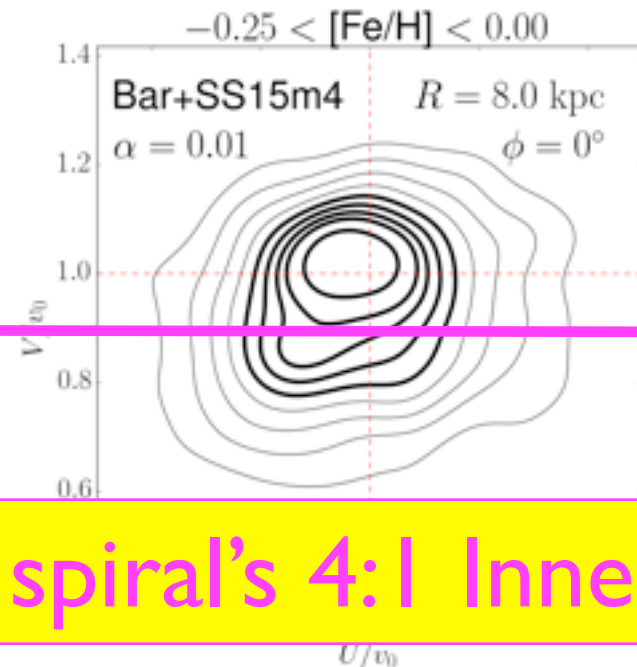
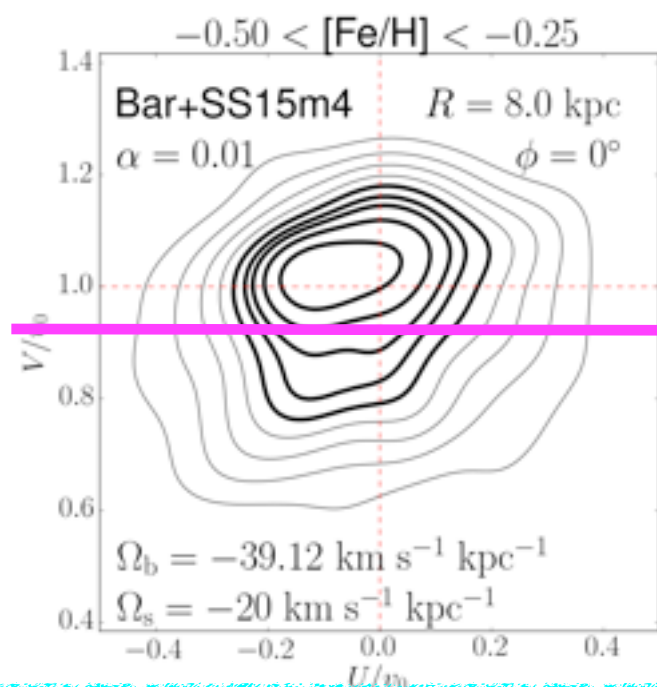
[Fe/H]

(2) slow bar + steady spiral (m=4)

$$\Omega_{\text{bar}} = 39,$$

$$\Omega_s = 20,$$

$$T_{\text{form}} = 8 \text{ Gyr}$$



spiral's 4:1 Inner Lindblad Resonance

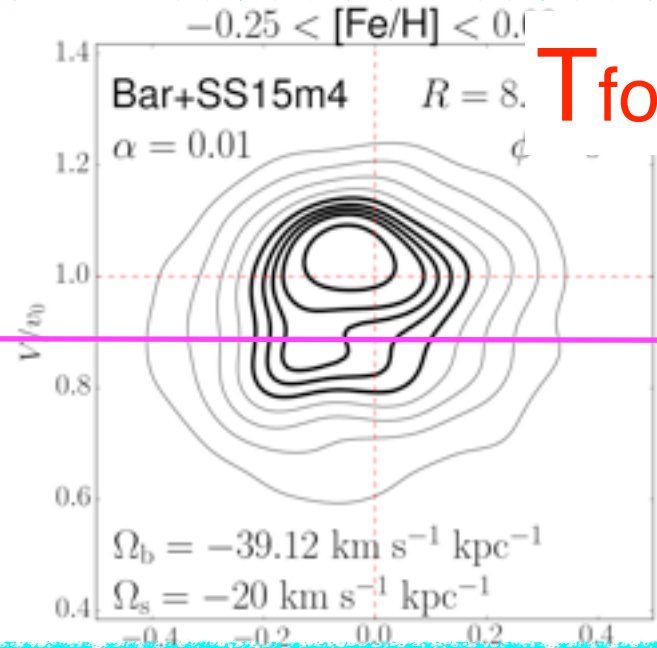
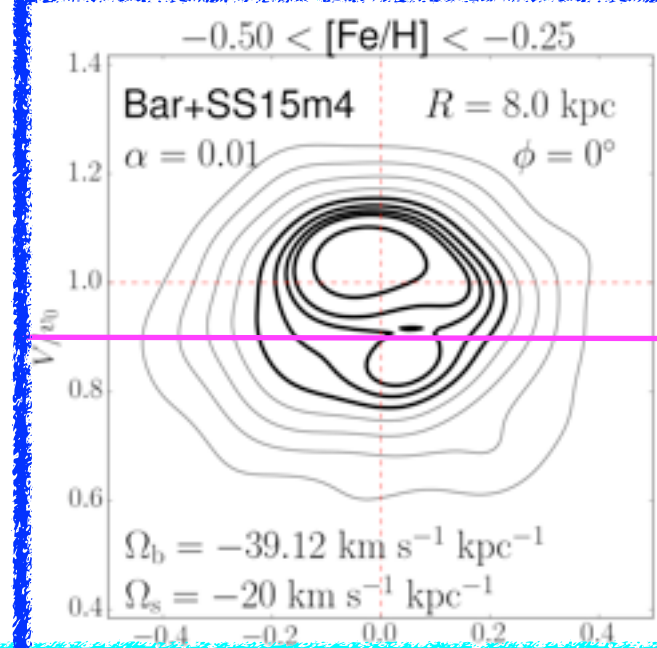
-0.5

-0.25

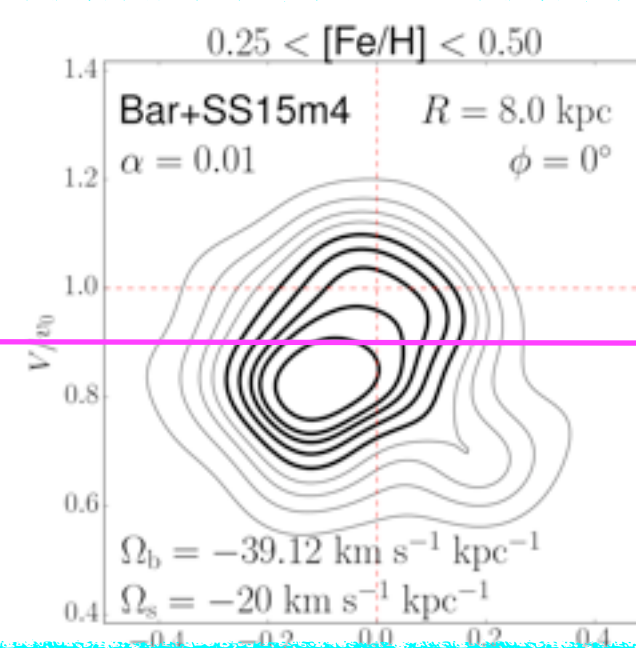
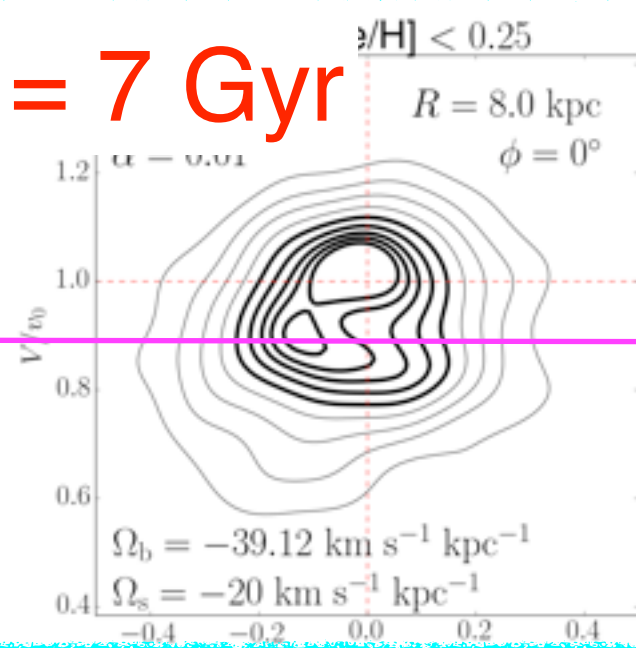
0

0.25

[Fe/H]



$$T_{\text{form}} = 7 \text{ Gyr}$$

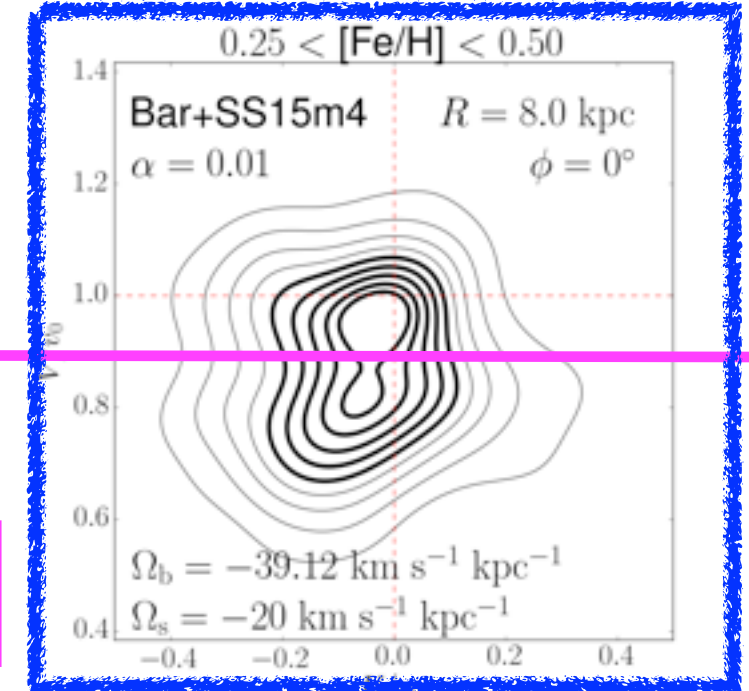
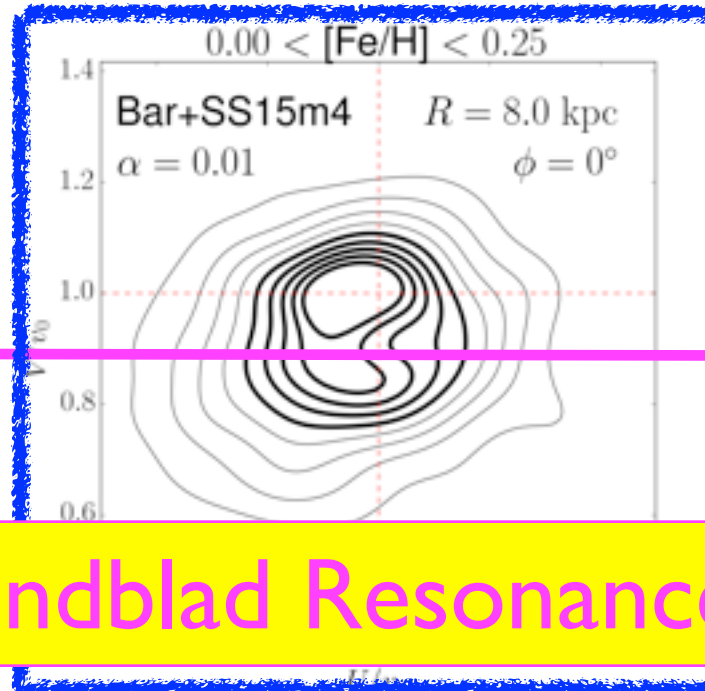
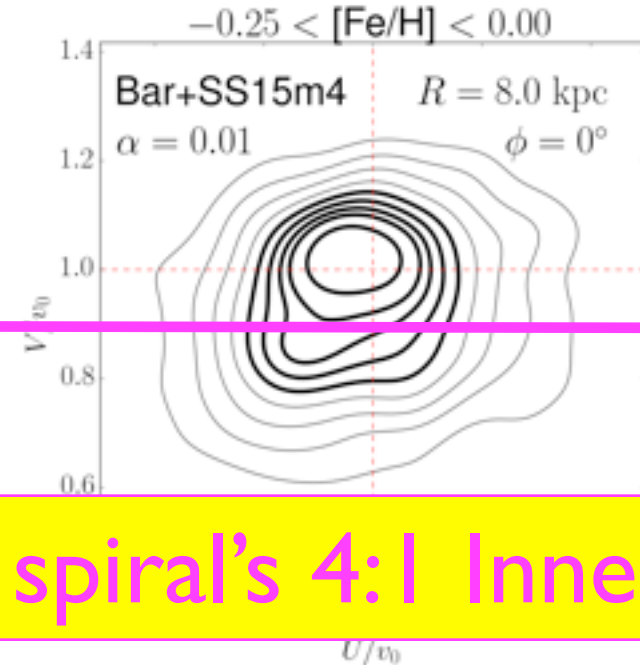
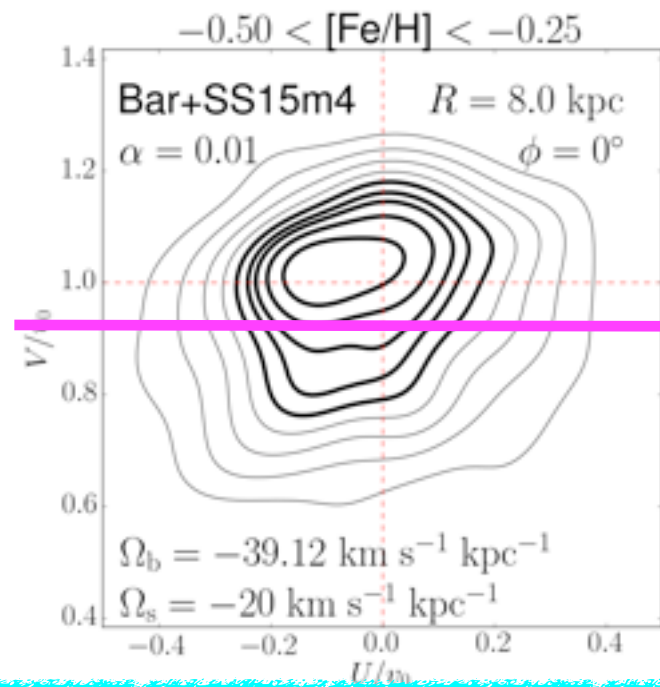


(2) slow bar + steady spiral (m=4)

$$\Omega_{\text{bar}} = 39,$$

$$\Omega_s = 20,$$

$$T_{\text{form}} = 8 \text{ Gyr}$$



spiral's 4:1 Inner Lindblad Resonance



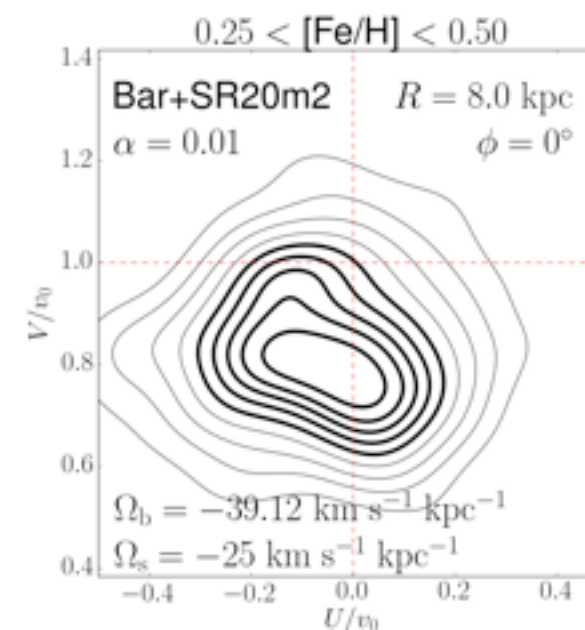
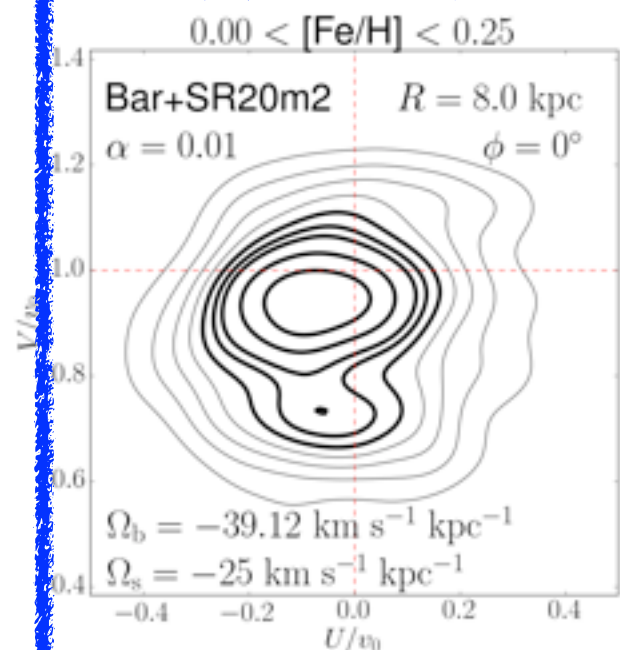
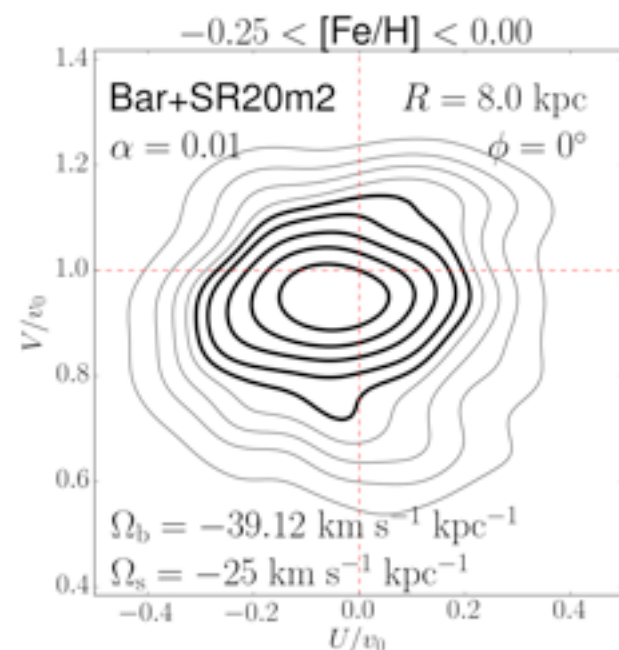
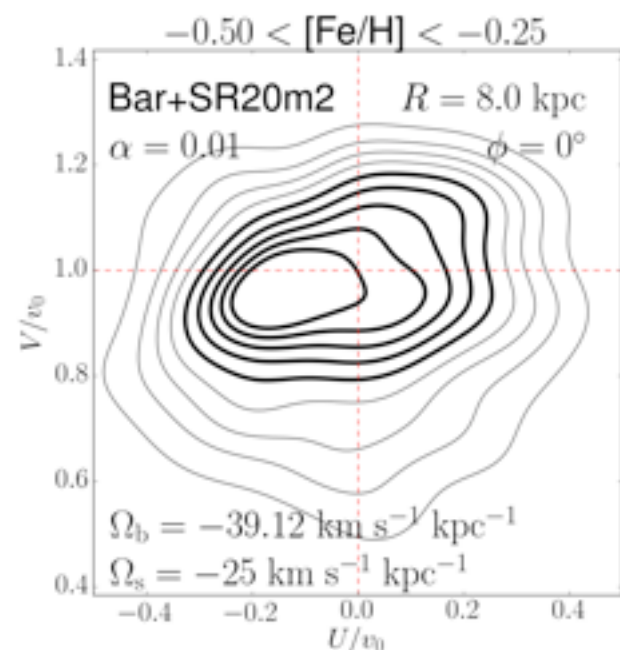
- Bimodality is due to spiral.
- $[\text{Fe}/\text{H}]$ -dependence is sensitive to T_{form} (due to chaotic orbits)
→ Observed $[\text{Fe}/\text{H}]$ -dependence is not informative.

(3) bar + transient spiral (m=2, lifetime = 100Myr)

$$\Omega_{\text{bar}} = 39,$$

$$\Omega_s = 25,$$

$$T_{\text{form}} = 8 \text{ Gyr}$$



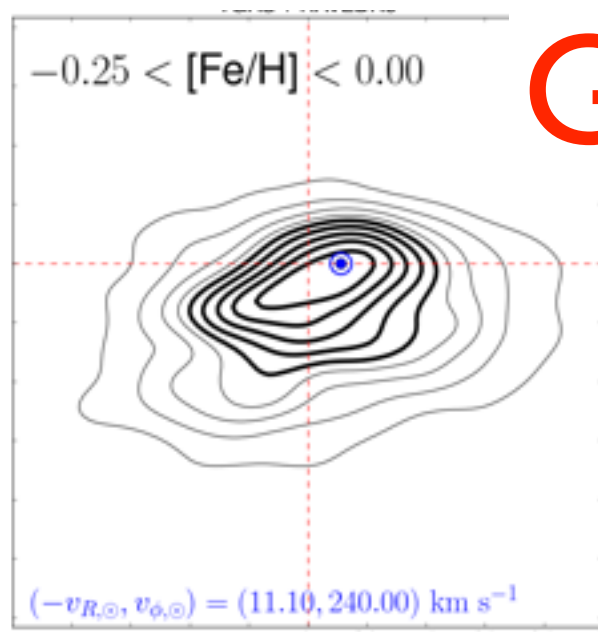
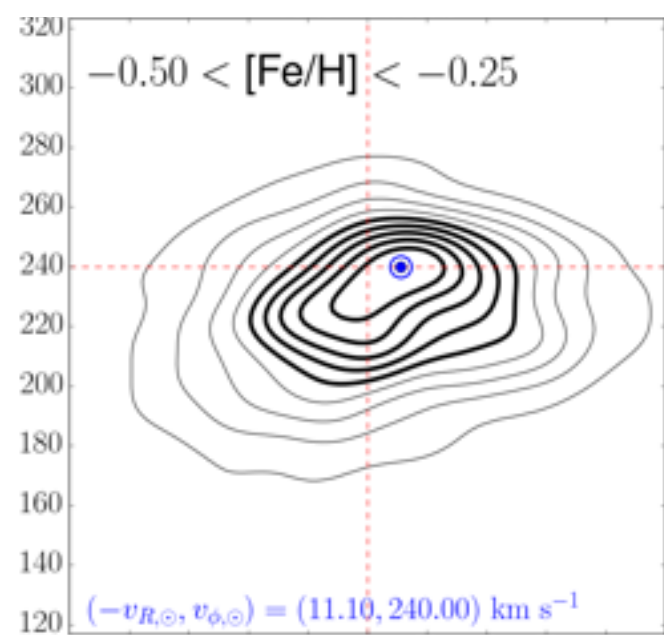
-0.5

-0.25

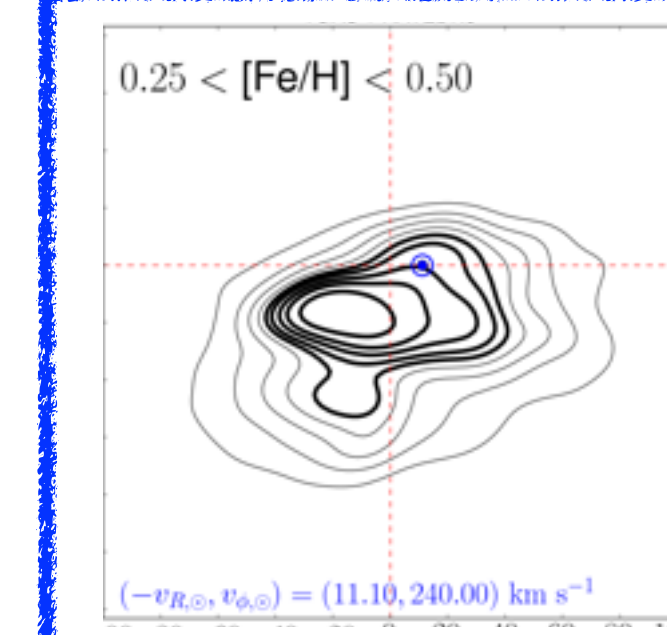
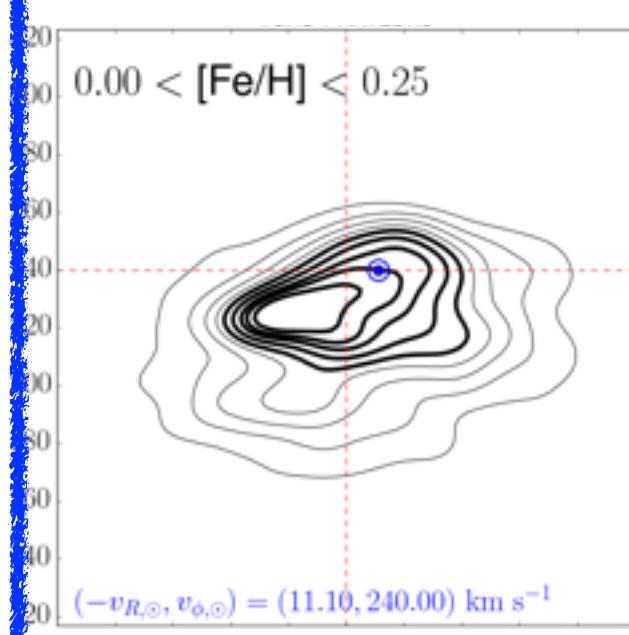
0

0.25

[Fe/H]

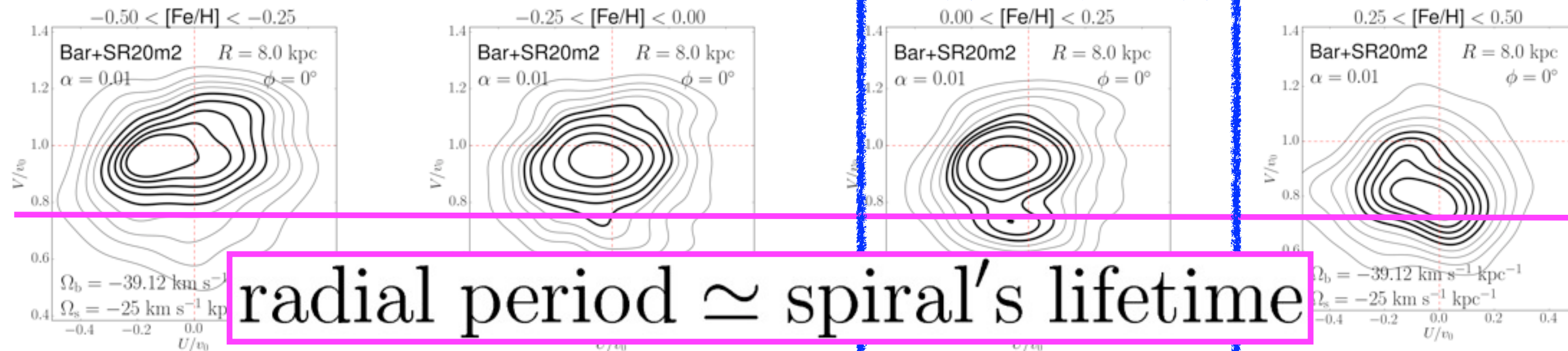


Gaia

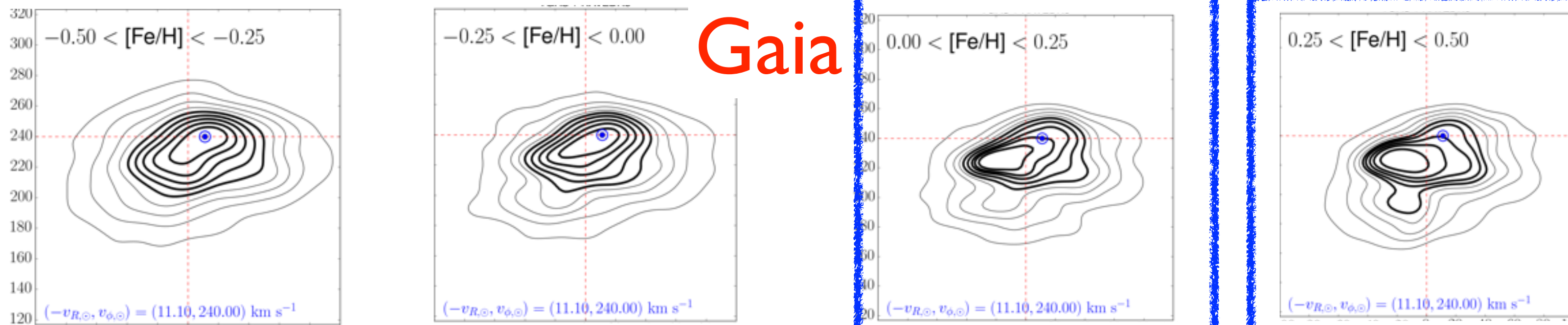


(3) bar + transient spiral (m=2, lifetime = 100Myr)

$\Omega_{\text{bar}} = 39,$ $\Omega_s = 25,$ $T_{\text{form}} = 8 \text{ Gyr}$



-0.5 -0.25 0 0.25 [Fe/H]

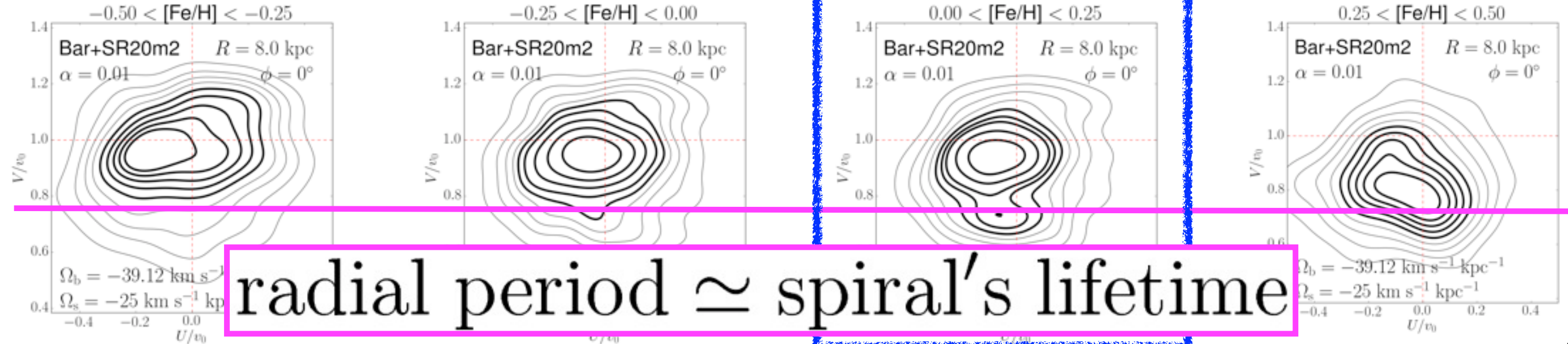


(3) bar + transient spiral (m=2, lifetime = 100Myr)

$$\Omega_{\text{bar}} = 39,$$

$$\Omega_s = 25,$$

$$T_{\text{form}} = 8 \text{ Gyr}$$



radial period \simeq spiral's lifetime

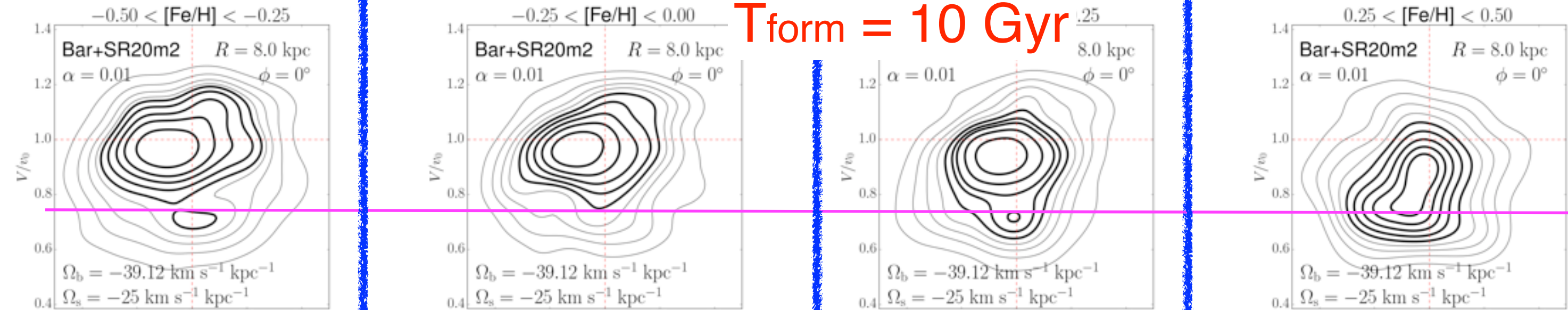
-0.5

-0.25

0

0.25

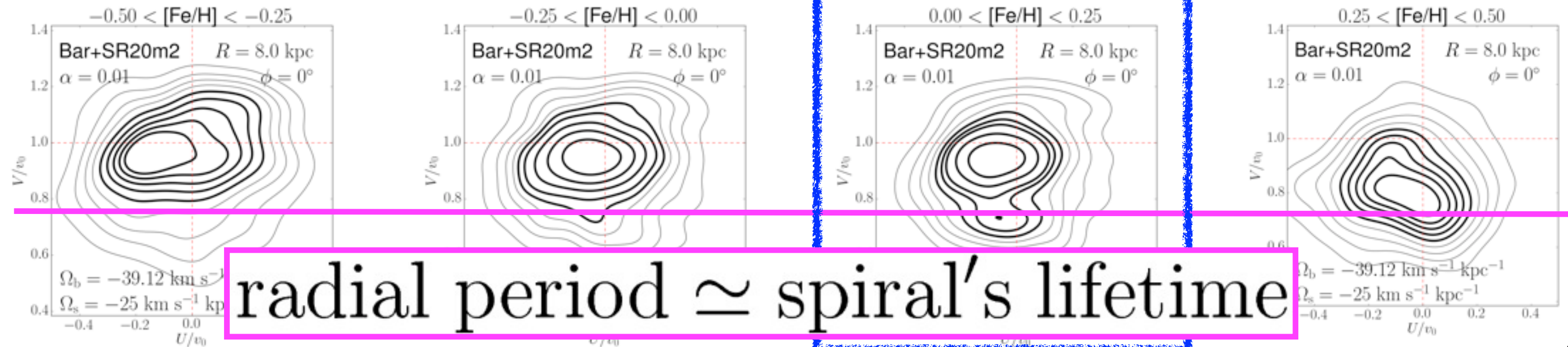
[Fe/H]



$$T_{\text{form}} = 10 \text{ Gyr}$$

(3) bar + transient spiral ($m=2$, lifetime = 100Myr)

$$\Omega_{\text{bar}} = 39, \quad \Omega_s = 25, \quad T_{\text{form}} = 8 \text{ Gyr}$$



radial period \simeq spiral's lifetime

-0.5 -0.25 0 0.25 [Fe/H]

- Bimodality is due to **spiral's lifetime**.
- [Fe/H]-dependence is sensitive to **Tform** (due to **chaotic orbits**)
→ **Observed [Fe/H]-dependence is not informative.**

TGAS+RAVE : [Fe/H]-dependence of Hercules

Conclusion

Bar only

○ : Fast bar

Naturally explains [Fe/H]-dependence of Hercules.

✗ : Slow bar

No Bimodal structure.

Slow bar + spiral

○ : slow bar + **steady** spiral

Bimodality : spiral's inner Lindblad resonance.

○ : slow bar + **transient** spiral

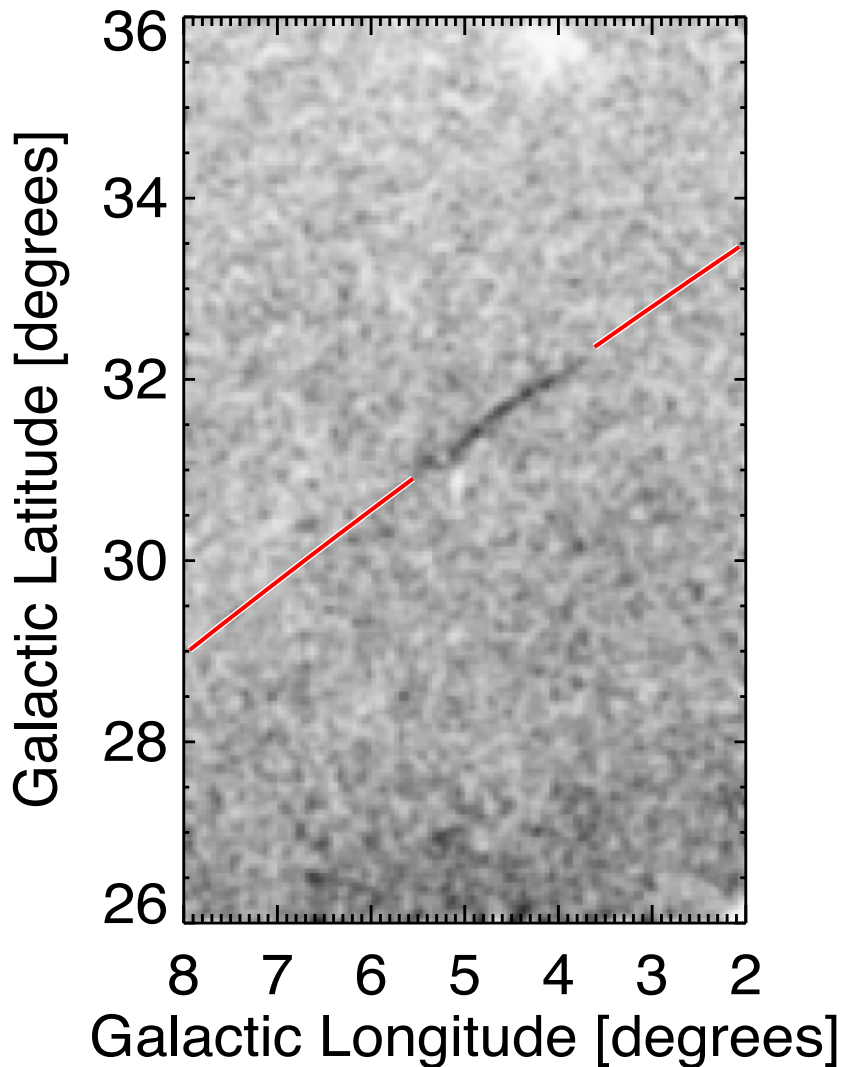
Bimodality : due to spiral's lifetime.

} [Fe/H]-dependence is
NOT informative
(**chaotic orbits**).

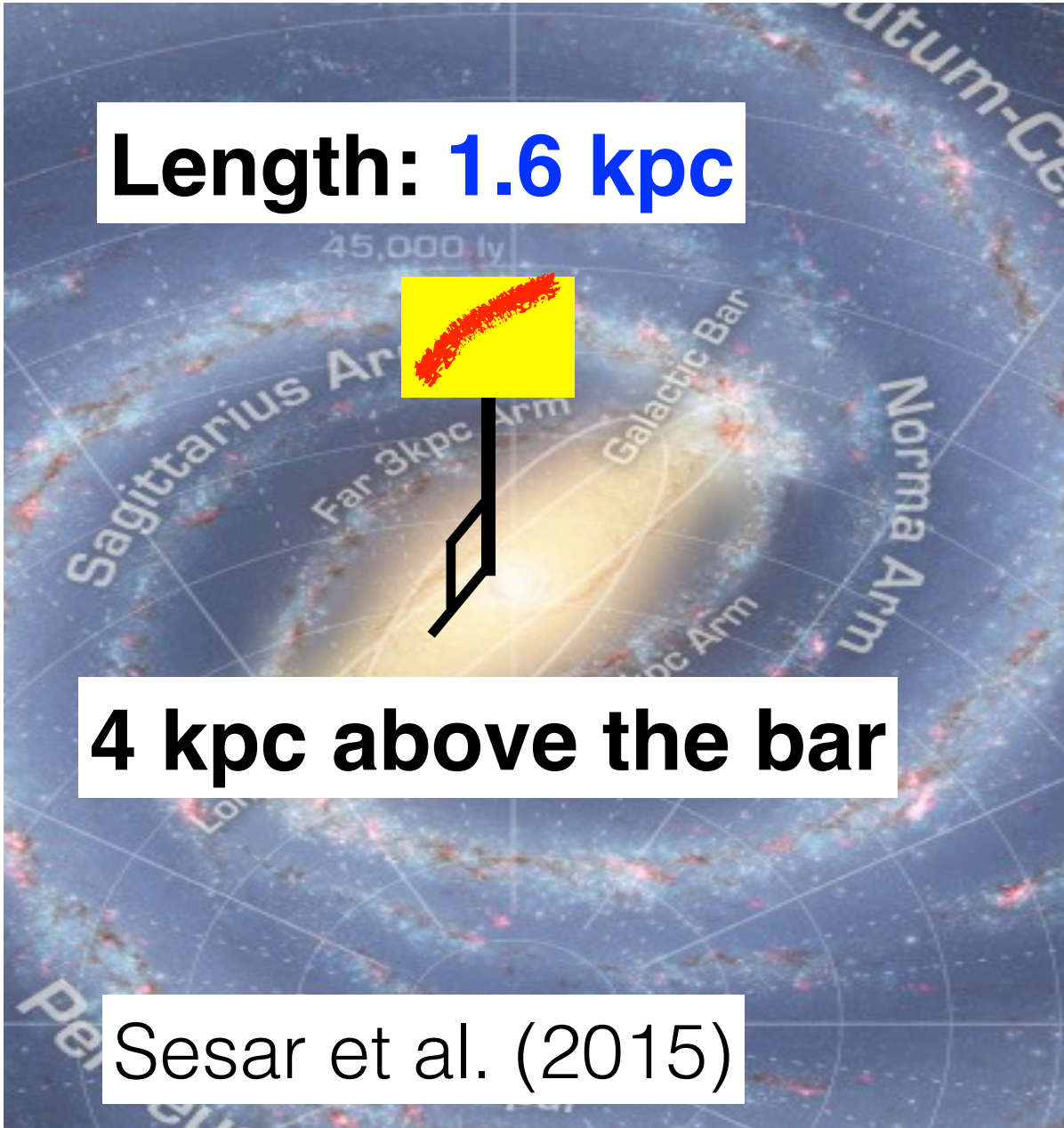
Independent measurement for Ω_{bar}

Hattori, Erkal, Sanders (2016)

Ophiuchus stream



Bernard et al. (2014)



Sesar et al. (2015)

