

The vertical force in the solar neighbourhood

Jorrit Hagen & Amina Helmi

Friday 28 April 2017
IAUS 330, Nice



university of
 groningen

faculty of science
 and engineering

kapteyn astronomical
 institute



credit: NASA, ESA, and T. Brown and J. Tumlinson (STScI)



The force-equation

- We explore the vertical force-equation:

$$-\frac{d\Phi}{dz} \equiv F_z = \frac{\sigma_z^2}{\nu} \frac{d\nu}{dz} + \frac{d\sigma_z^2}{dz} + \frac{\text{cov}(v_R, v_z)}{R} [1 - \gamma_{\nu, R} - \gamma_{\text{cov}(v_R, v_z), R}]$$

where:

$$\gamma_{Q(x), x} = -\frac{x}{Q(x)} \frac{dQ(x)}{dx}$$

- The surface mass density is approximated by:

$$\Sigma(z) \approx \frac{|F_z(z)|}{2\pi G}$$

The vertical force equation & dark matter

- Near the mid-plane, the baryonic surface density is expected to be dominant over a possible DM surface density.
- Therefore, to constrain a DM density we need to probe up to sufficiently large galactic heights.

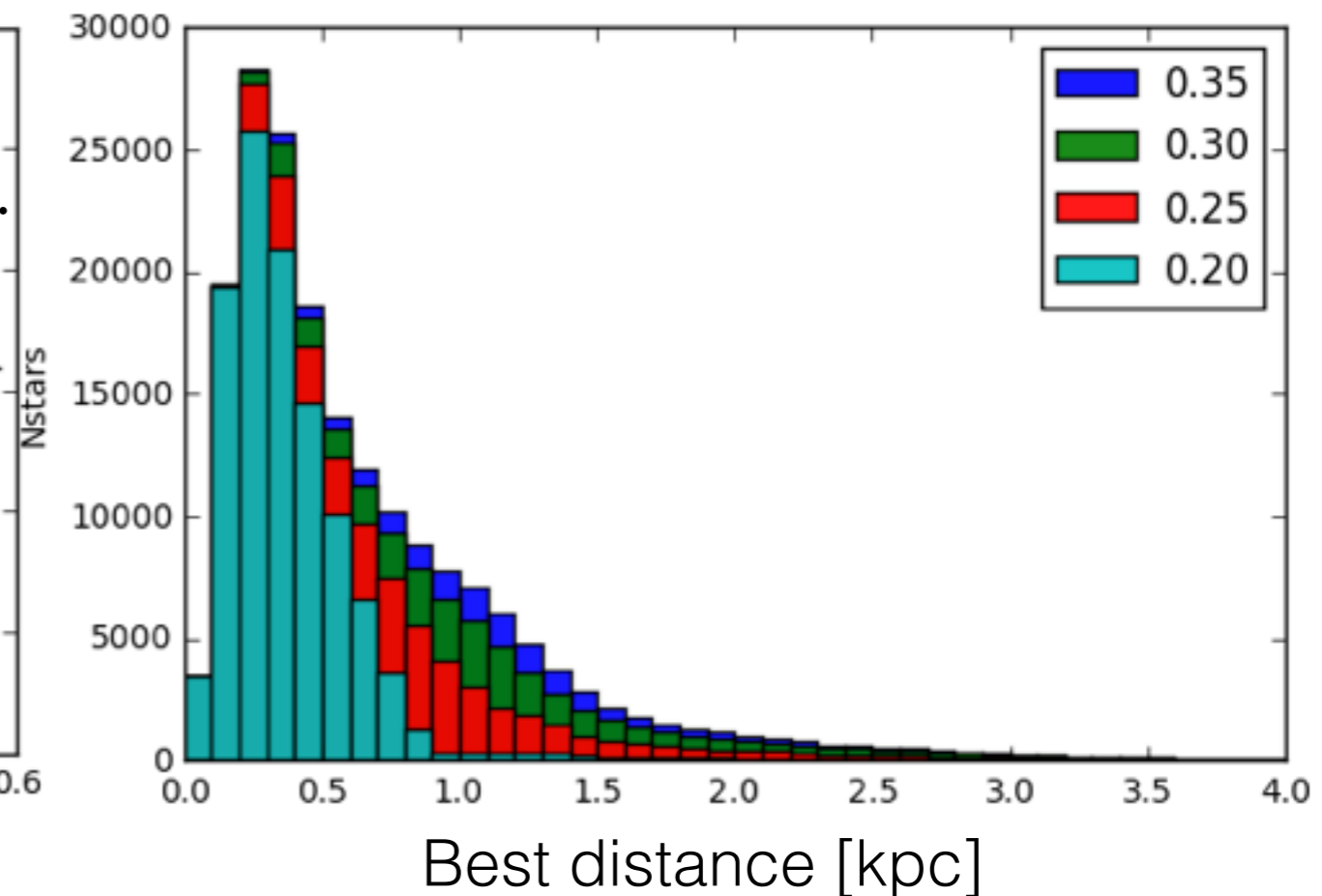
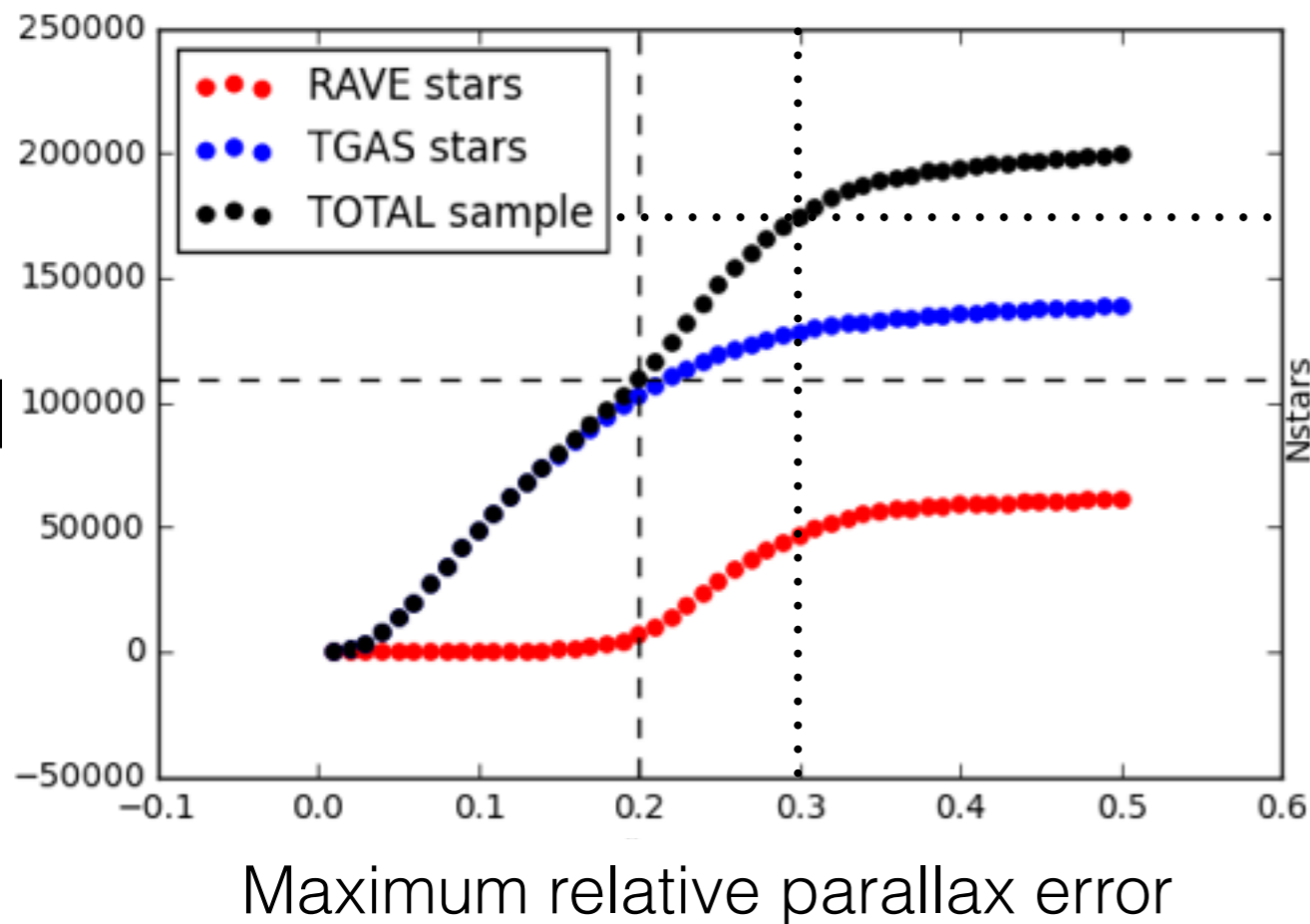


Data



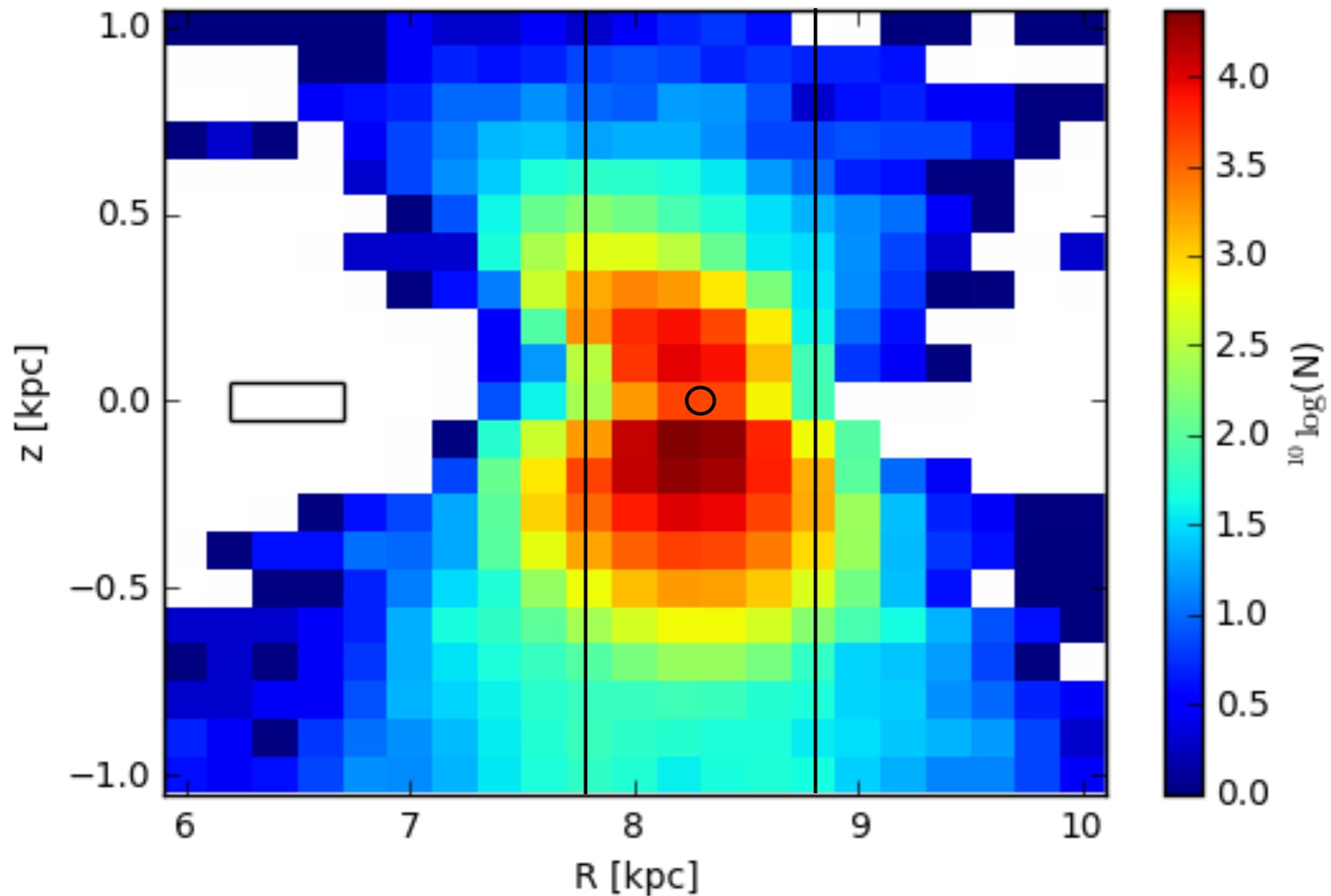
- TGASxRAVE = 6D phase-space information for about 200.000 stars!
- Selection Criteria:
parallax > 0
parallax_error / parallax < 0.2
- Parallaxes are either taken from TGAS or from RAVE DR5: the measurement with the best relative error on the parallax is used.
 - RAVE radial velocities if:
eHRV < 8 km/s
CorrelationCoeff > 10
 - RAVE distances only if:
ALGO_CONV != 1
SNR > 20

The effect of the maximum relative parallax errors on the sample



- We choose a maximum of 20% relative distance error

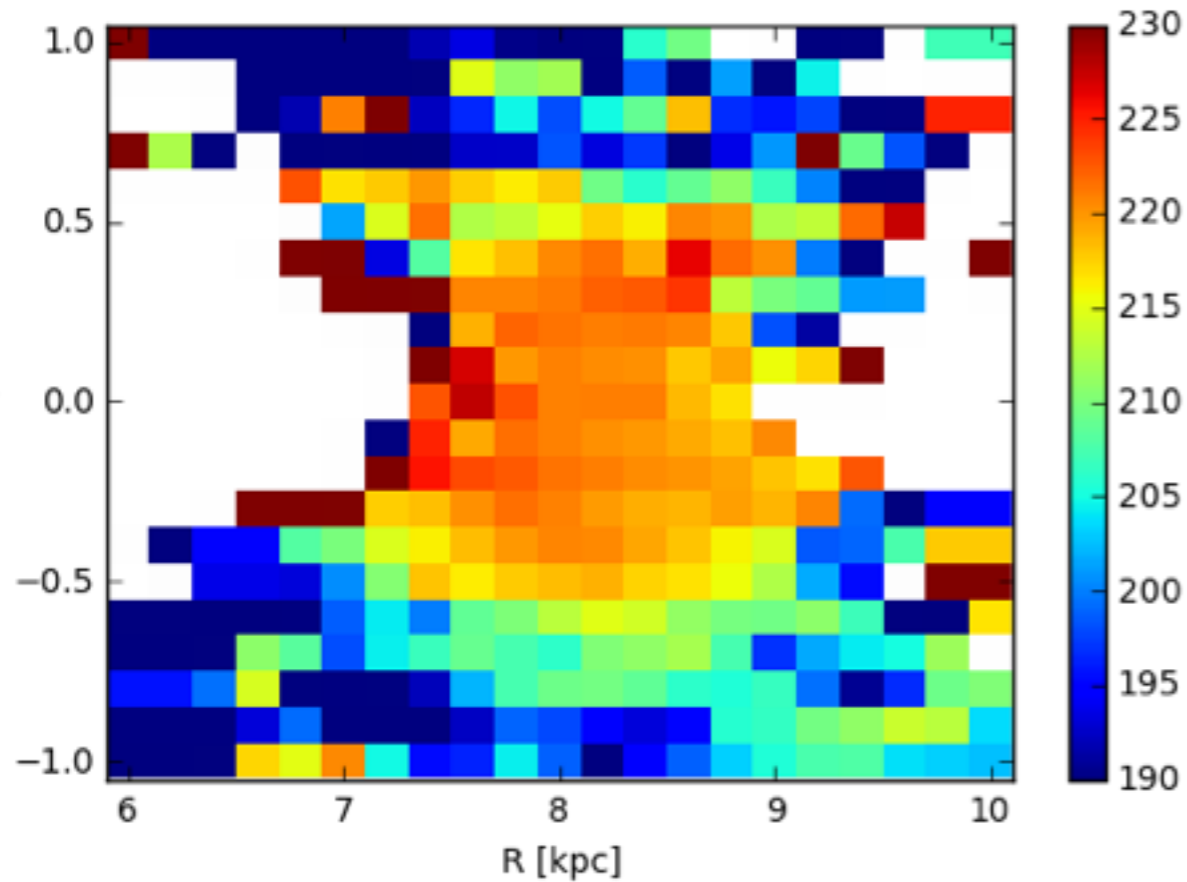
Distribution of stars in our sample



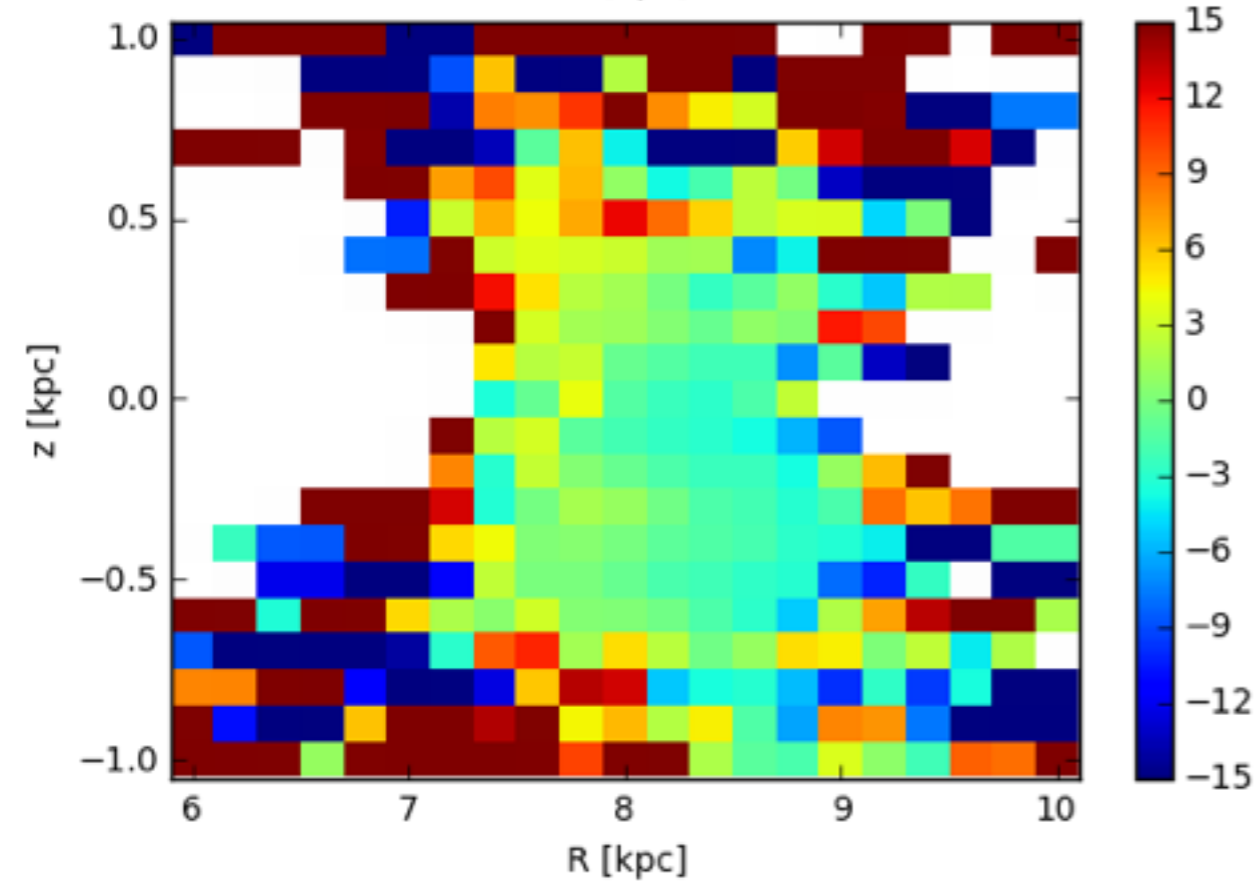
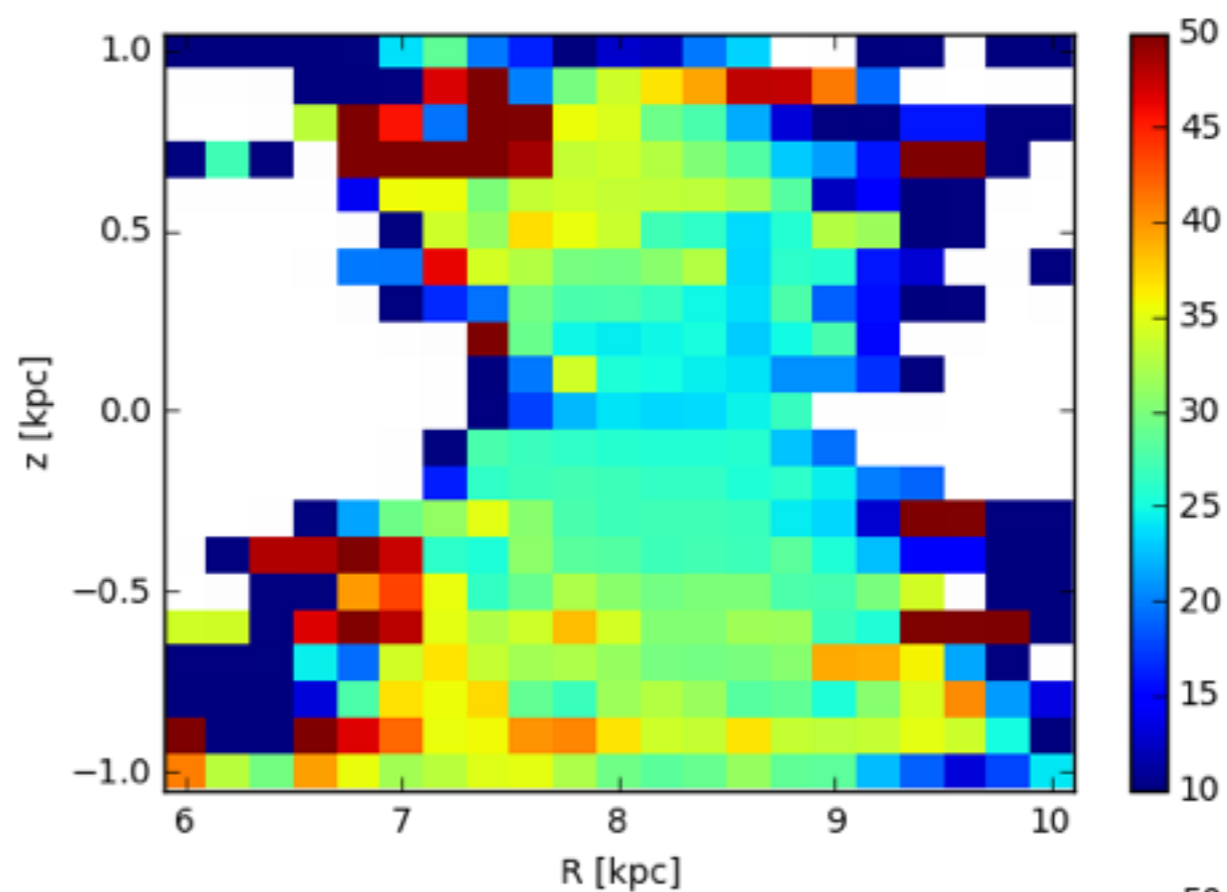
20% parallax error sample: ~ 110000 stars
30% parallax error sample: ~ 175000 stars

Sun at $R = 8.3$ kpc & $z = +14$ pc
 $v_{\text{LSR}} = 228.5$ km/s
 $(U, V, W) = (11.1, 12.24, 7.25)$ km/s

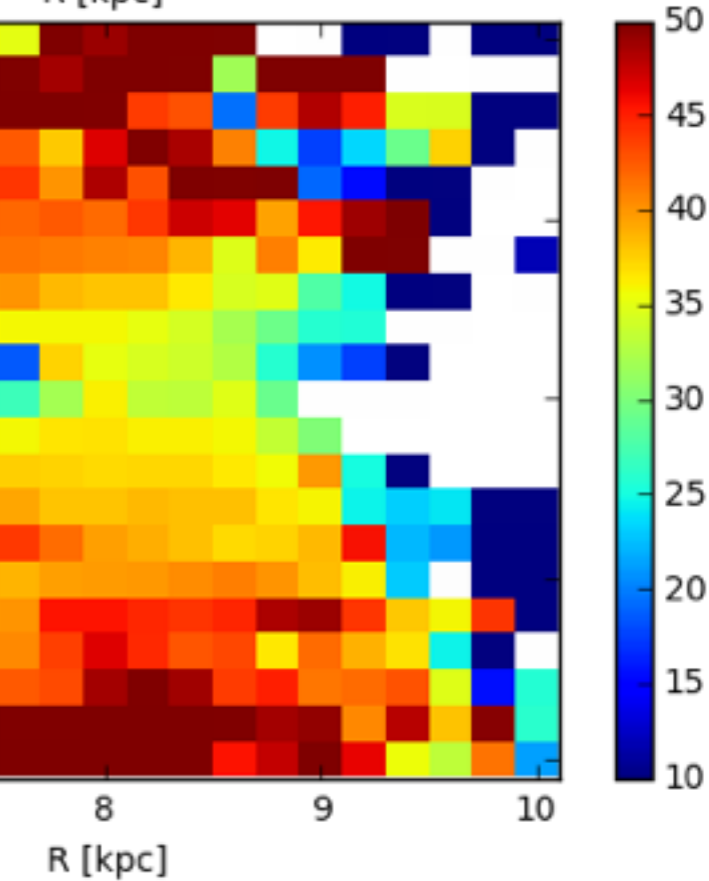
$$\langle v_\phi \rangle$$



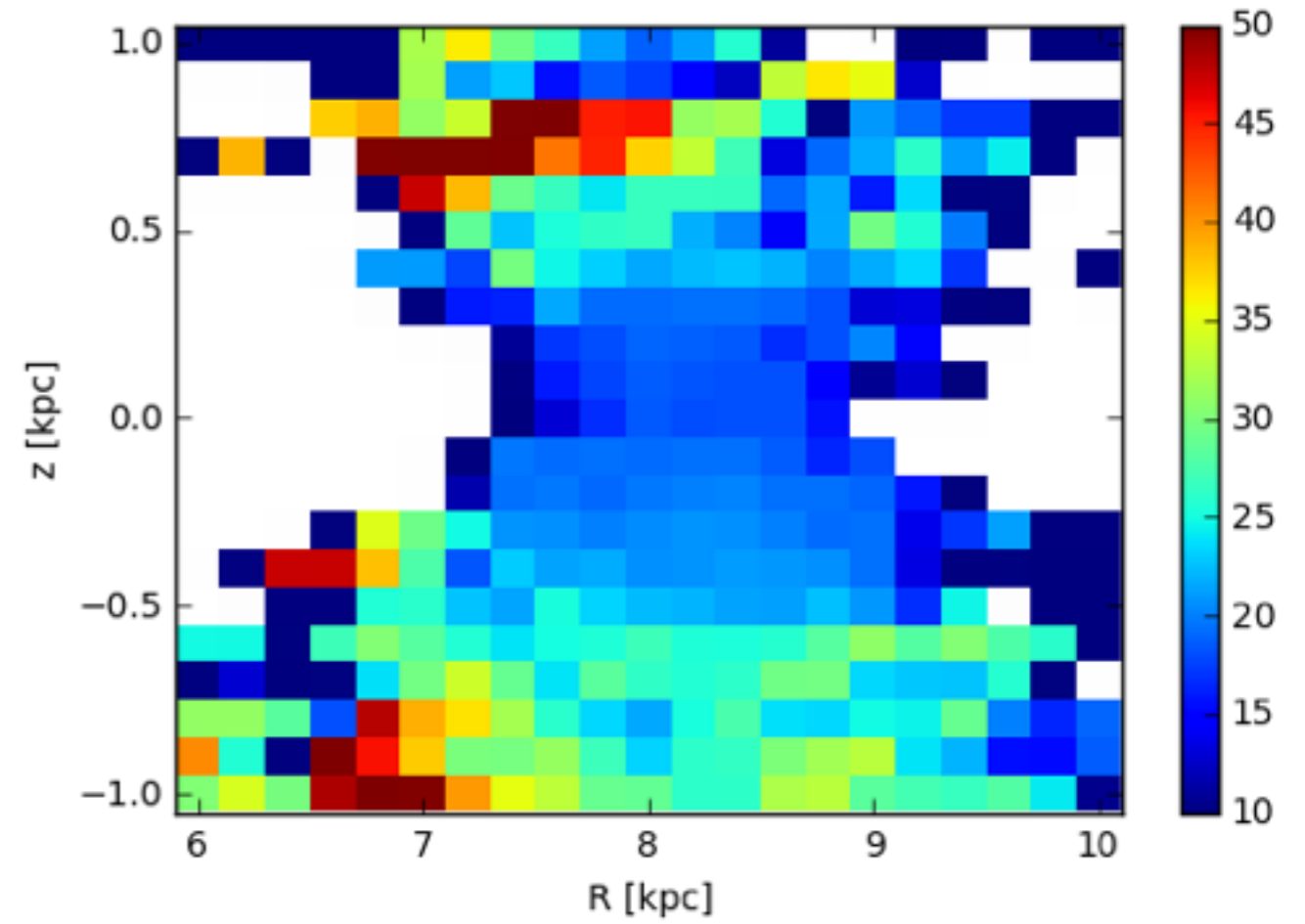
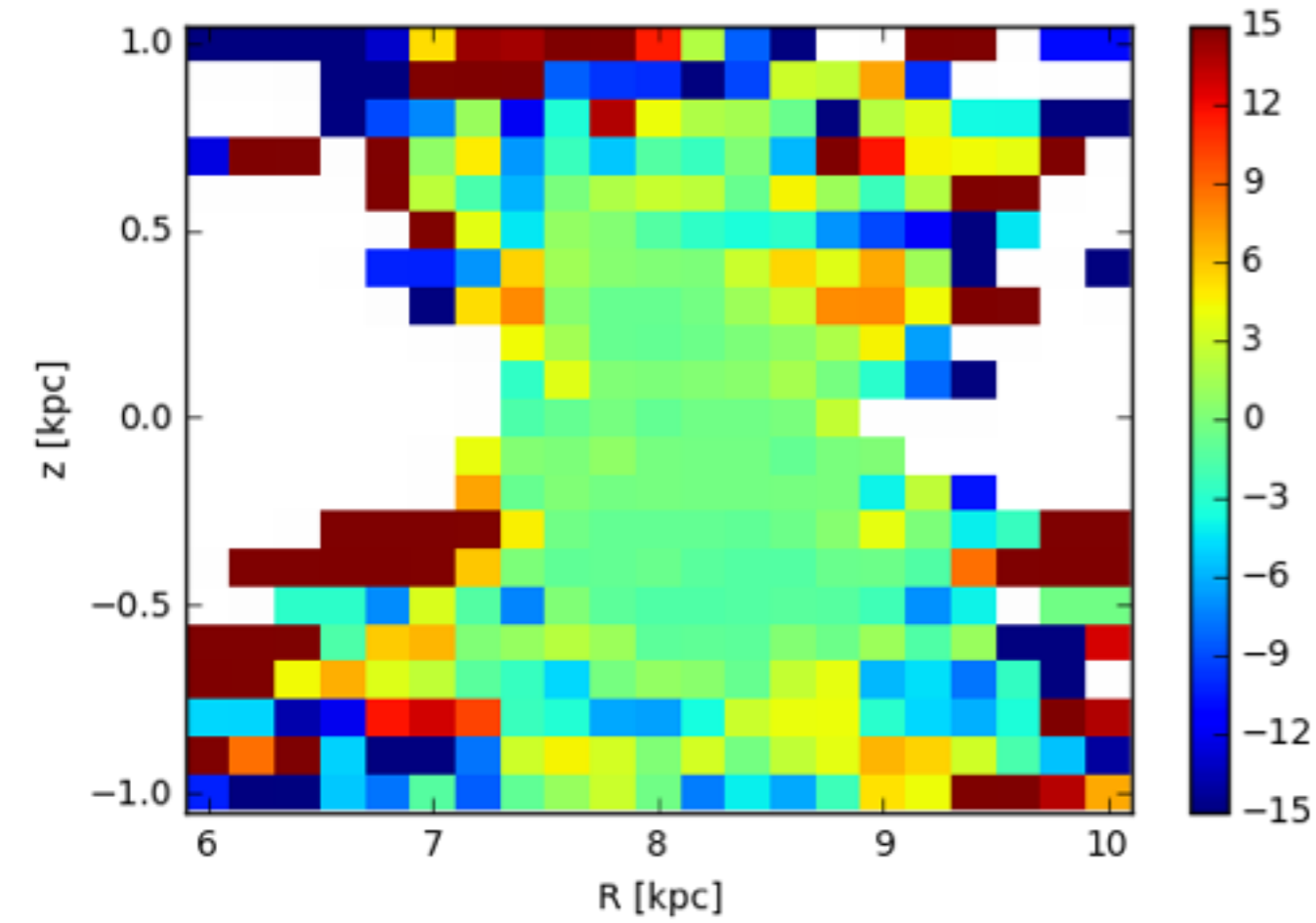
$$\sigma(v_\phi)$$



$$\langle v_R \rangle$$

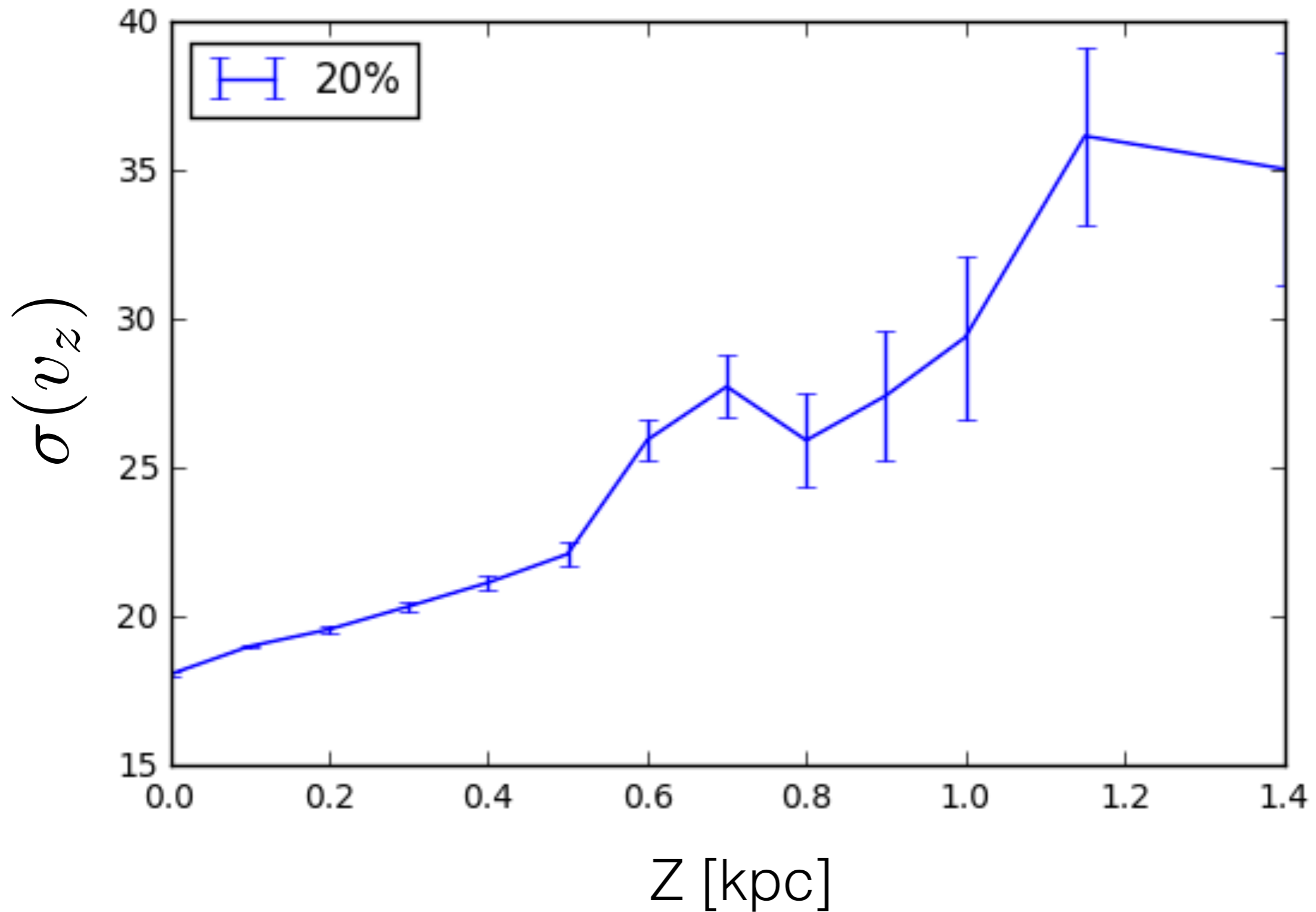


$$\sigma(v_R)$$

$\langle v_z \rangle$ $\sigma(v_z)$ 

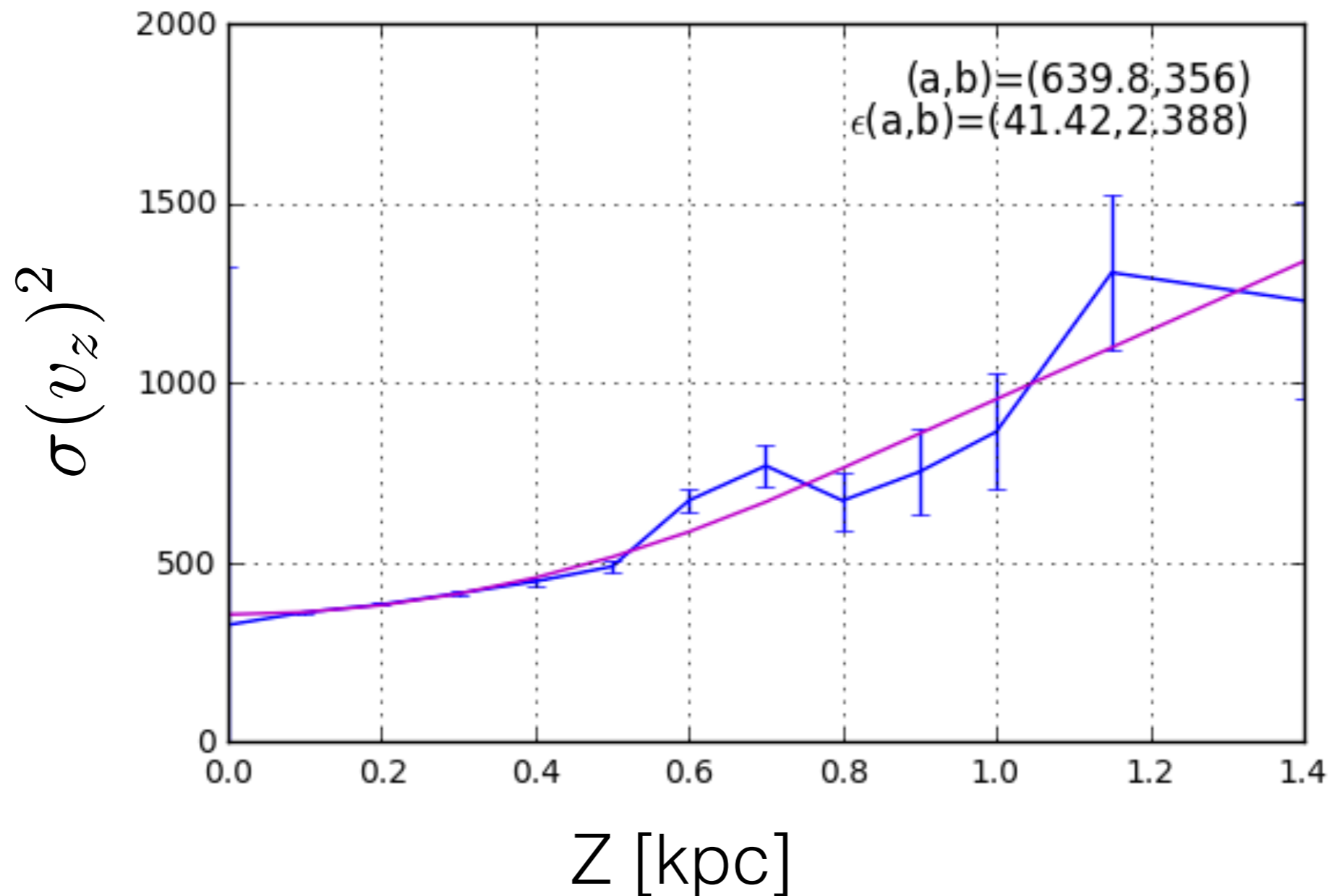
$$-\frac{d\Phi}{dz} \equiv F_z = \frac{\sigma_z^2}{\nu} \frac{d\nu}{dz} + \frac{d\sigma_z^2}{dz} + \frac{\text{cov}(v_R, v_z)}{R} \left[1 - \gamma_{\nu, R} - \gamma_{\text{cov}(v_R, v_z), R} \right]$$

Vertical velocity dispersion at the solar radius.



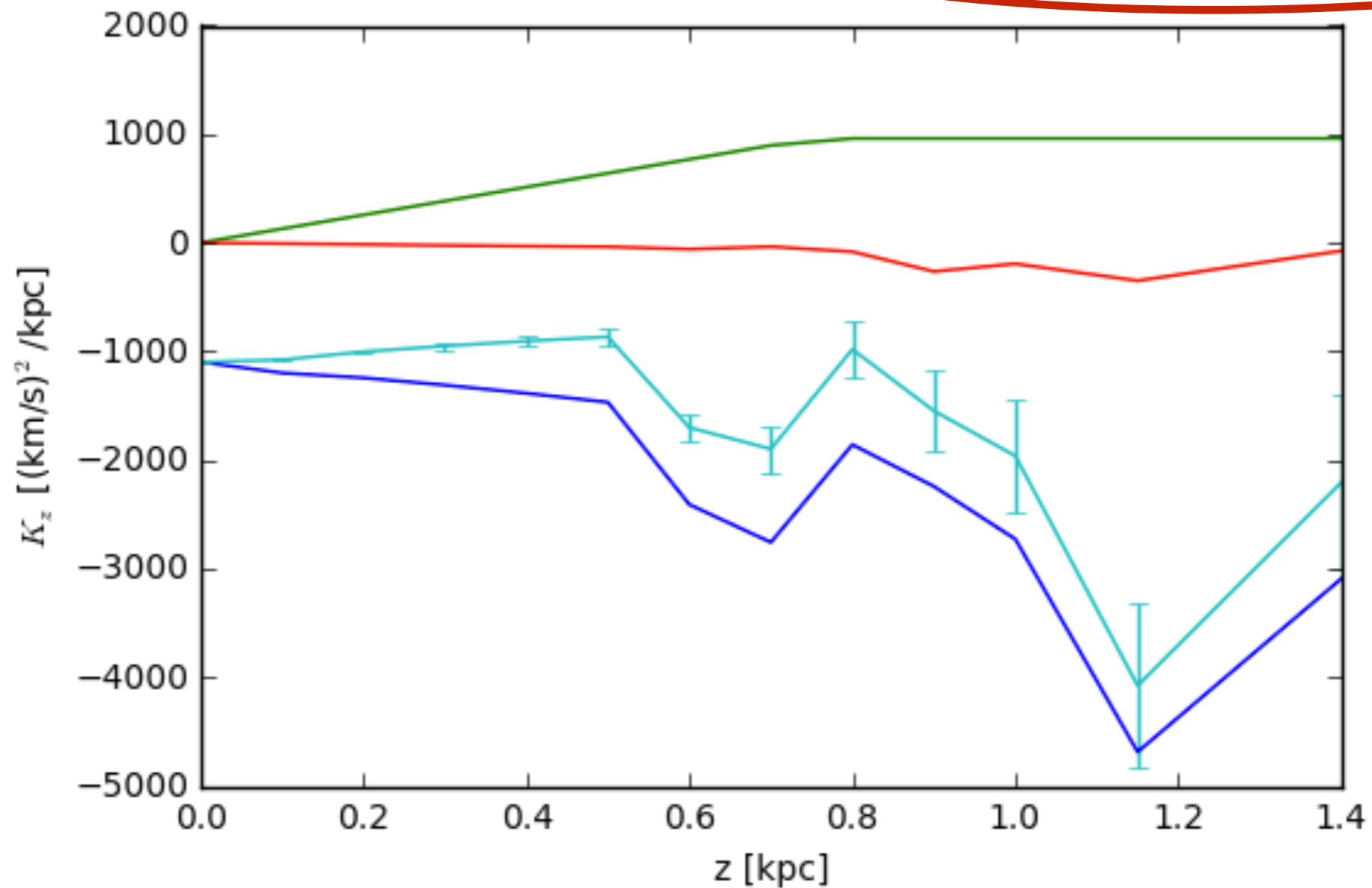
The vertical dispersion profile

$$-\frac{d\Phi}{dz} \equiv F_z = \frac{\sigma_z^2}{\nu} \frac{d\nu}{dz} + \frac{d\sigma_z^2}{dz} + \frac{\text{cov}(v_R, v_z)}{R} [1 - \gamma_{\nu, R} - \gamma_{\text{cov}(v_R, v_z), R}]$$

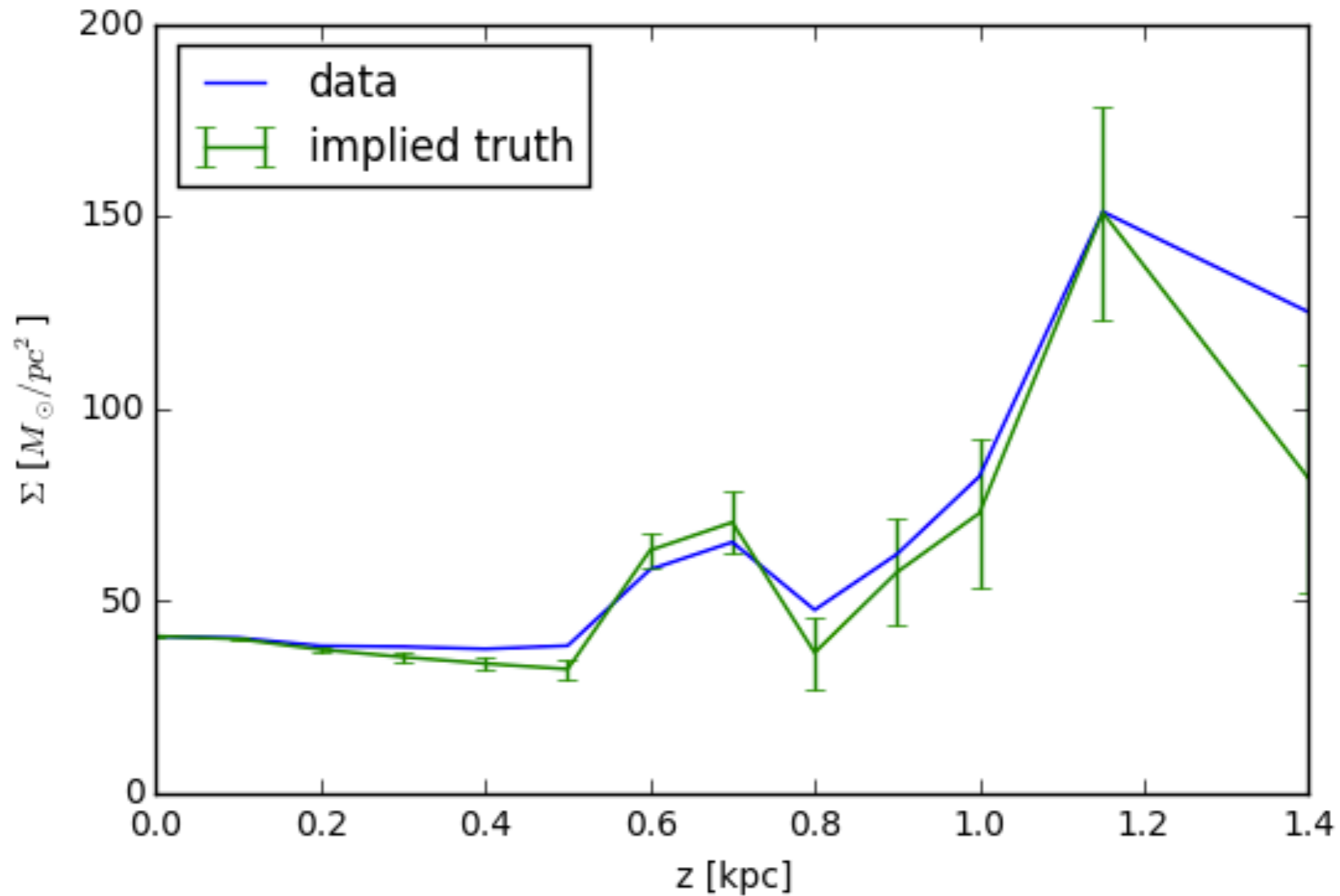


Contribution of the individual terms

$$-\frac{d\Phi}{dz} \equiv F_z = \frac{\sigma_z^2}{\nu} \frac{d\nu}{dz} + \frac{d\sigma_z^2}{dz} + \frac{\text{COV}(v_R, v_z)}{R} [1 - \gamma_{\nu, R} - \gamma_{\text{COV}(v_R, v_z), R}]$$



The implied surface mass density



$$\Sigma(z) \approx \frac{|F_z(z)|}{2\pi G}$$

Mass model

- We model the stellar contribution in the solar neighbourhood by a single disk:

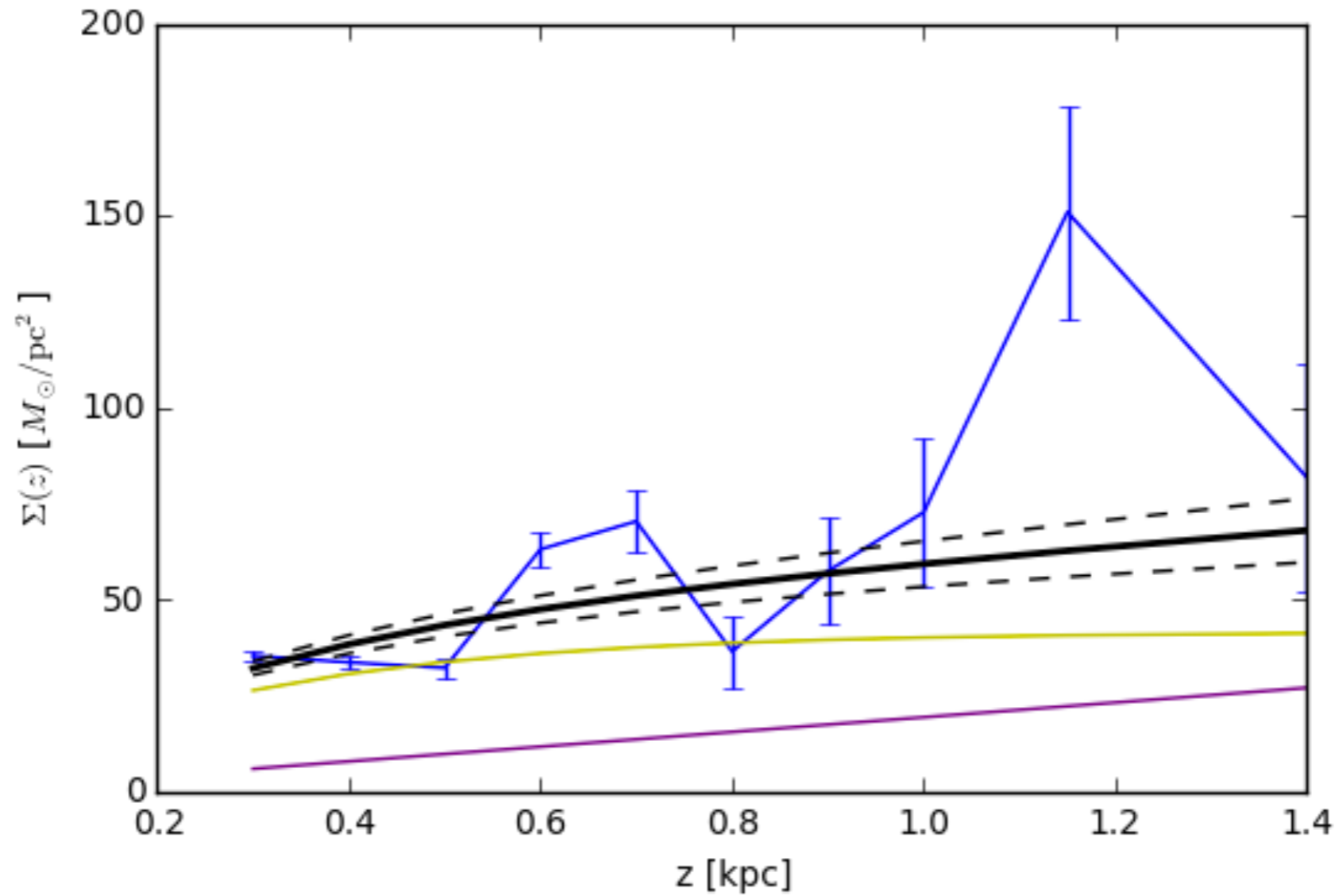
$$M_{\text{disk}} = 4.5 \times 10^{10} M_{\odot}$$

$$h_R = 2.5 \text{ kpc}$$

$$h_z = 0.3 \text{ kpc}$$

- We allow for a dark matter component by assuming a constant dark matter density.

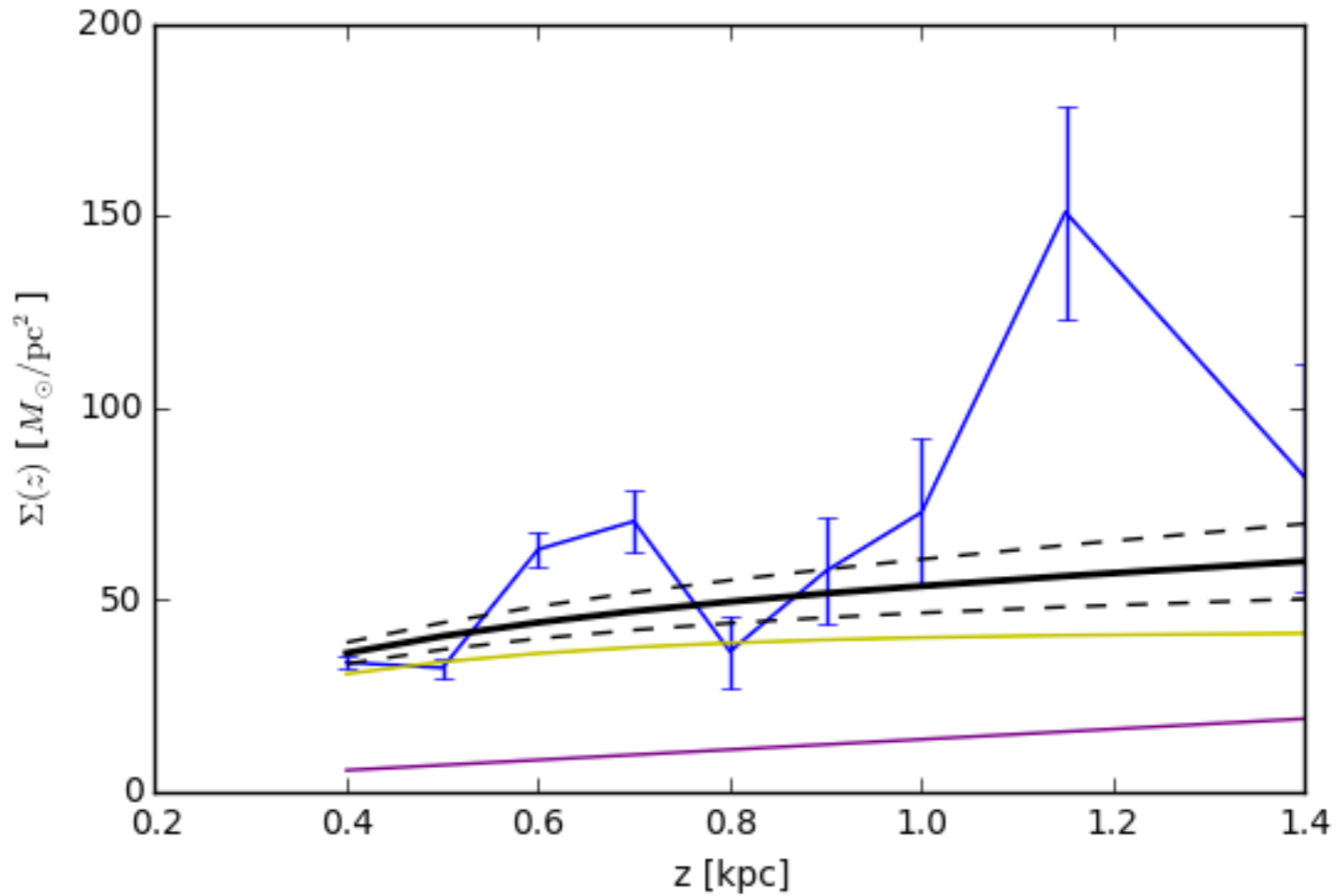
Mass models



$$\rho_{DM}(R = R_{\odot}, z = 0) = 0.010 M_{\odot}/\text{pc}^3$$

$$\text{error}(\rho_{DM, R_{\odot}}) = 0.003 M_{\odot}/\text{pc}^3$$

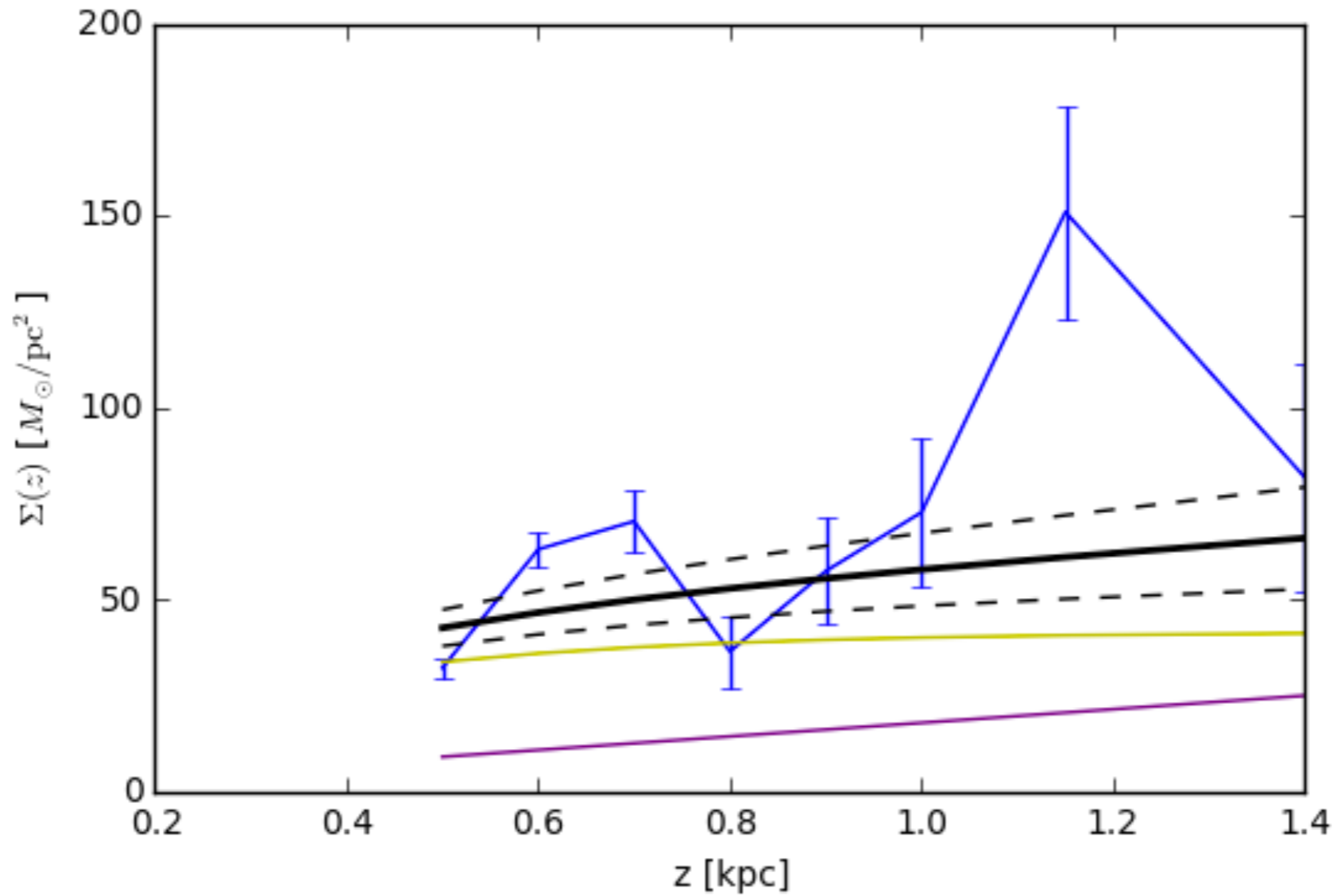
Mass models



$$\rho_{DM}(R = R_{\odot}, z = 0) = 0.007 M_{\odot}/\text{pc}^3$$

$$\text{error}(\rho_{DM, R_{\odot}}) = 0.003 M_{\odot}/\text{pc}^3$$

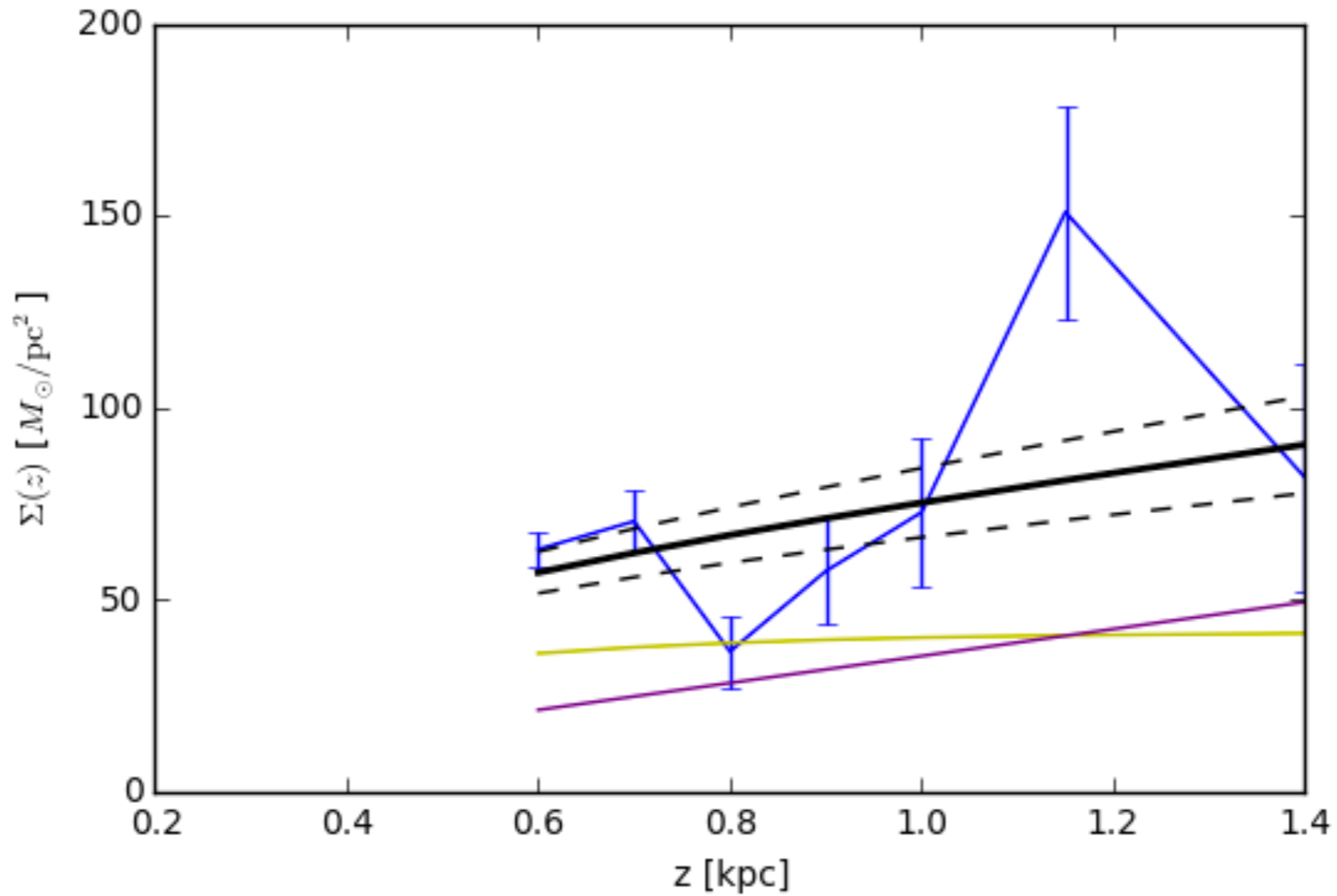
Mass models



$$\rho_{DM}(R = R_{\odot}, z = 0) = 0.009 M_{\odot}/\text{pc}^3$$

$$\text{error}(\rho_{DM, R_{\odot}}) = 0.005 M_{\odot}/\text{pc}^3$$

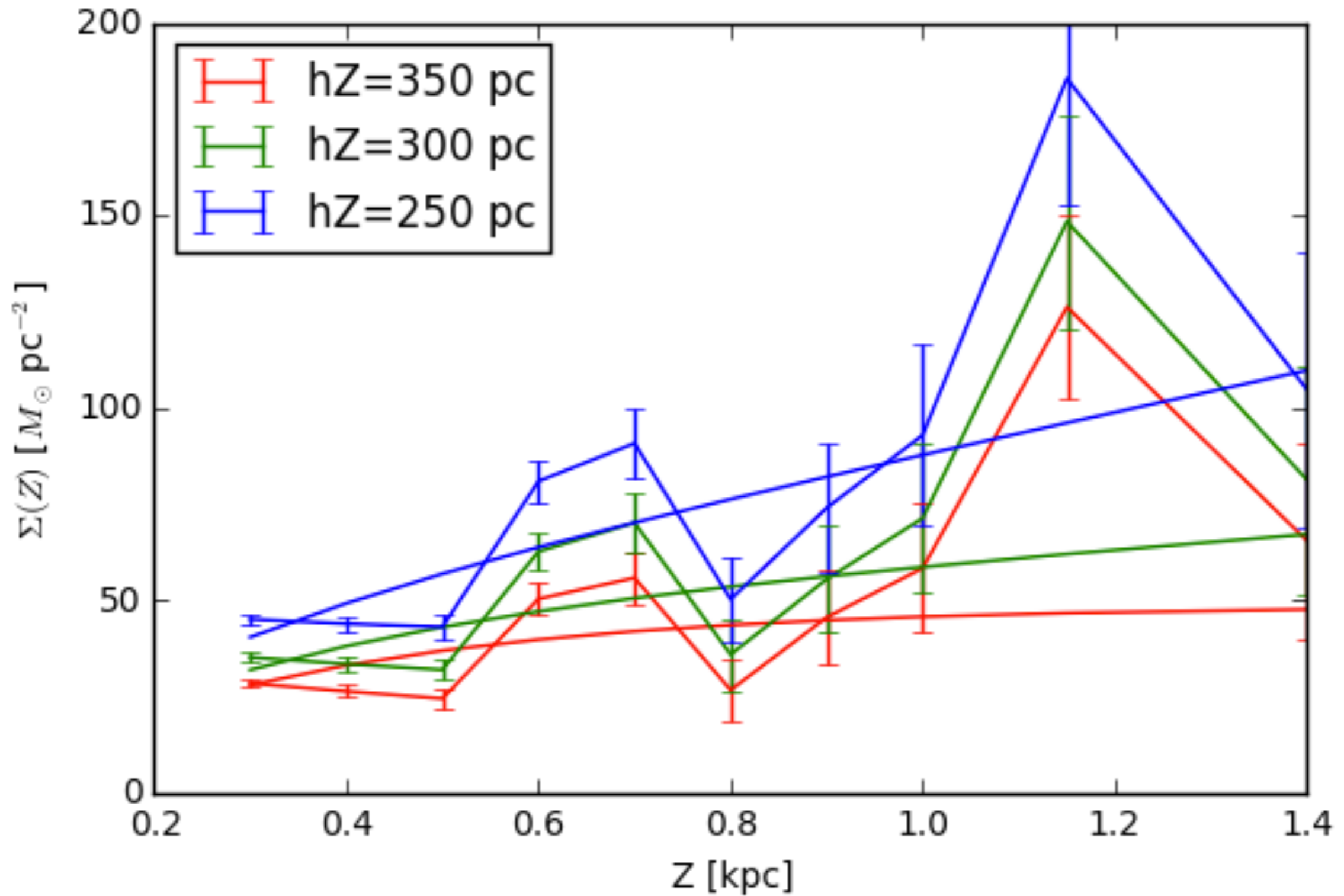
Mass models



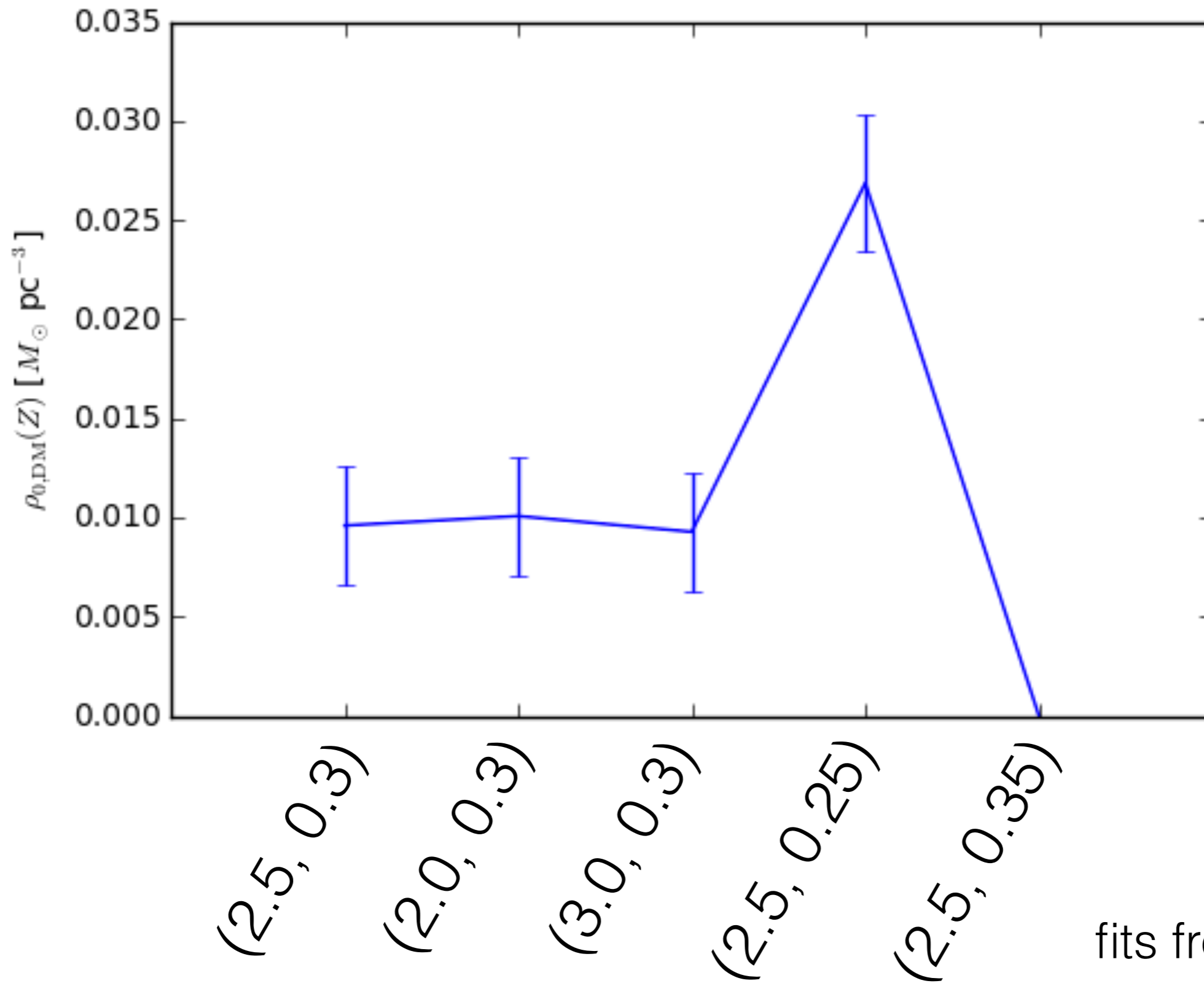
$$\rho_{DM}(R = R_{\odot}, z = 0) = 0.018 M_{\odot}/\text{pc}^3$$

$$\text{error}(\rho_{DM, R_{\odot}}) = 0.005 M_{\odot}/\text{pc}^3$$

Varying hz

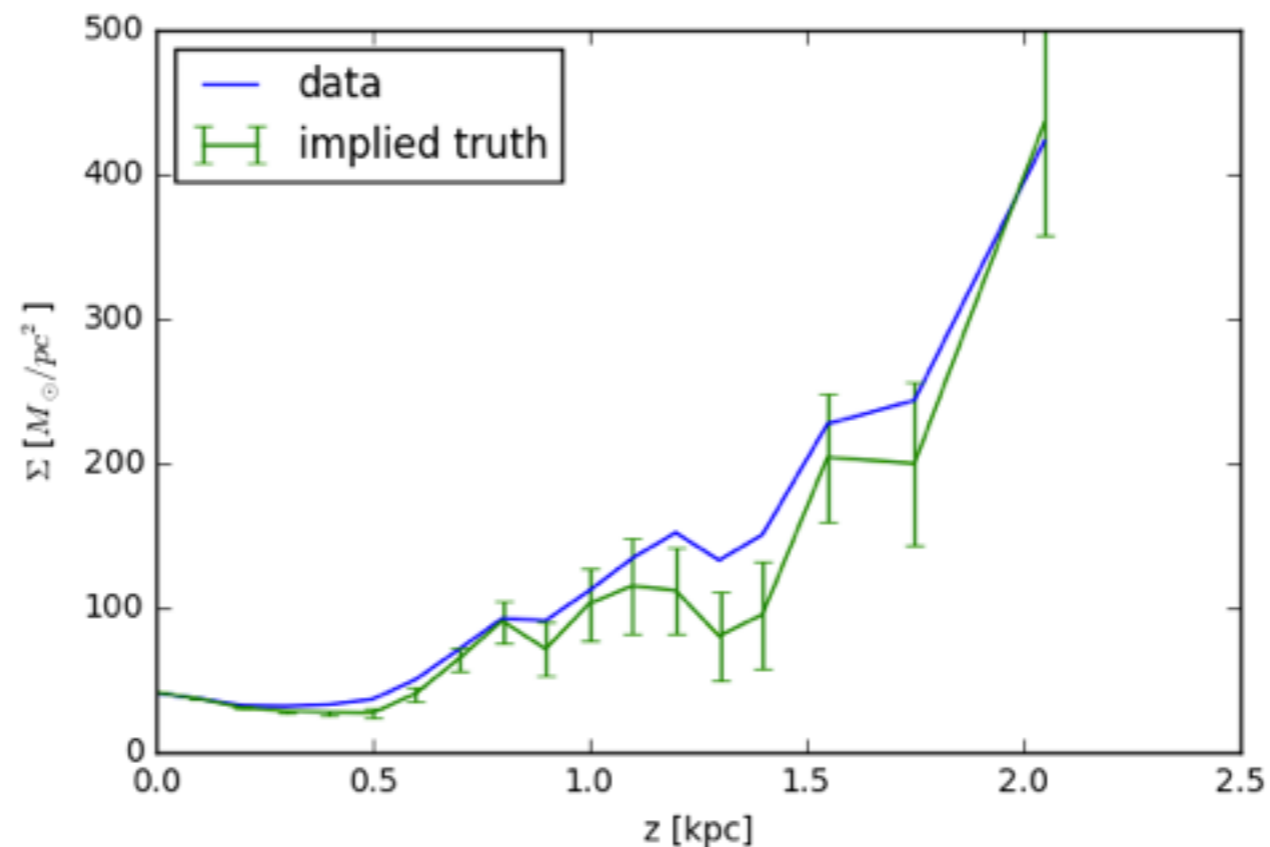
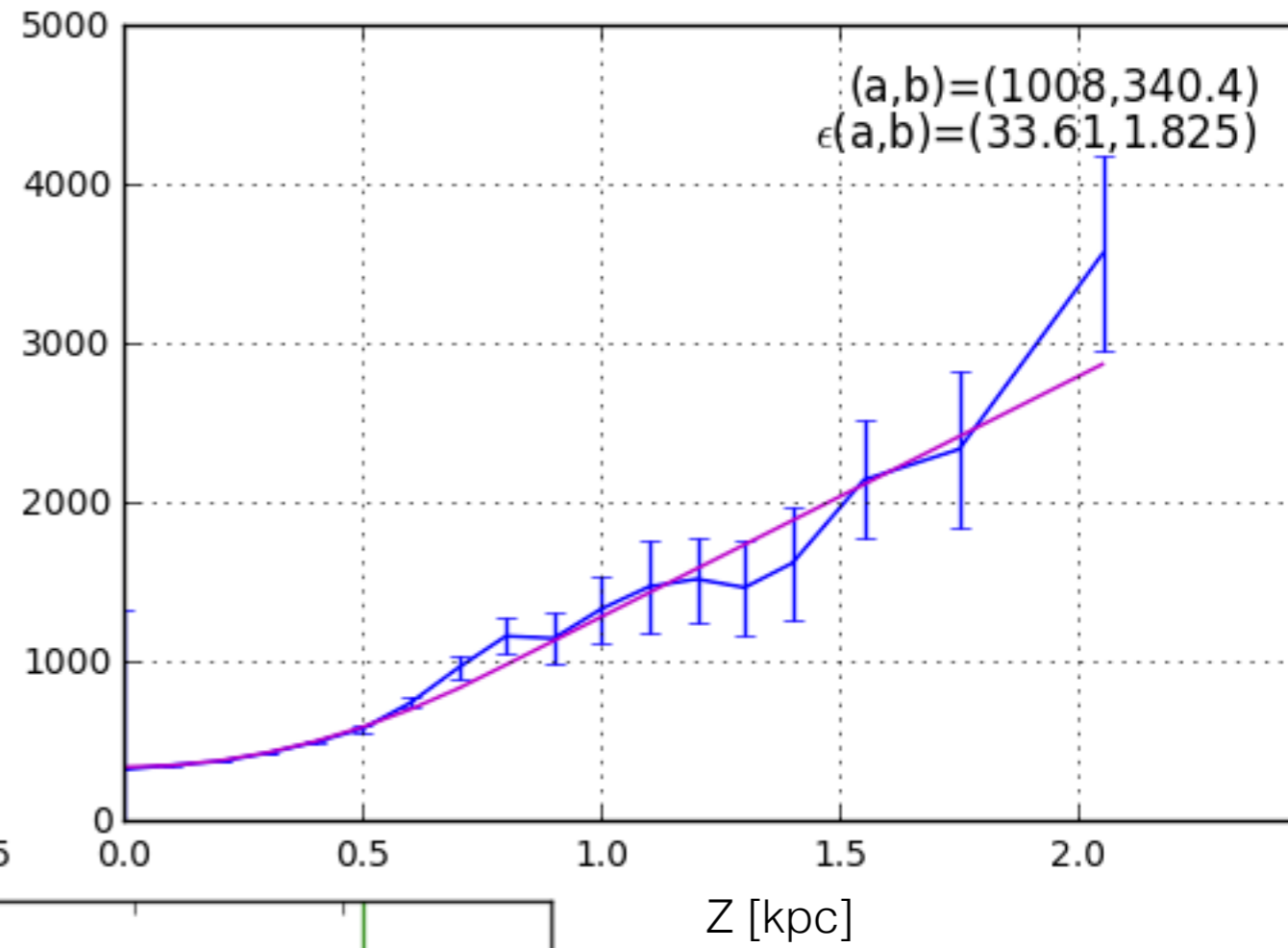
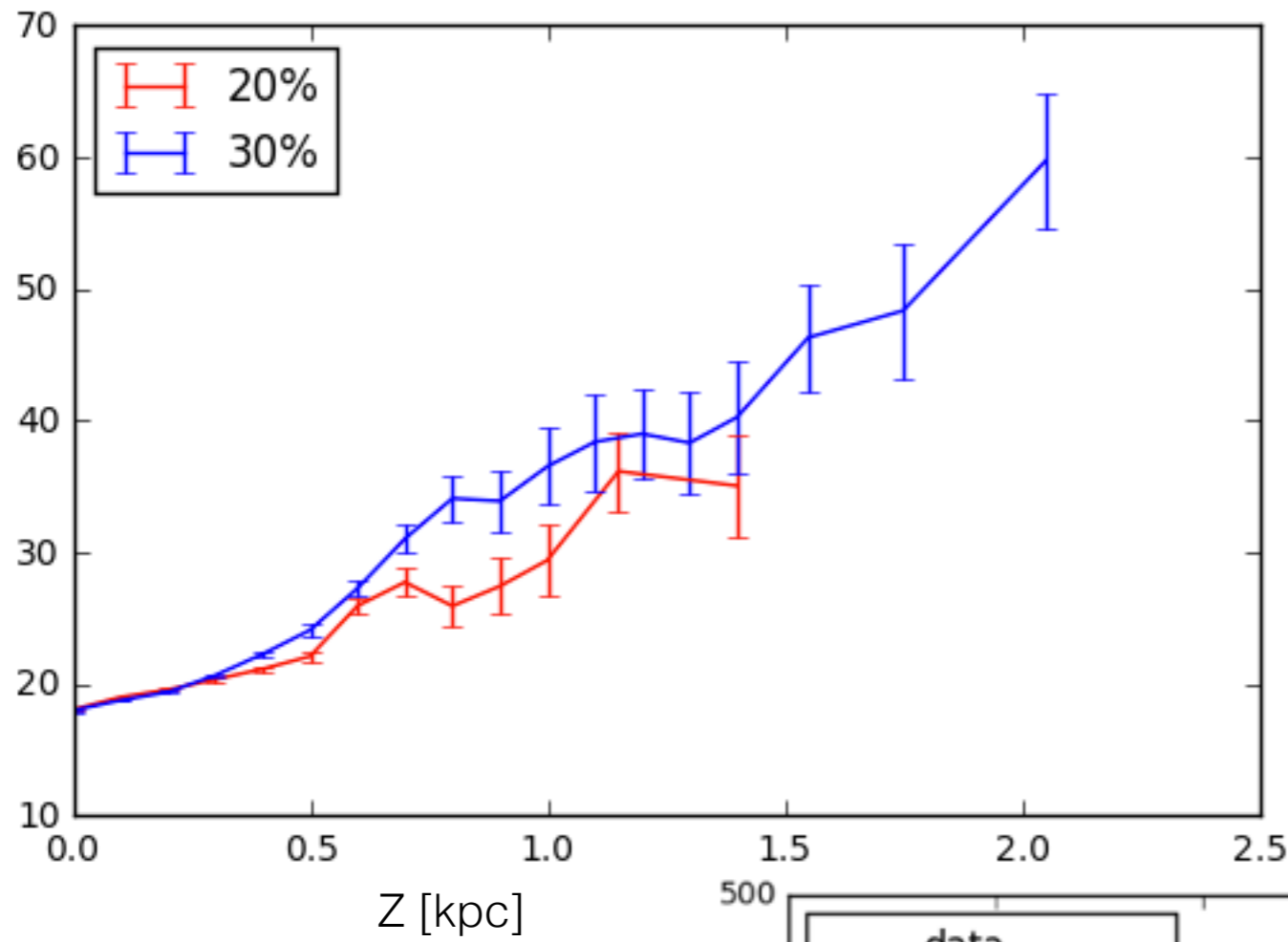


Varying (h_R, h_z)

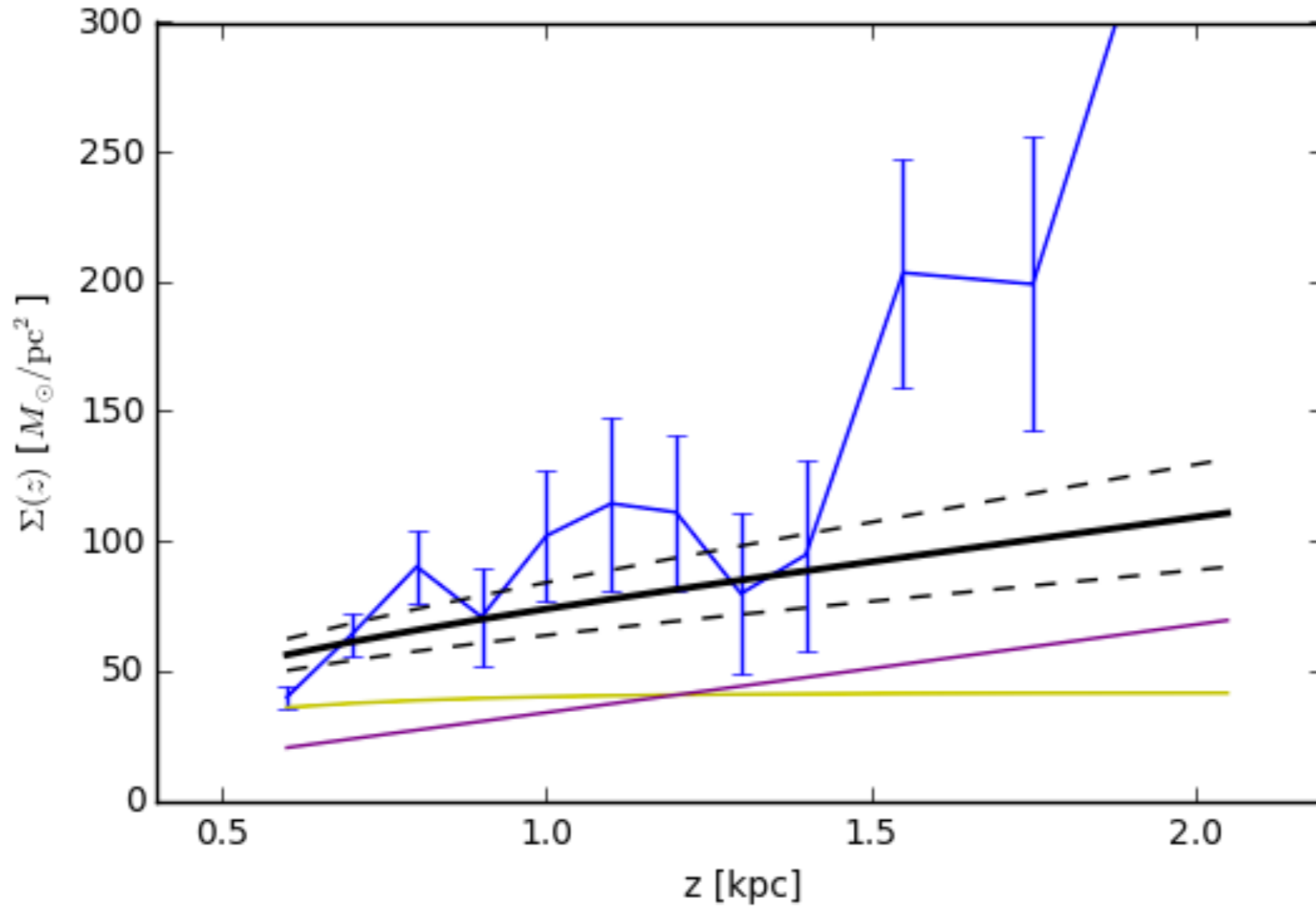


fits from $z=0.3$ kpc

30% parallax error sample



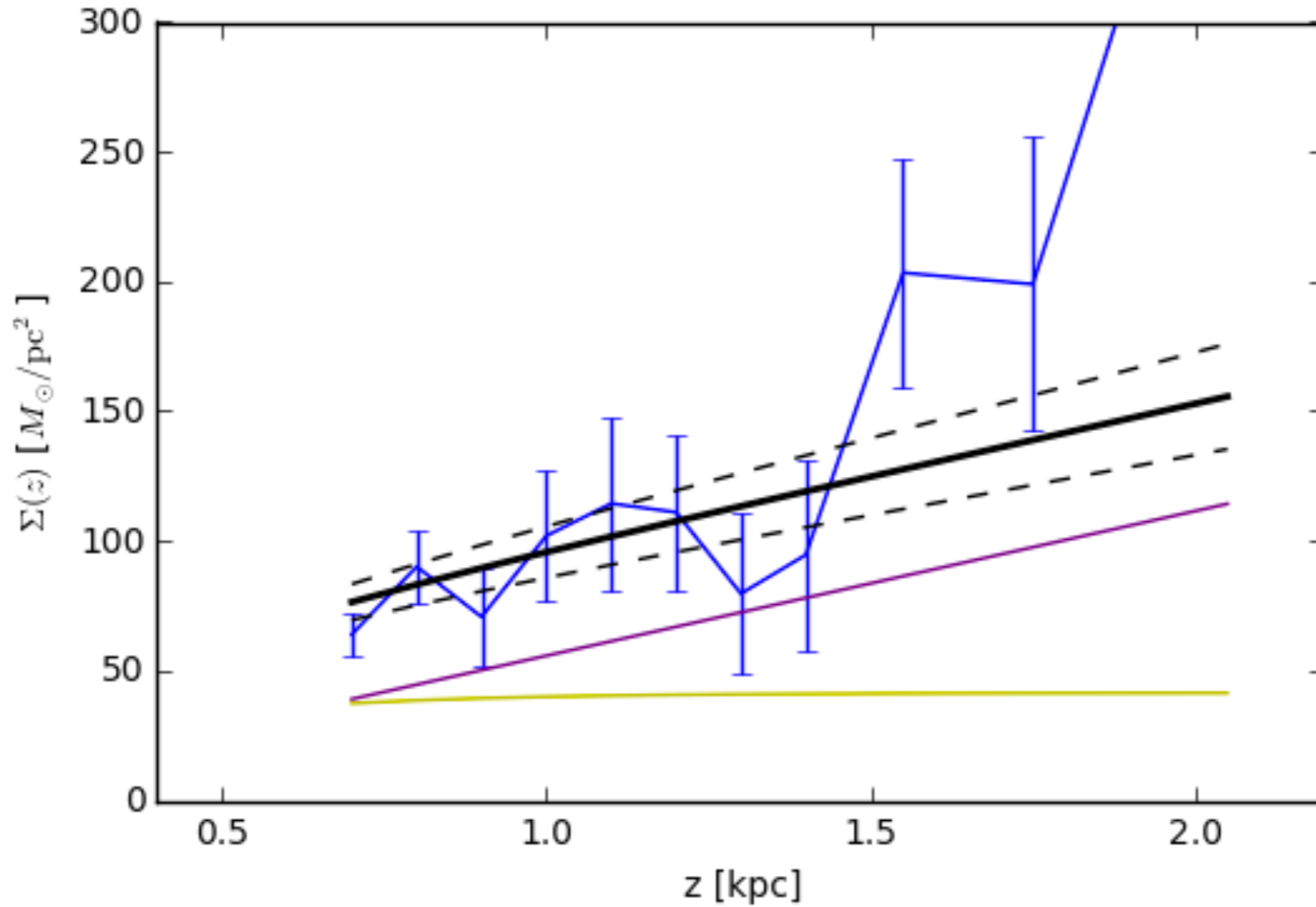
Mass models



$$\rho_{DM}(R = R_{\odot}, z = 0) = 0.017 M_{\odot}/\text{pc}^3$$

$$\text{error}(\rho_{DM, R_{\odot}}) = 0.005 M_{\odot}/\text{pc}^3$$

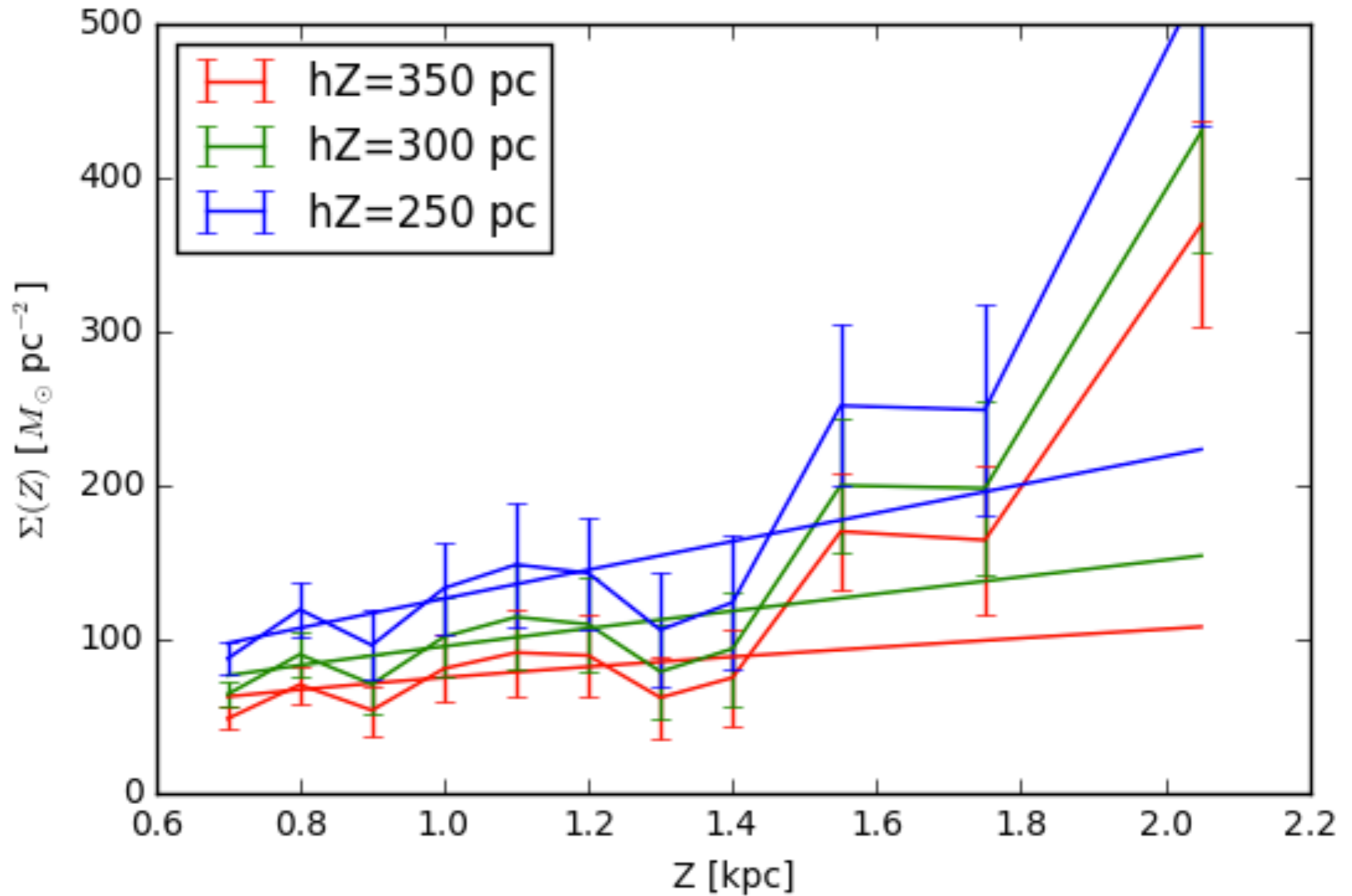
Mass models



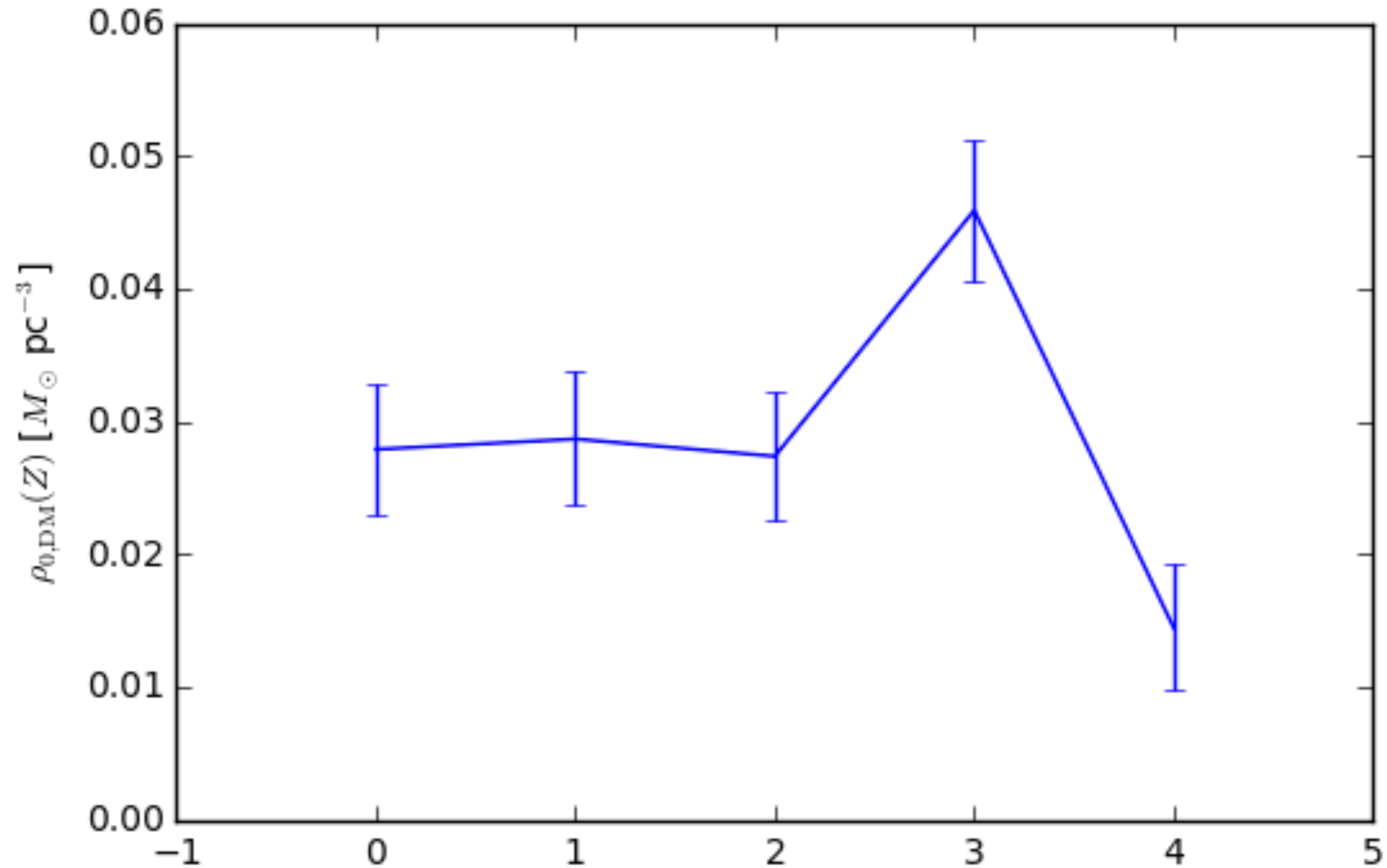
$$\rho_{DM}(R = R_{\odot}, z = 0) = 0.027 M_{\odot}/\text{pc}^3$$

$$\text{error}(\rho_{DM, R_{\odot}}) = 0.005 M_{\odot}/\text{pc}^3$$

Varying hz



Varying (h_R, h_z), 30% sample



(2.5, 0.3)

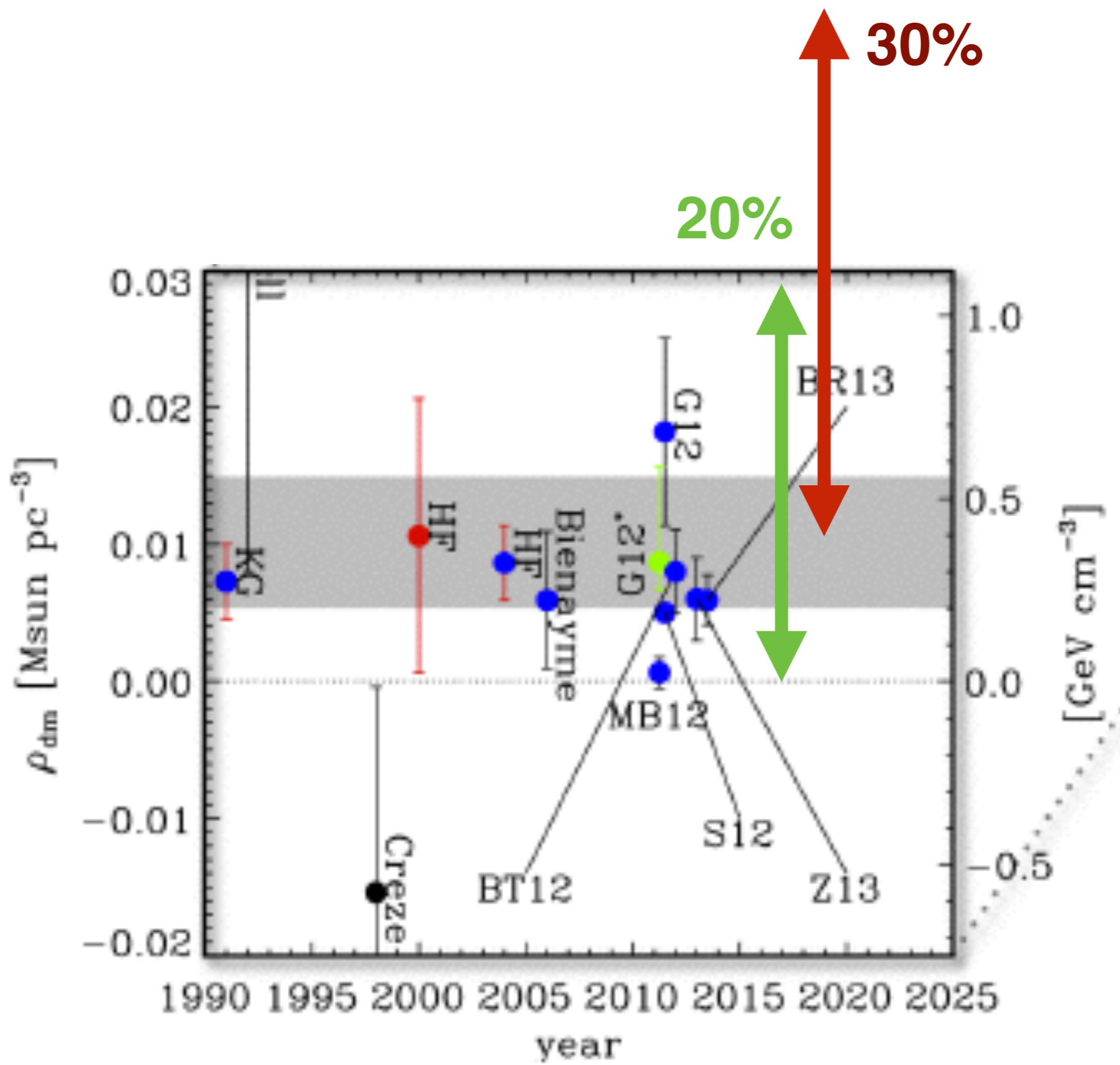
(2.0, 0.3)

(3.0, 0.3)

(2.5, 0.25)

(2.5, 0.35)

fits from $z=0.7$ kpc



Summary

- We attempted to model the DM density by a single disk component.
- We obtain large errors and are looking at the data, to see why we obtain different results.
- Errors on disk parameters can have a significant influence on the implied dark matter density at the solar position.
- Gaia DR2: more & accurate proper motions, distances and radial velocities.

Questions